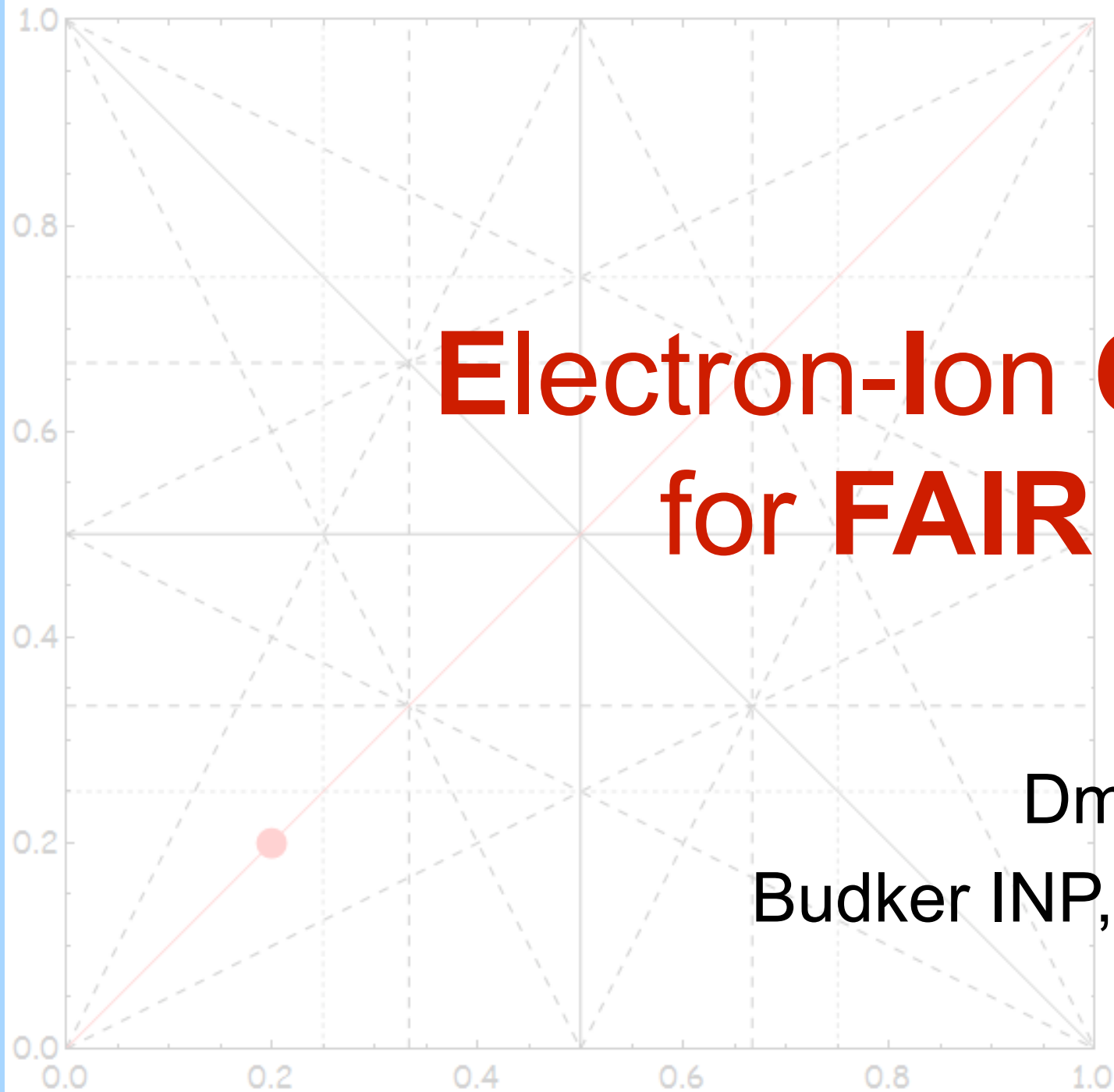


Electron-Ion Collider for FAIR Project

Dmitry Shwartz

Budker INP, Novosibirsk



Outline

- ELISe experiment at Electron-Ion Collider
- EIC overview & parameters
- Interaction Region adopted for fission experiments
- Luminosity approach & limitations
- Emittance of electron beams, changeable emittance
- Chromaticity correction in EAR
- EAR Dynamic Aperture optimization: "best pairs" method.
- NESR (collider mode) DA estimations
- Conclusion

ELISE experiment @ EIC

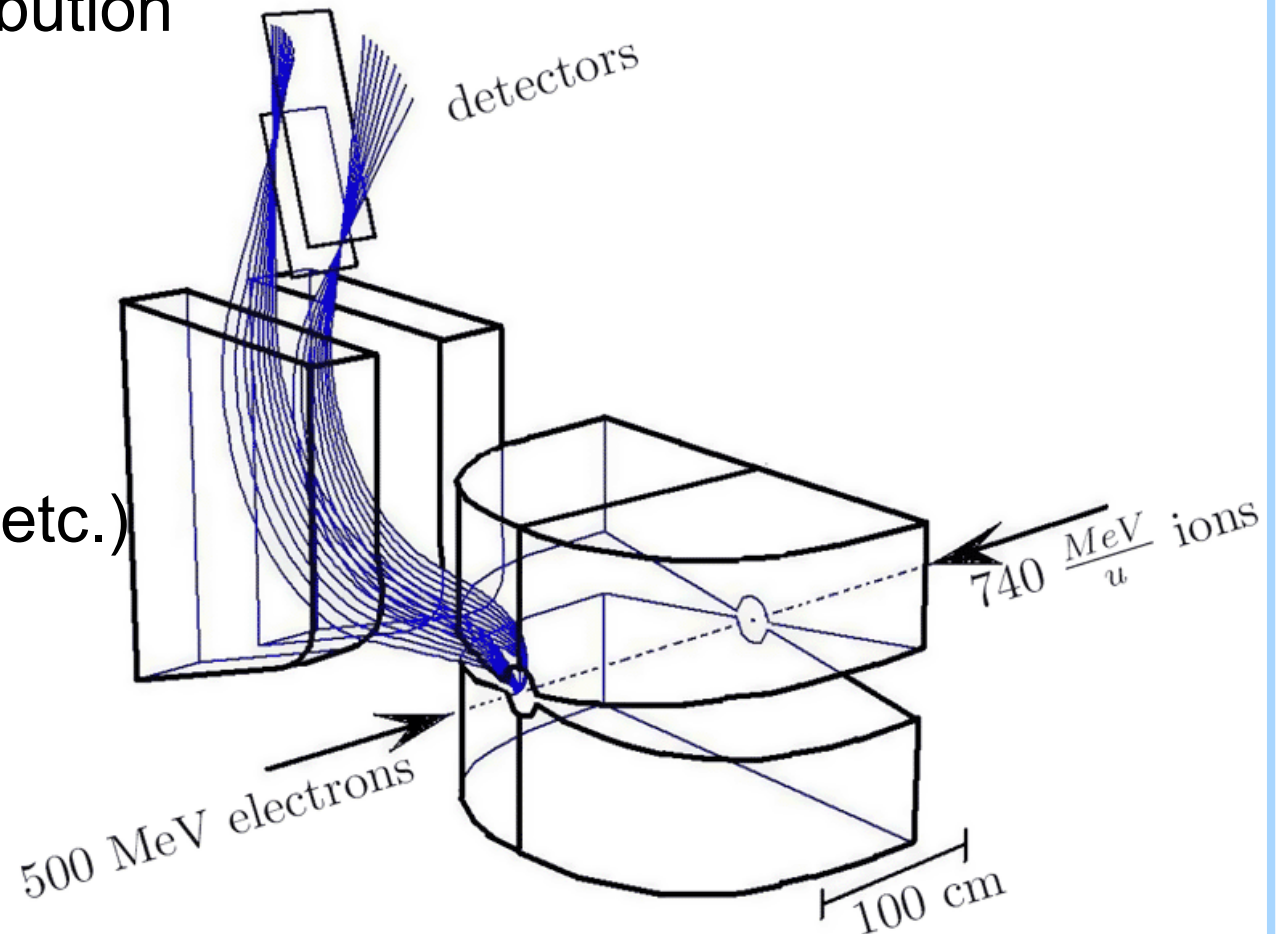
Electrons scattering on the nucleus:

1) elastic (charge distribution of exotic nuclei)

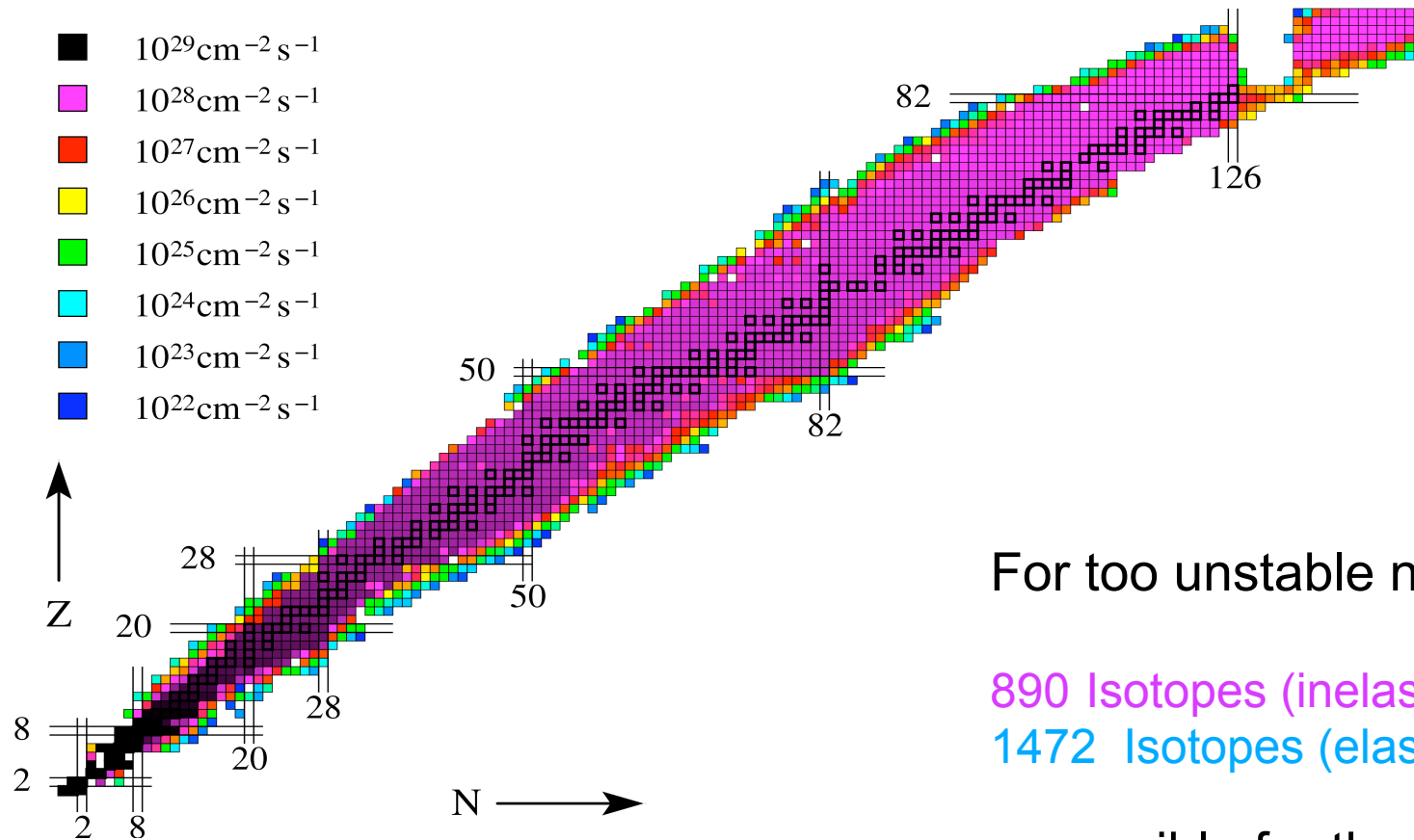
$$L_{\text{req}} \sim 10^{24} \text{cm}^{-2} \text{s}^{-1};$$

2) inelastic (electromagnetic excitations etc.)

$$L_{\text{req}} \sim 10^{28} \text{cm}^{-2} \text{s}^{-1}$$



ELISE mission



For too unstable nuclei ($T_{1/2} < 1\text{d}$)

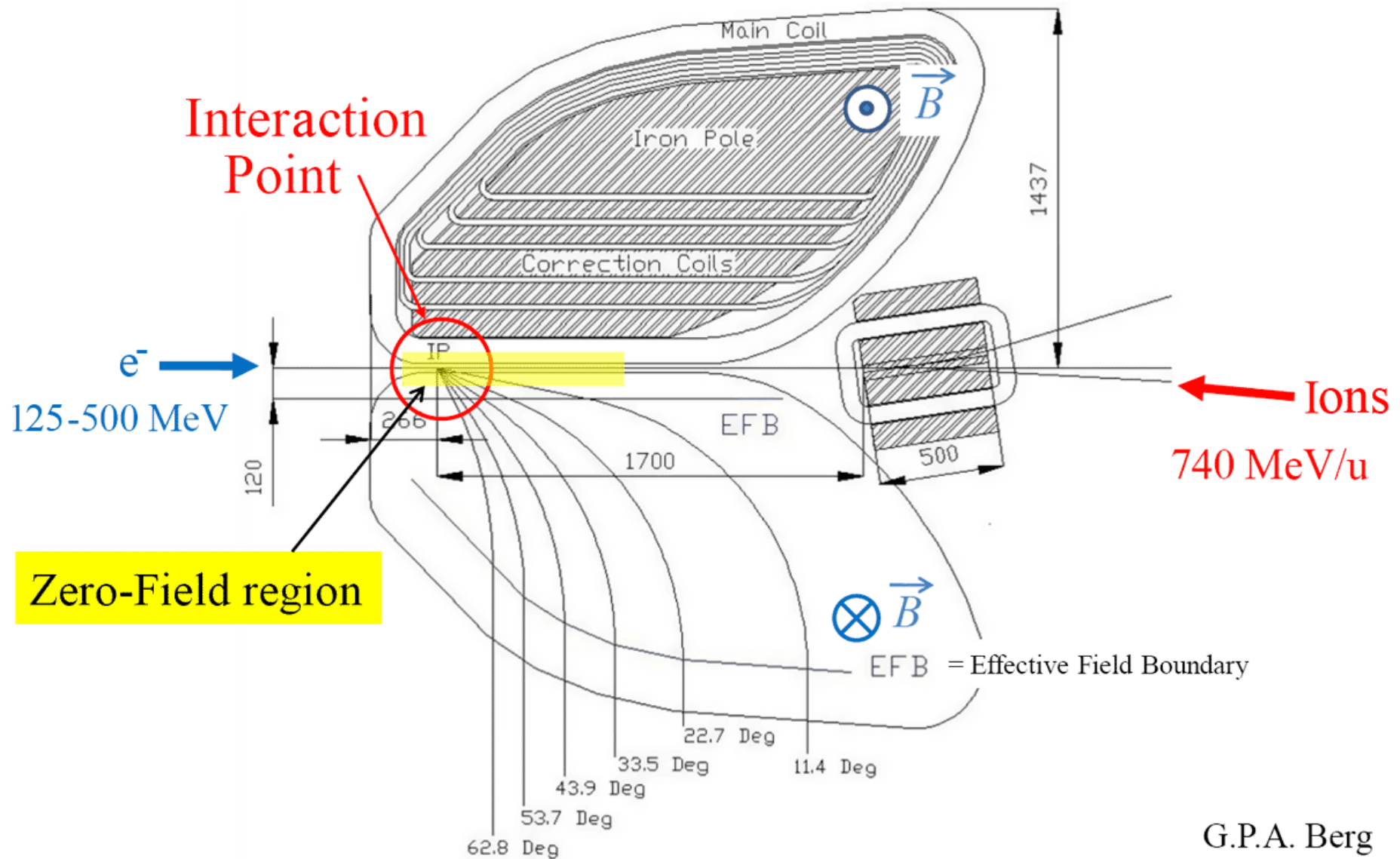
890 Isotopes (inelastic scattering)

1472 Isotopes (elastic scattering)

accessible for the first time!

by H.Simon

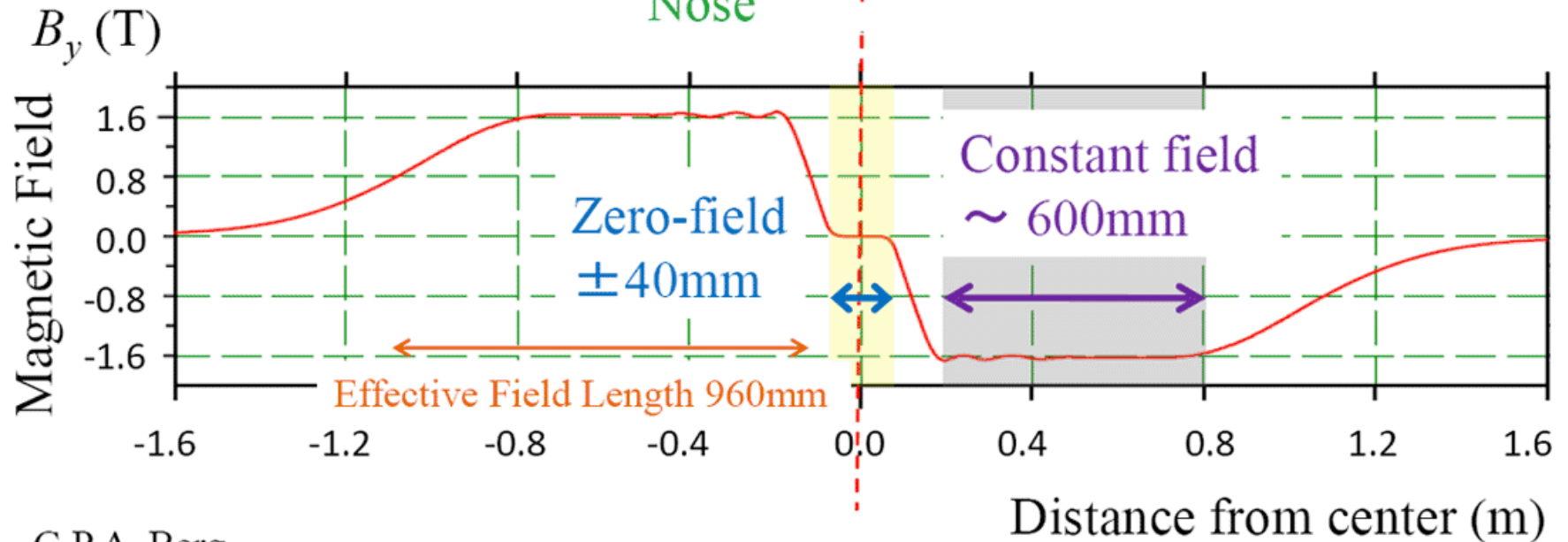
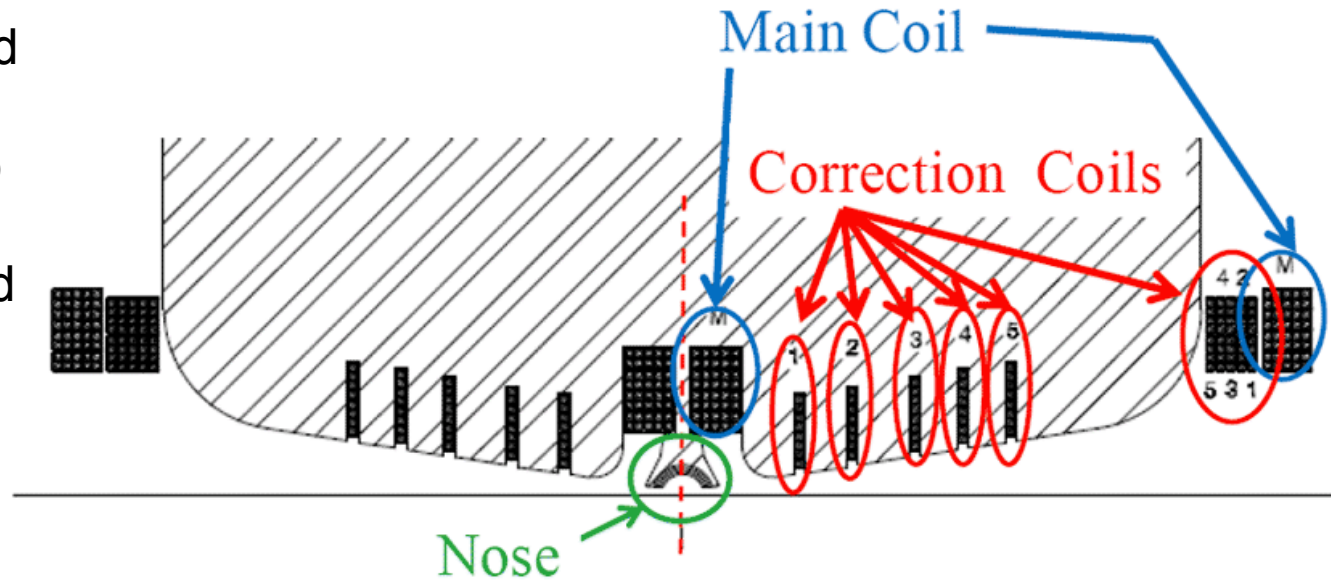
ELISE pre-deflector magnet (“Butterfly”), top view



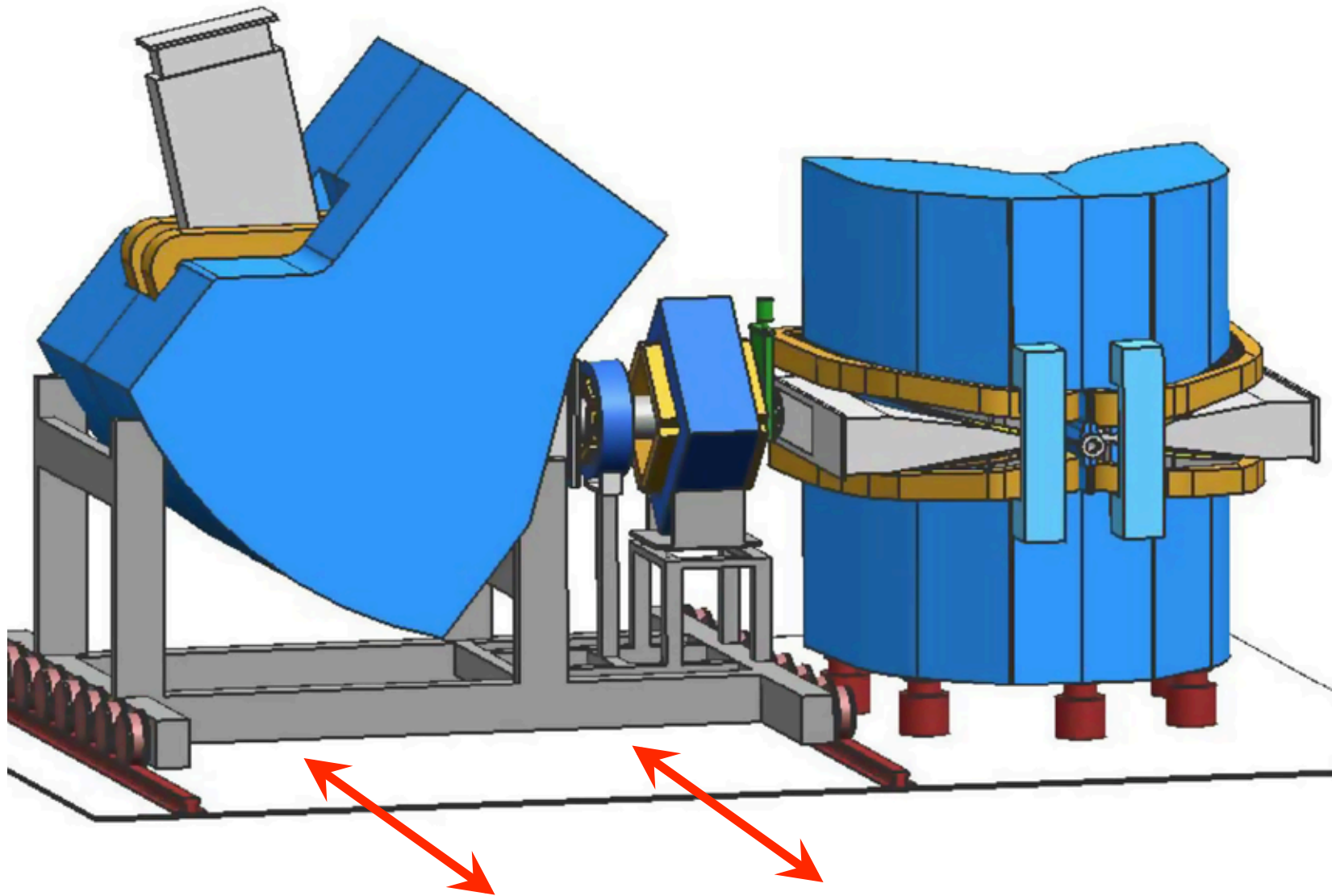
G.P.A. Berg

Butterfly magnet field transverse distribution

Specially designed magnet with expanding gap (to keep wide vertical angle for scattered electrons), but uniform field

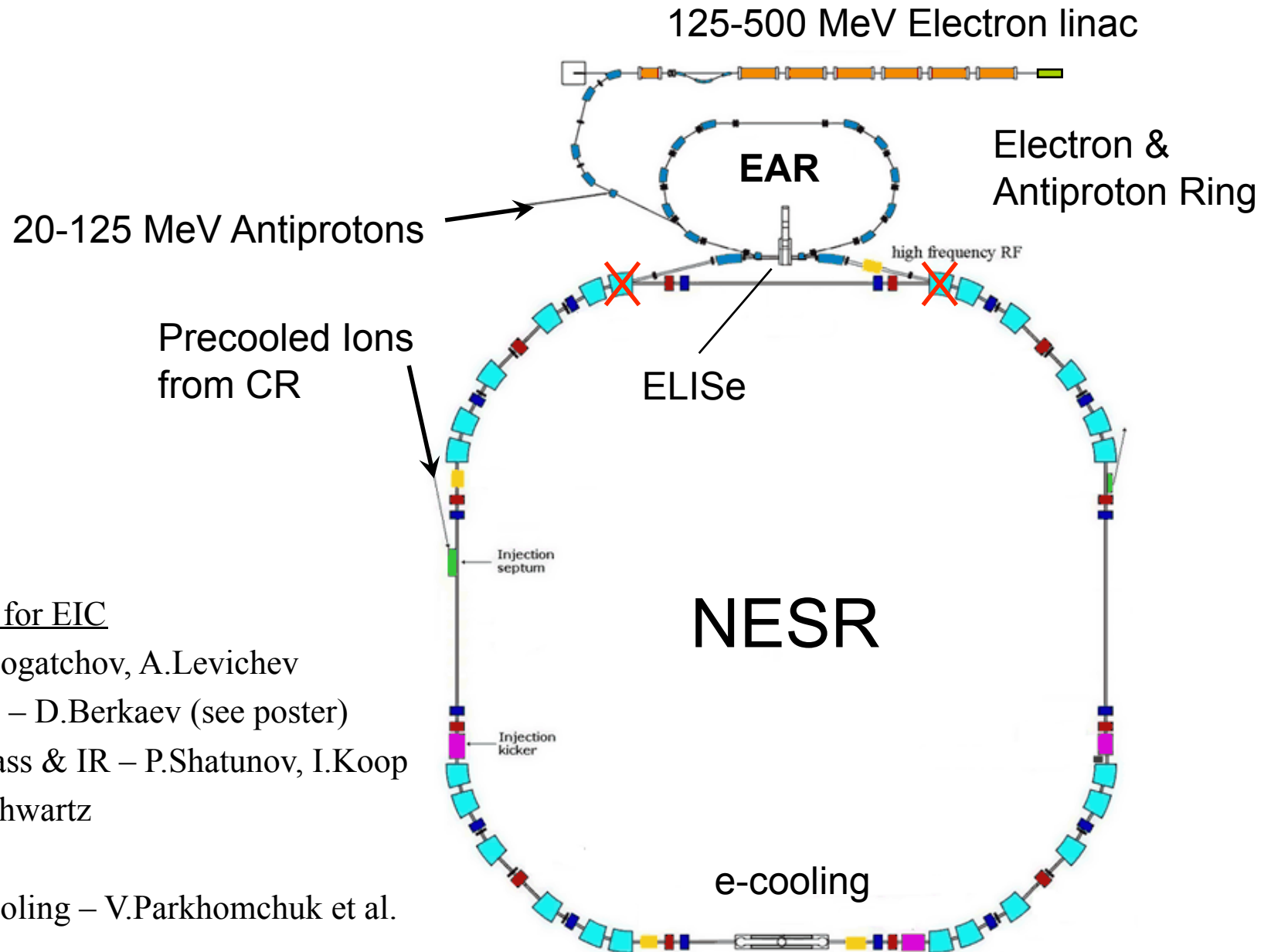


ELISE spectrometer 3D view



The assembly (except "butterfly") is movable on the rails to make scan along beam axis (i.e. electron scattering angle)

EIC General View



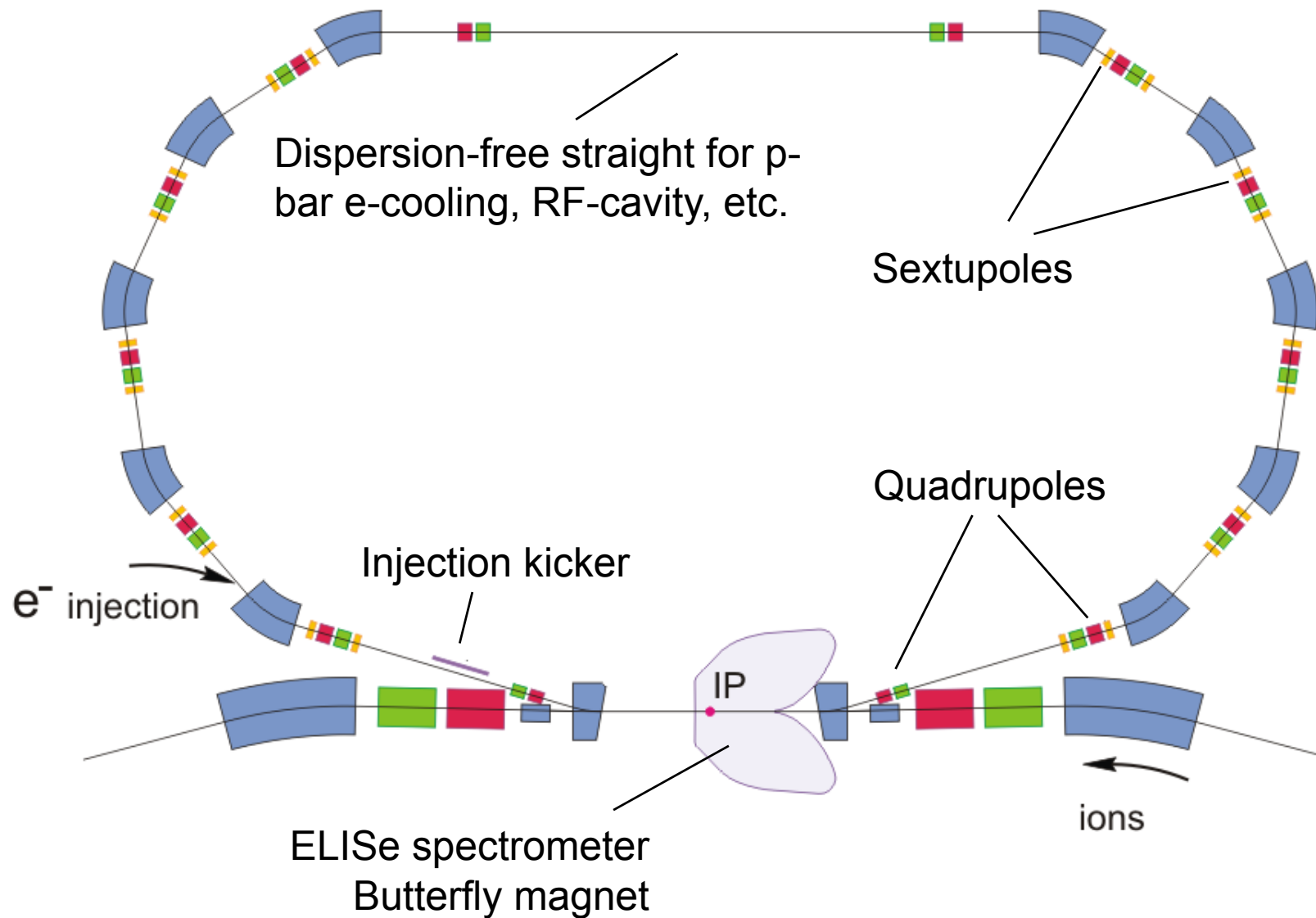
BINP activity for EIC

- 1) Linac – P.Logatchov, A.Levichev
 - 2) e^- beamline – D.Berkaev (see poster)
 - 3) NESR bypass & IR – P.Shatunov, I.Koop
 - 4) EAR – D.Shwartz
- +
- 5) Electron cooling – V.Parkhomchuk et al.

Table of parameters

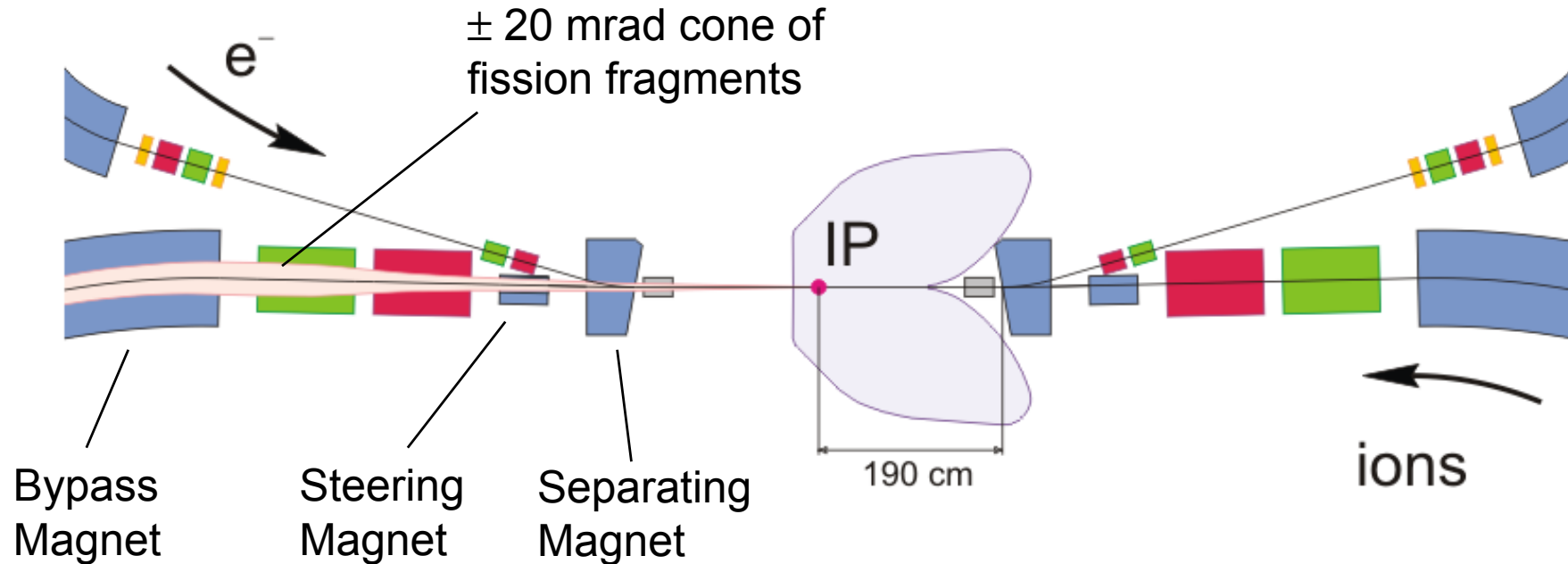
	EAR	NESR
Energy, E	125 ÷ 500 MeV	740 MeV/u
Revolution frequency, f_0	5.5717 MHz	1.1143 MHz
RF harmonic number, q	24	40?
Number of bunches	8	40
Bunch population	$5 \cdot 10^{10}$	$9 \cdot 10^8$
Betatron tunes, ν_x, ν_y	4.2, 3.2	4.55, 2.55
Beta functions in IP, β_x^*, β_y^*	100 cm, 15 cm	
Beam emittances, $\epsilon_{x,y}$	$4 \cdot 10^{-6}$ cm·rad	
Beam sizes in IP, σ_x, σ_y	0.15mm, 0.06mm	
Bunch length, σ_s	4 cm	15 cm
Momentum compaction, α_p	0.034	0.036
Momentum spread, $\sigma_{\Delta p/p}$	$3.2 \cdot 10^{-4}$	$4 \cdot 10^{-4}$
Damping time, τ_x	70 ms	20 ms
Luminosity, L	$1 \cdot 10^{28}$ cm ⁻² s ⁻¹	

EAR layout



Interaction Region layout

- 1) Large space for ELISE spectrometer (deflection "butterfly-magnet")
- 2) 100 cm space in reverse direction needed for photon detection
- 3) "Local bump" to compensate different SM field (different electrons energy)
- 4) **Wide aperture bypass section in NESR for fission experiments**

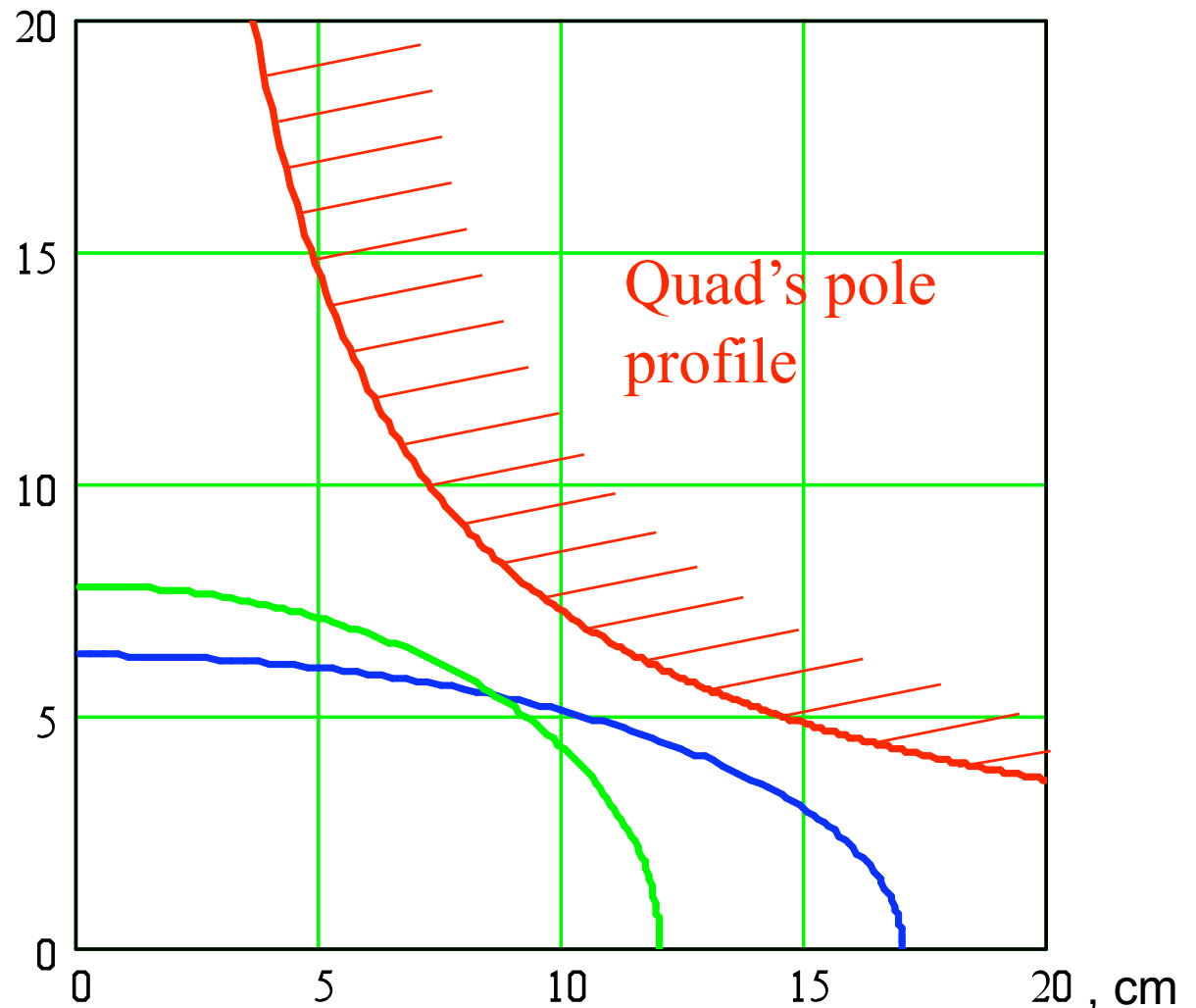


Bypass quads aperture requirements

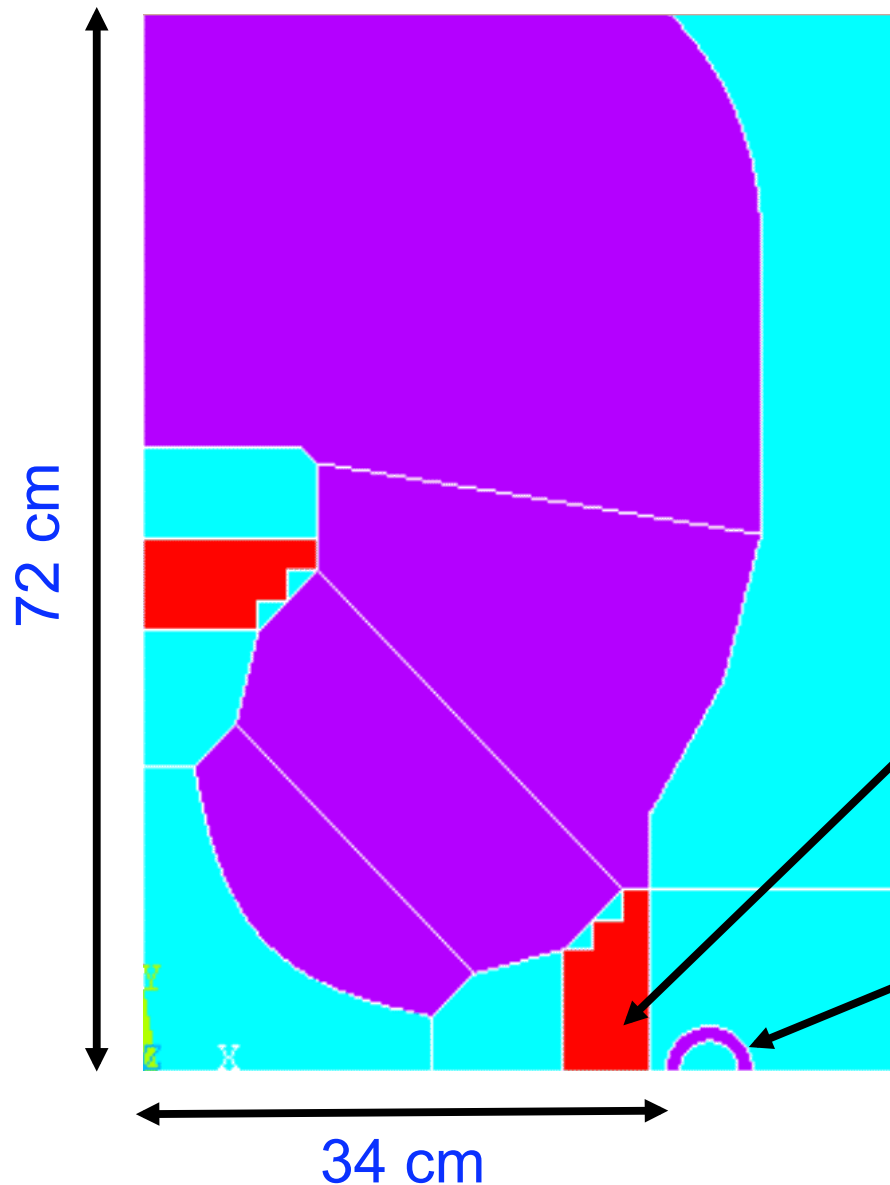
Zones in NESR **D-** and **F-** quads occupied by ± 20 mrad fission projectiles.

Some margins foreseen for case of $BR > 13 \text{ T}\cdot\text{m}$.

Bore radius 12 cm.



NESR bypass quads



“Figure eight” quadrupoles,
 \varnothing 24 cm inscribed diameter,
 $G = 0.85$ kGs/cm gradient,
 $L = 100$ cm length,
 ~ 40 kW power consumption

Warm coil
60 kA*turns

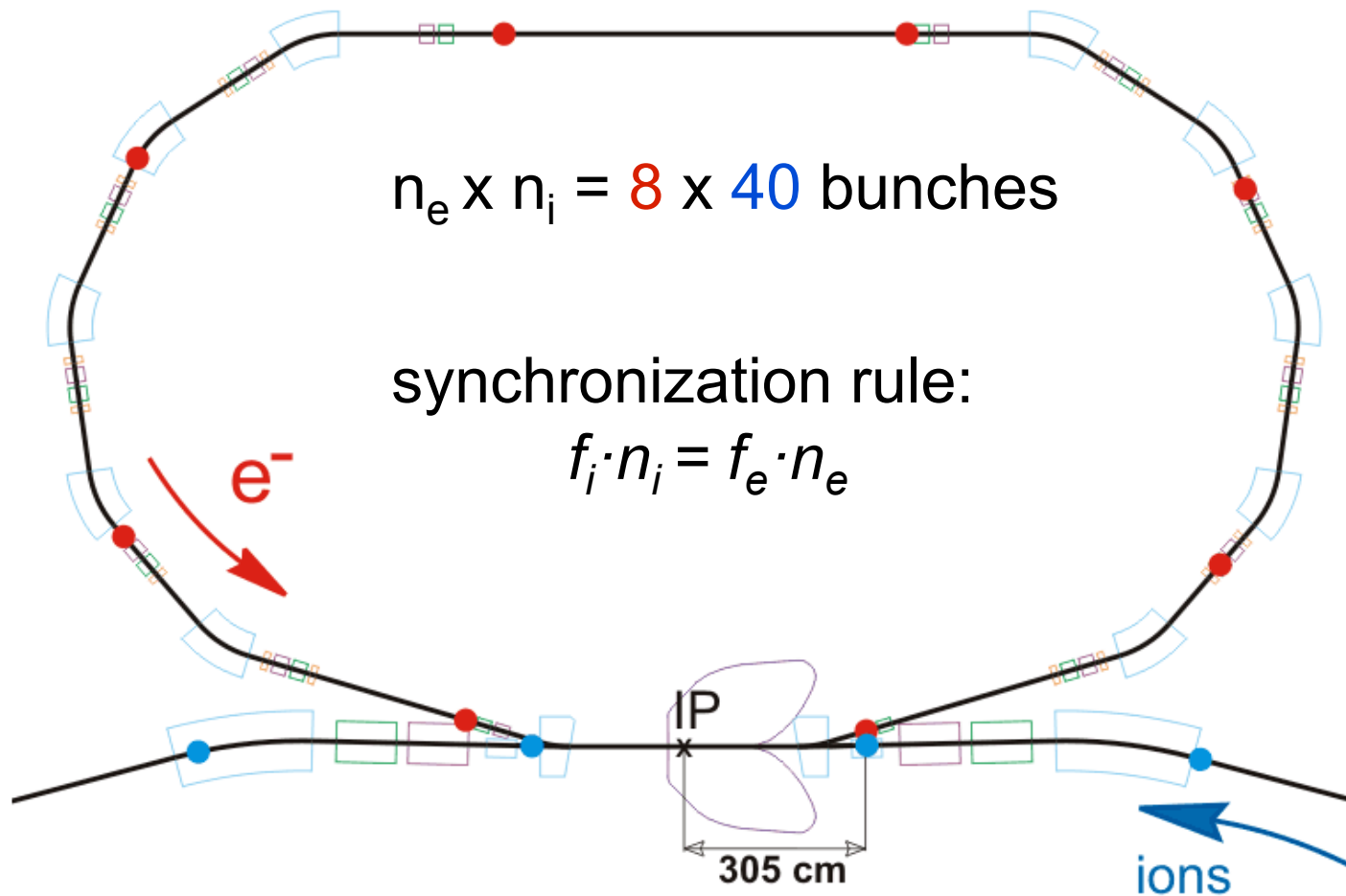
Zero field shield for
electron beam

EAR final
focus quads:



by P.Shatunov

Ion & electron bunches



- 1) Each electron bunch meets with 5 ion bunches
- 2) Distance to 1-st parasitic crossing $L_p = 305$ cm, where bunches are separated into different vacuum chambers

Lattice functions in synchrotron

$$\begin{aligned} \frac{1}{\beta_x} x''(s) &= \dots \\ + \frac{1}{\beta_y} y''(s) &= \dots \end{aligned}$$

$$\textcircled{R} \quad x(s) = \sqrt{\beta_x(s)} \cos(\sqrt{\frac{1}{\beta_x}} s)$$

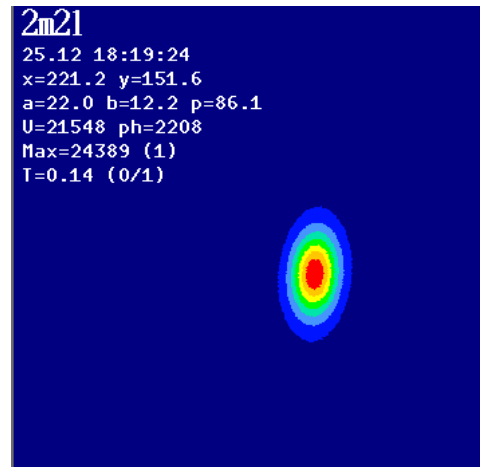
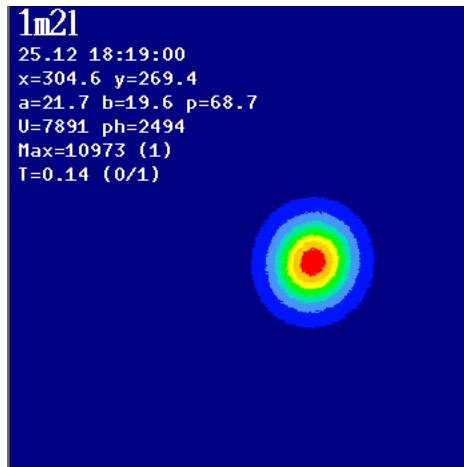
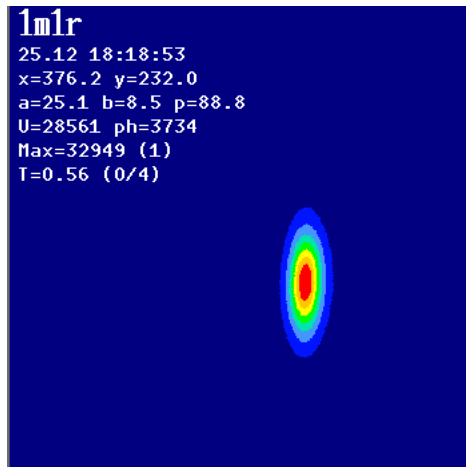
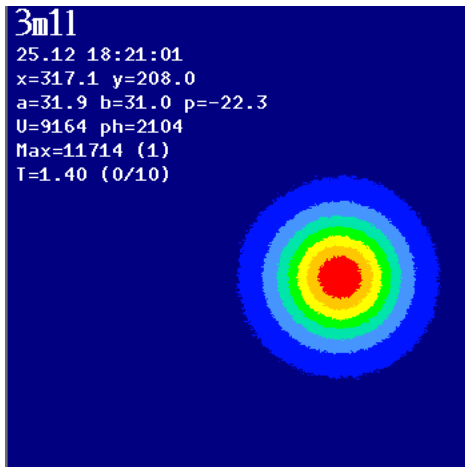
$$\theta_x(s) = \sqrt{\frac{1}{\beta_x}} \sin(\sqrt{\frac{1}{\beta_x}} s)$$

$$\beta_x(s) = \dots$$

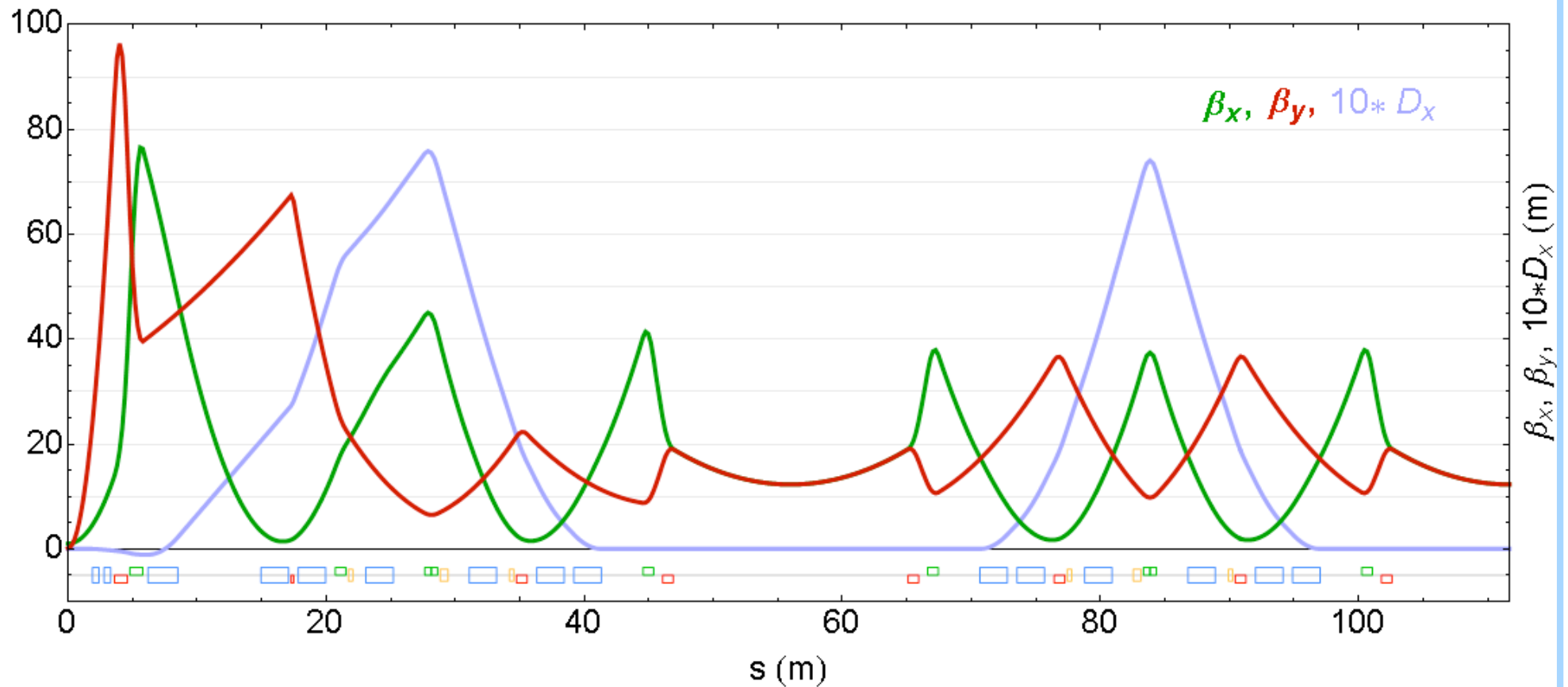
$$\frac{B\rho}{p}$$

$$\theta_x(s) = \sqrt{\frac{222}{E} D}$$

Round beam at VEPP-2000



NESR lattice



Collider mode breaks 4-fold regular NESR optics symmetry, but two arcs stay almost unperturbed

Luminosity limitations: beam-beam

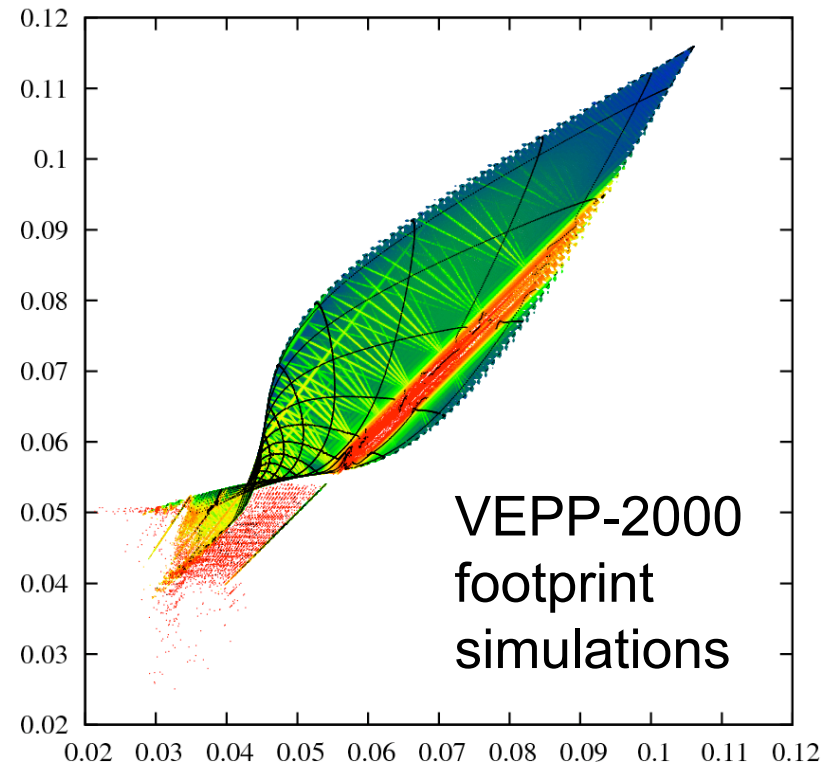
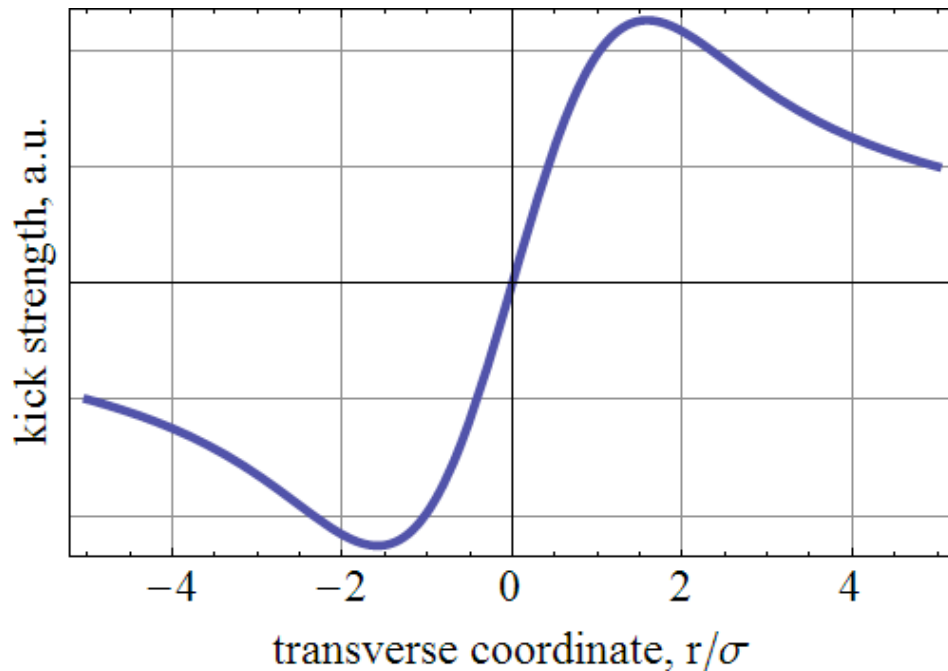
Assuming $\beta_{i,x} = \beta_{e,x}$, $\beta_{i,y} = \beta_{e,y}$,

$$\epsilon_{i,x} = \epsilon_{e,x} = \epsilon_{ixz} = \epsilon_{eyx} \frac{N_r}{A} \frac{N_{r_{ebp}}}{2\epsilon_{ixz}}$$

The problem with beam-beam interaction is a strong nonlinearity of beam-beam force

Beam-beam parameter ξ - the tune shift in linear approximation

$\xi_{max} \sim 0.05$



Luminosity limited by beam-beam

Beam-beam effects are important only for ion beam and thus limit the opposite (electron) beam intensity:

$$N_{eb} = \frac{A}{Zr} \frac{2v\epsilon_{iix} \bar{\omega}}{px} \chi \begin{matrix} \uparrow \neq \\ \leftarrow \vdots \\ \rightarrow \Rightarrow \end{matrix} \sqrt{\frac{z}{x}}$$

Luminosity expressed via threshold beam-beam parameter:

$$L_{tot} = \frac{A}{Z} \frac{\bar{\omega}\epsilon_{ixi}}{2r_{px} \sqrt{\frac{z}{x}}} \begin{matrix} \uparrow \neq \\ \leftarrow \vdots \\ \rightarrow \Rightarrow \end{matrix}$$

Luminosity depends only on total ion beam current, not on the number of bunches. For weak ion beams (with no IBS problems) rationally to operate in 1x1-bunch regime to avoid potential difficulties with collective beam-beam effects.

Luminosity limitations: IBS

Tuneshift due to intrabeam scattering:

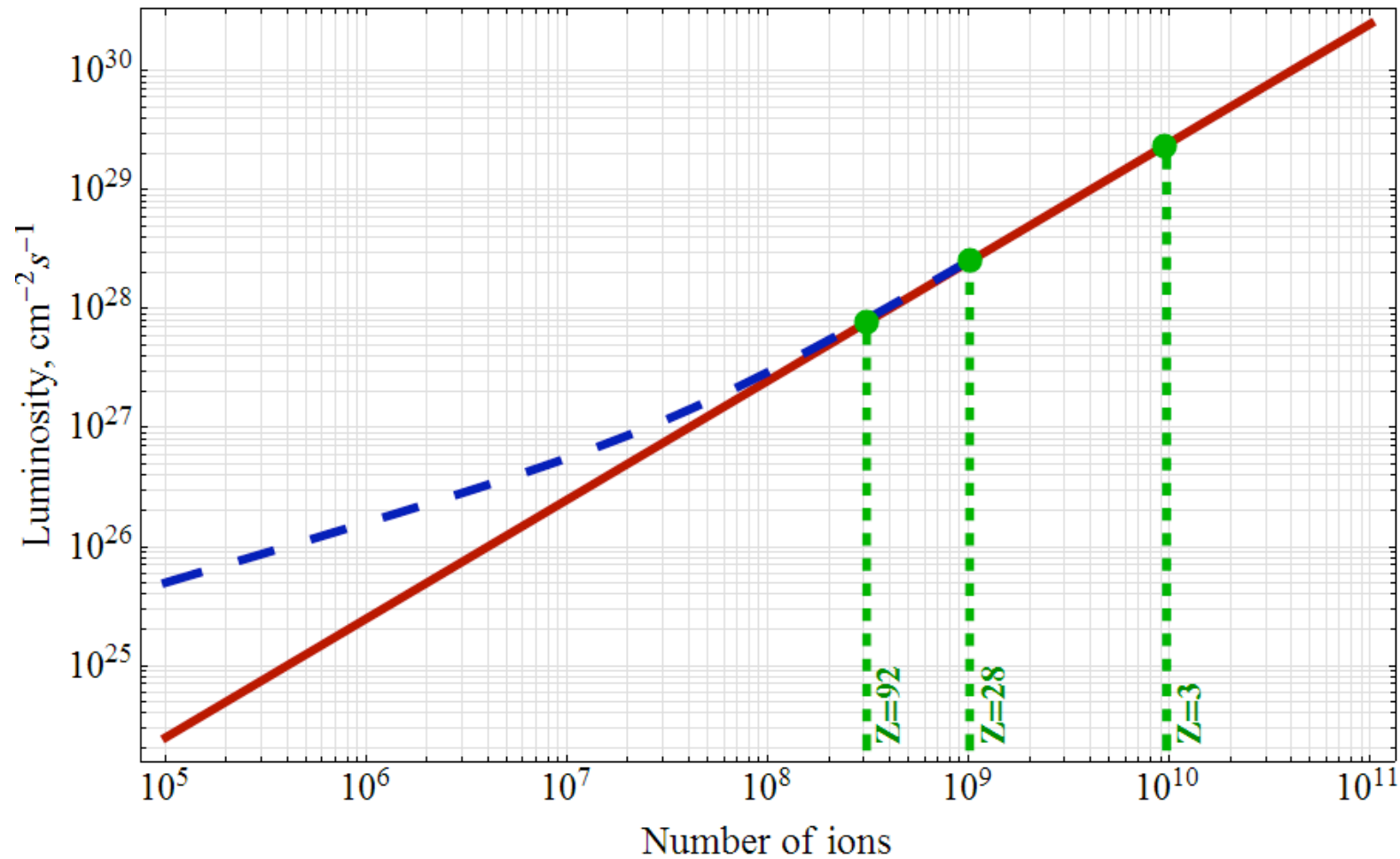
$$\Delta \lambda_{\text{IBS}} \sim \frac{Z^2 R}{A} \frac{N_{ibp}}{\epsilon_{ii}^{3/2} \chi} \frac{1}{2\sqrt{\nu \theta_s}} \quad B\lambda_{\text{max}} \sim 0.1$$

IBS tuneshift strongly depends on energy, and becomes negligible for ultra-relativistic electron beams ($\gamma_i = 0.8303$, $\gamma_e = 1000$). IBS thus limits ion beam intensity.

Limitations for the ion beam intensity (with given emittance):

$$\frac{N_{ibis}}{\chi} = \frac{A}{Z^2 R} \frac{\epsilon^{3/2} \lambda \nu \theta}{p} \frac{1}{2\sqrt{\nu \theta_s}}$$

Luminosity Approach



Luminosity limited by beam-beam interaction.

Ion beam intensity limited by IBS.

Additional benefit for low-intensive ion beams

Luminosity benefit for exotic ion beams

Not mentioned ion beam intensity limitation – the production rate!

If available number of ions (exotic and radioactive)

$N_{ib} \ll N_{ib\ max}$ (for given $\varepsilon = 5 \cdot 10^{-6} \text{ cm}$),

let us cool the beam down $\varepsilon \rightarrow 1 \cdot 10^{-7} \text{ cm}$

Gain in luminosity:

- 1) Higher density in the core of electron beam (gain factor: x2)
- 2) Less nonlinearities in beam-beam force, larger ξ (gain factor: x10)

Nevertheless the electron beam emittance should be significantly reduced (while its intensity - increased to raise particles density and beam-beam parameter).

Beam emittance in electron storage rings

The balance between strong radiation damping and quantum fluctuations of synchrotron radiation forms Gaussian electron bunch distribution during several damping times, $\tau \sim 50$ ms (@ 500 MeV).

Momentum spread: $\frac{\Delta E}{E} = \frac{55}{323} \frac{\varphi_e}{E} \frac{\langle 1/r_0^3 \rangle}{\langle 1/r_0^2 \rangle} \epsilon^2$

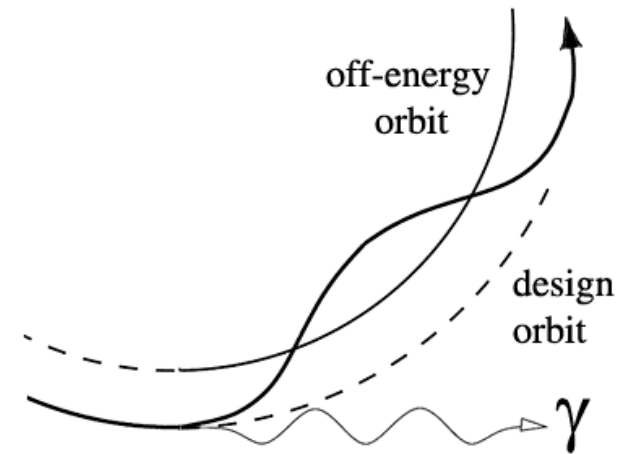
Bunch length: $\theta_l = \frac{c - p}{Y_s} \frac{\theta_E}{E}$

Horizontal emittance: $\chi_x = \frac{55}{323} \frac{\varphi_e}{J_x} \frac{\langle H r_0^3 \rangle}{\langle 1/r_0^2 \rangle} \epsilon^2$

where $H = \frac{1}{2} \left(\frac{dx}{ds} \right)^2 + \frac{1}{\rho} x$

Vertical emittance: $\chi_z = \frac{1}{2} \frac{1 - \kappa}{\beta_z} \epsilon^2$

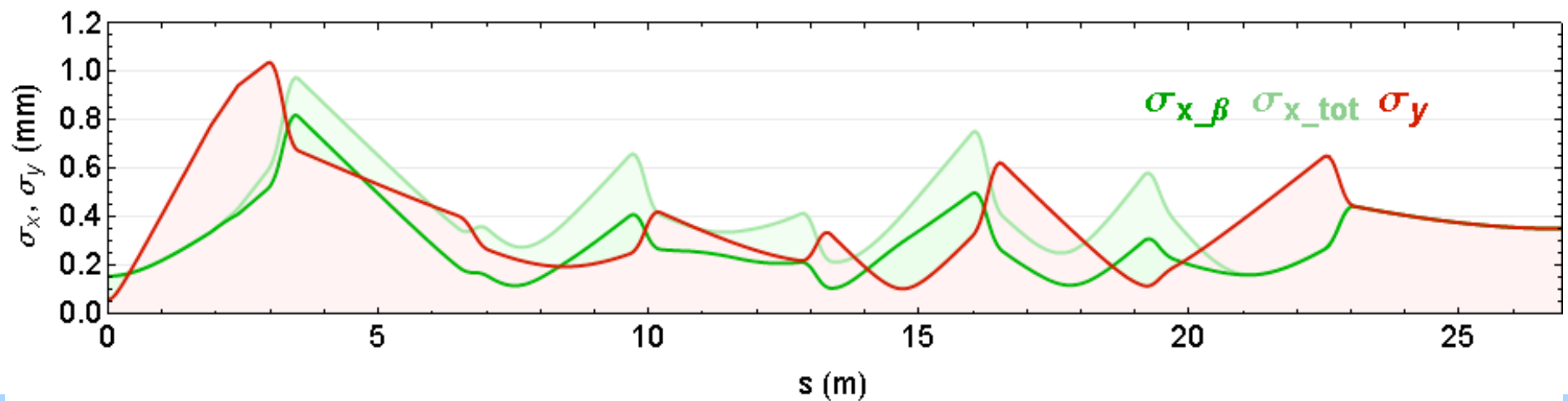
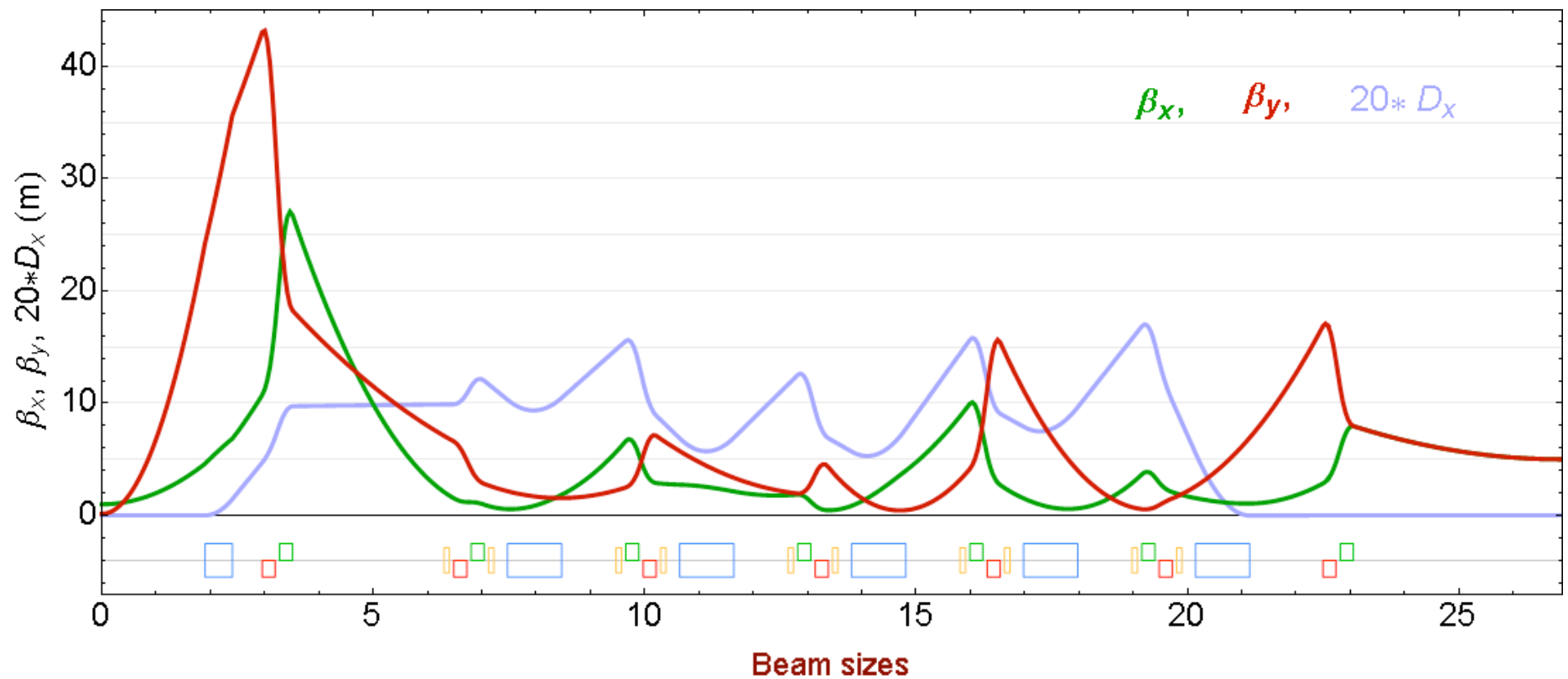
where $\kappa \ll 1$ – betatron coupling coefficient



Working point should be at the coupling resonance!

$$\left\{ \begin{matrix} \lambda_x \\ \lambda_z \end{matrix} \right\} = \left\{ \begin{matrix} 1 \\ 0 \end{matrix} \right\}$$

EAR lattice functions & beam size



Chromaticity correction

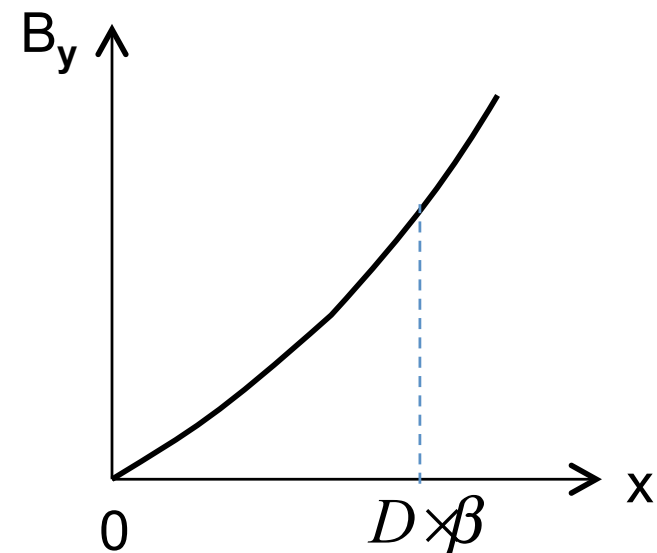
Natural tune chromaticity in EAR ring:

$$\frac{\oplus \mathcal{Q}_x}{\oplus \beta} = +7 \quad \frac{\oplus \mathcal{Q}_y}{\oplus \beta} = +10$$

Uncompensated negative natural tune chromaticity:

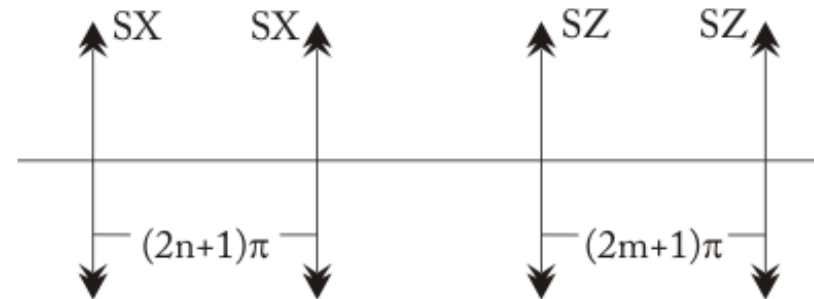
- synchro-betatron coupling & resonances
- footprint (due to beam momentum spread)
- **head-tail instability!** (with very low threshold)

Sextupoles needed to compensate tune dependence on momentum deviation.



Planning sextupole families

1. Self-compensated families of sextupoles arranged with proper betatron phase advance (works well for long multi-cell arcs).

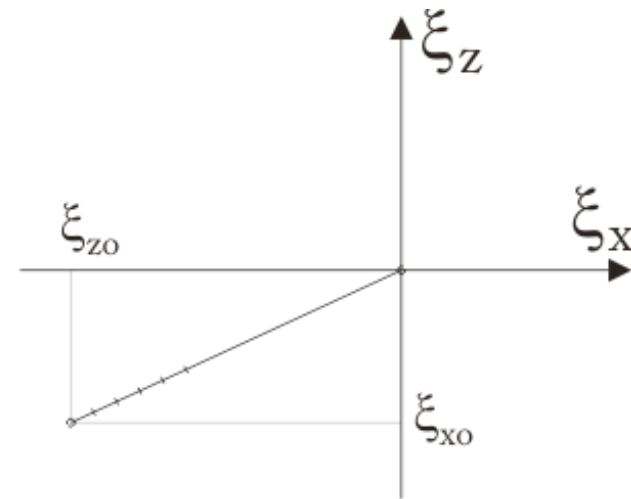


2. Harmonic analysis of sextupole field distribution via resonant perturbation theory. Nearest resonance's strength suppression. (Only if the working point close to single nonlinear resonance).

$$\frac{\oplus H_z}{\oplus \alpha^2} (\cos(3\psi) \cos(\Omega) \leftrightarrow n)$$

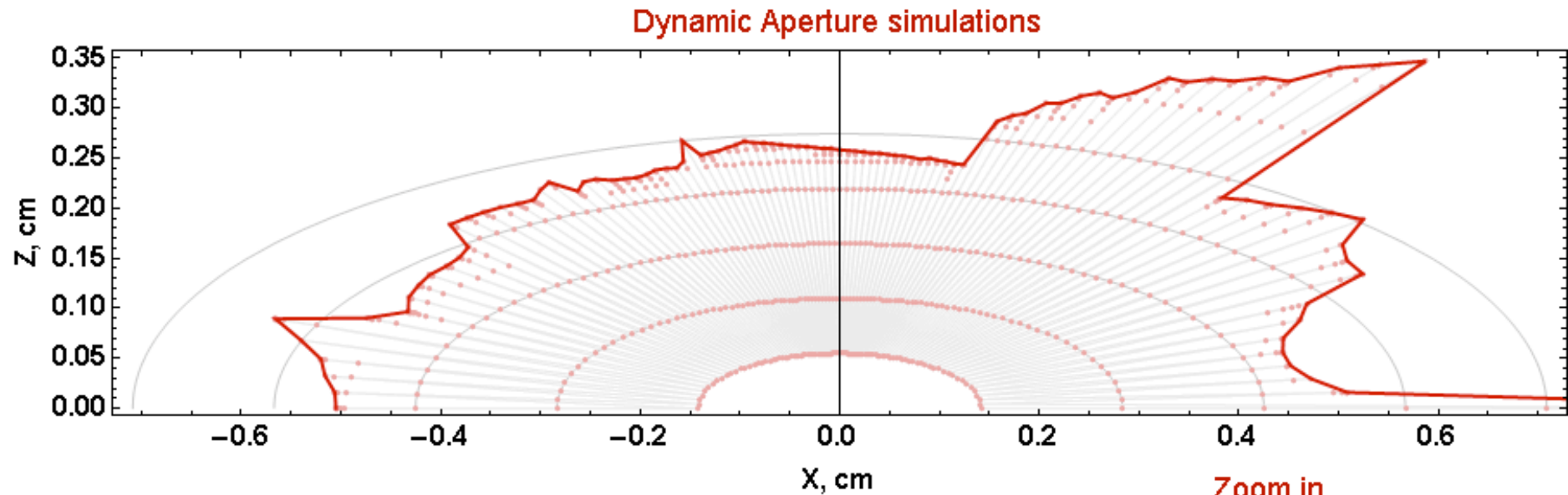
3. "Best pairs" optimization scheme (E.Levichev, P.Piminov, EPAC'2006).

Portion of chromaticity is compensated by one pair (SX_i, SZ_i), that gives the largest DA.



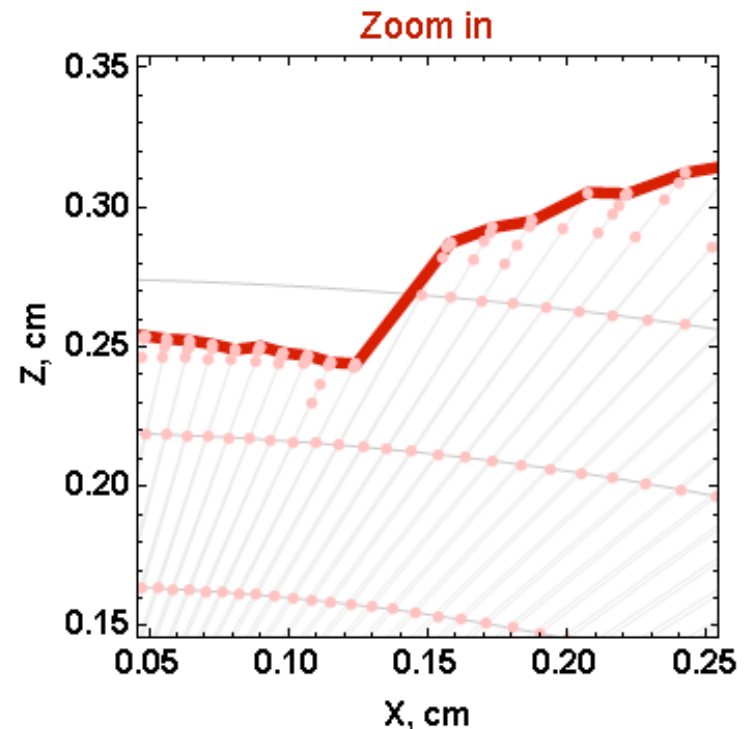
Dynamic Aperture (DA) - the region (in 4D phase space) of particle coordinates with stable betatron oscillations

Dynamic Aperture simulations

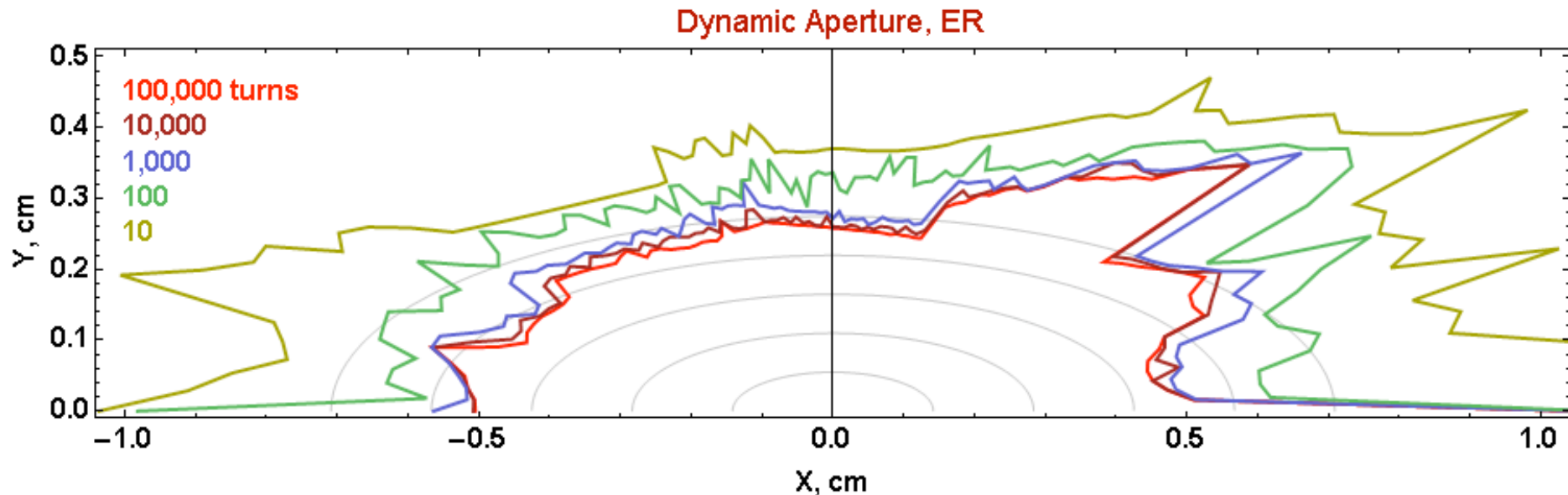


Each point of x-z plane of initial particle deviations tested to be stable by tracking with use of SAD code (KEK, Japan).

The steps decrease nearby DA border from 10σ to 0.01σ .



DA estimation accuracy vs. tracking parameters



Transverse damping time $\tau_{x,z} \sim 60$ msec,
revolution frequency $f_0 \sim 5.5$ MHz

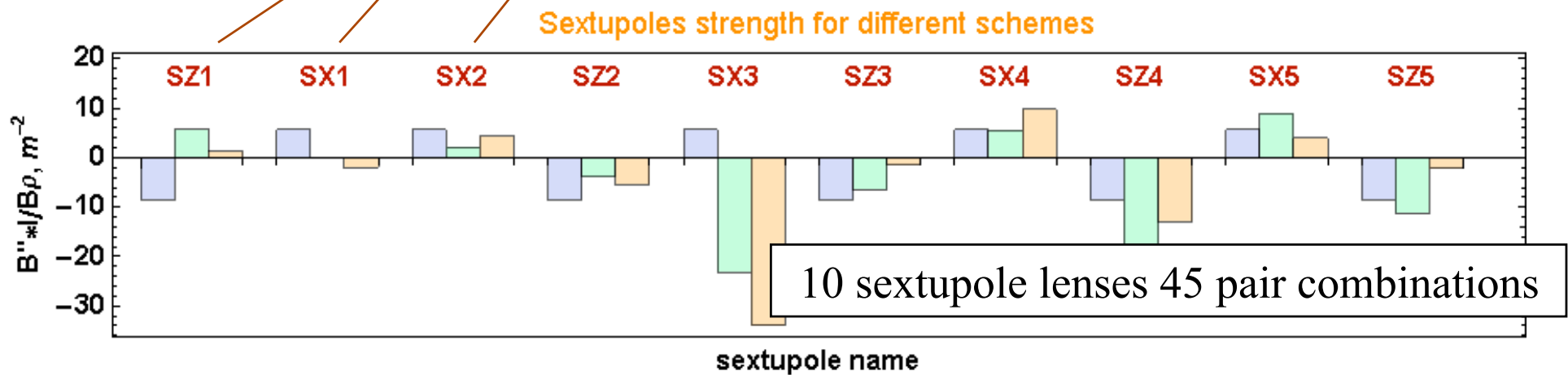
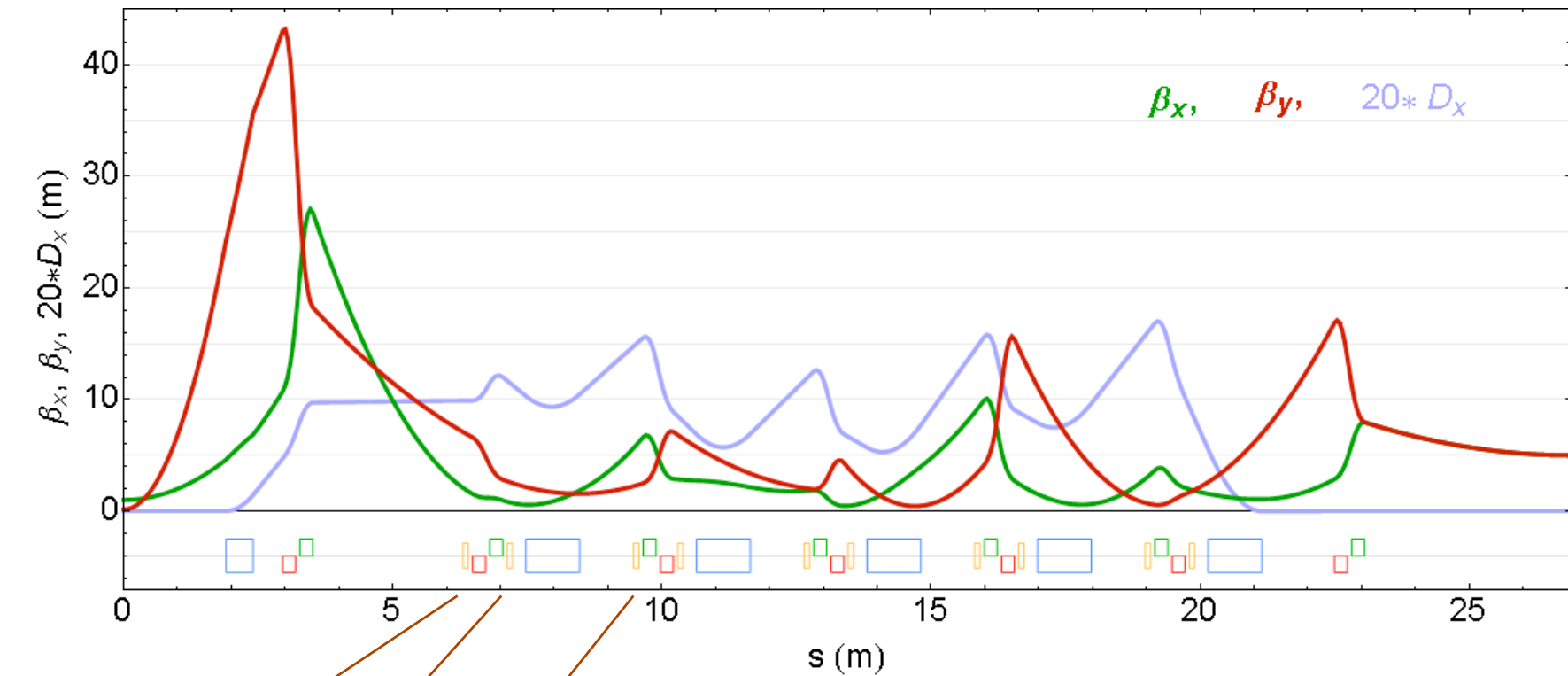
\Rightarrow 300 000 turns tracking?

Too much!

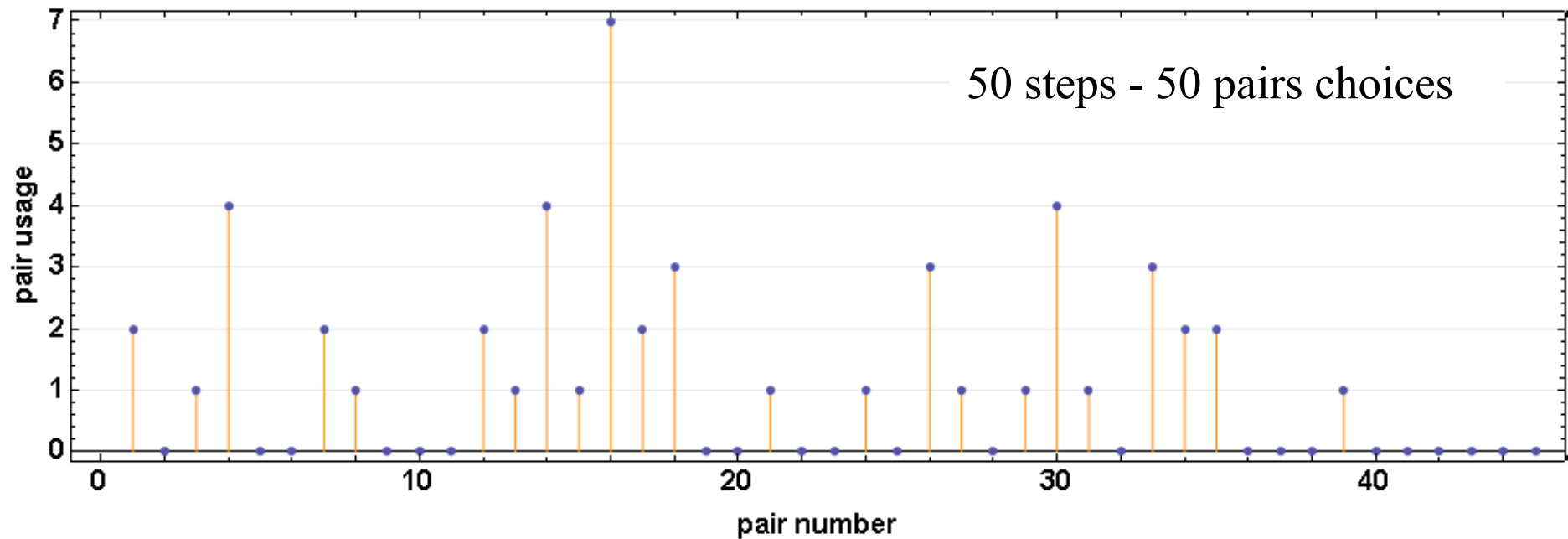
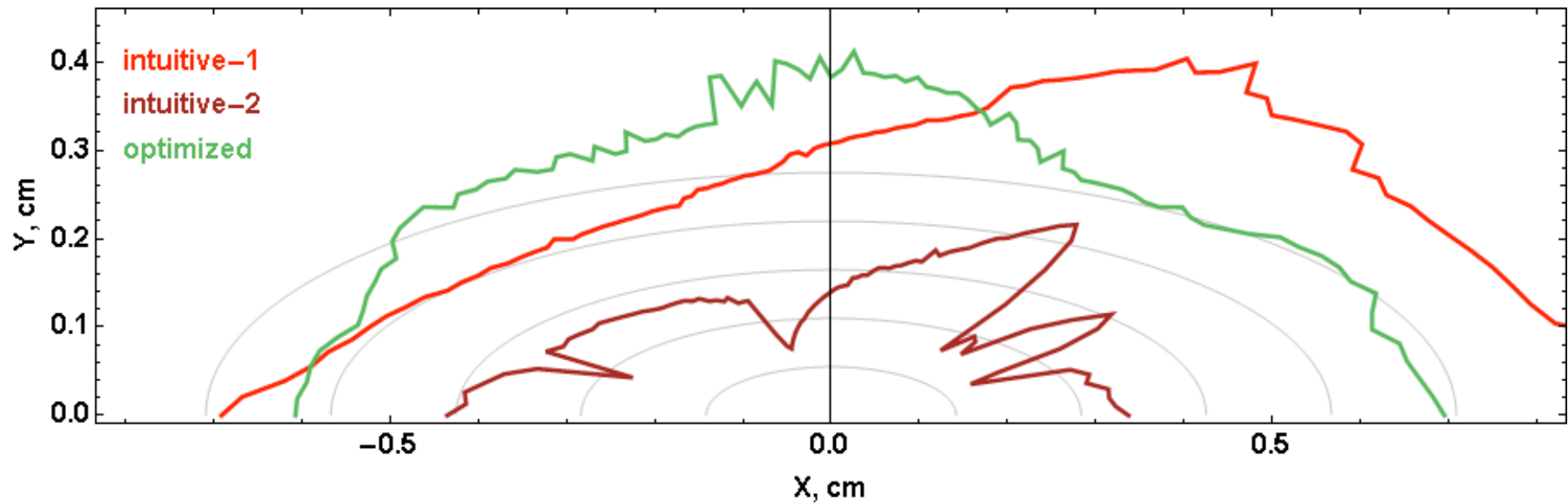
2000-5000 turns used for standart DA estimations.
Only 300 turns for routine optimization procedures.

turns	DA/ σ
10	55.98
100	40.57
1000	34.63
10000	32.81
100000	32.81

Solutions for sextupole scheme



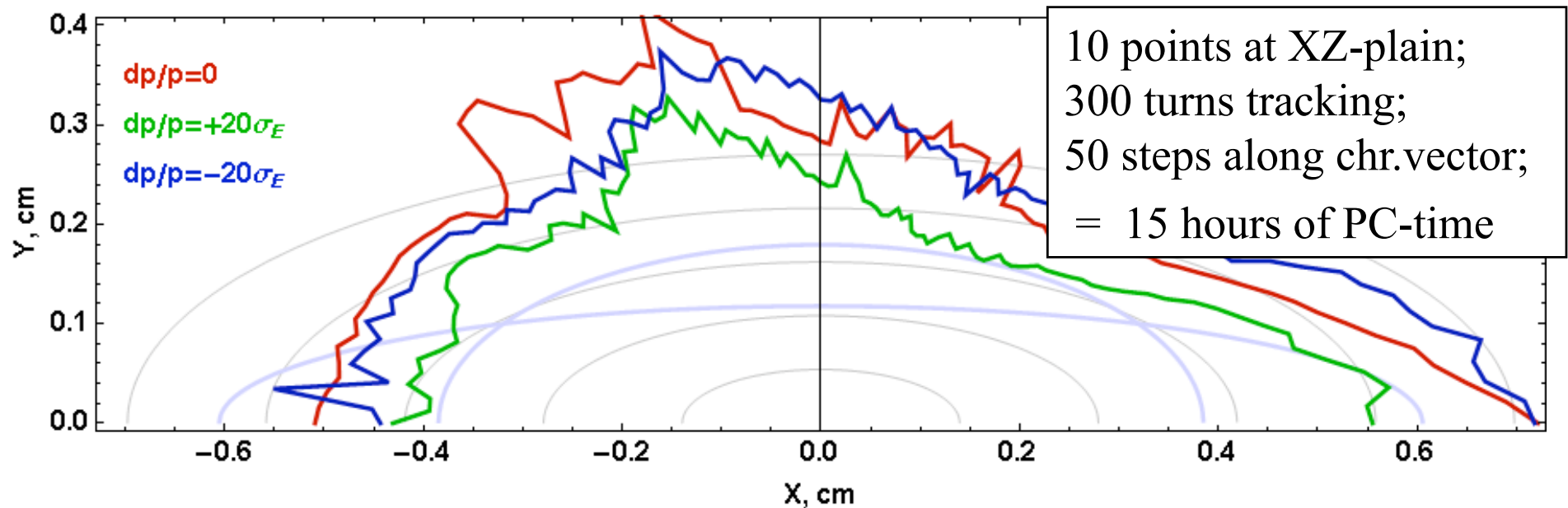
Solutions for sextupole scheme



Dynamic Aperture optimized

Finally, optimization procedure also included:

- 1) switched on nonlinear quadrupole fringe fields;
- 2) DA estimations for on-energy and off-energy particles $dp/p = \{-10\sigma, 0, +10\sigma\}$ simultaneously.

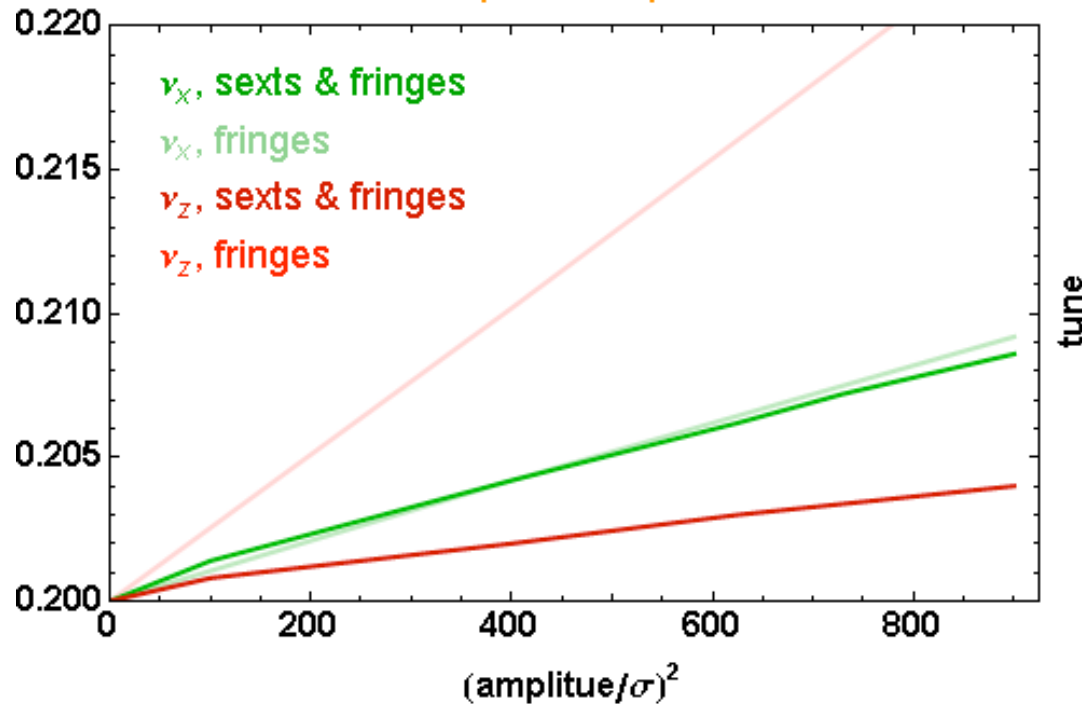


Gray lines – $n \cdot 10 \cdot \text{beamsize}$

Light blue lines – physical aperture of $\varnothing 40\text{mm}$ vacuum chamber

Nonlinear particle dynamics

Tune amplitude dependence

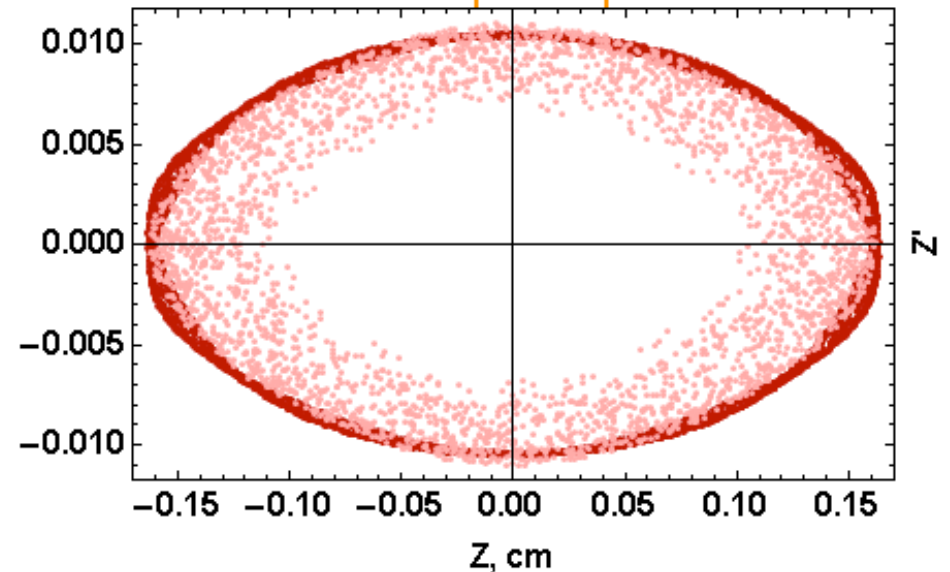


Octupole fields produce tune-amplitude shift in the first order of perturbation theory.

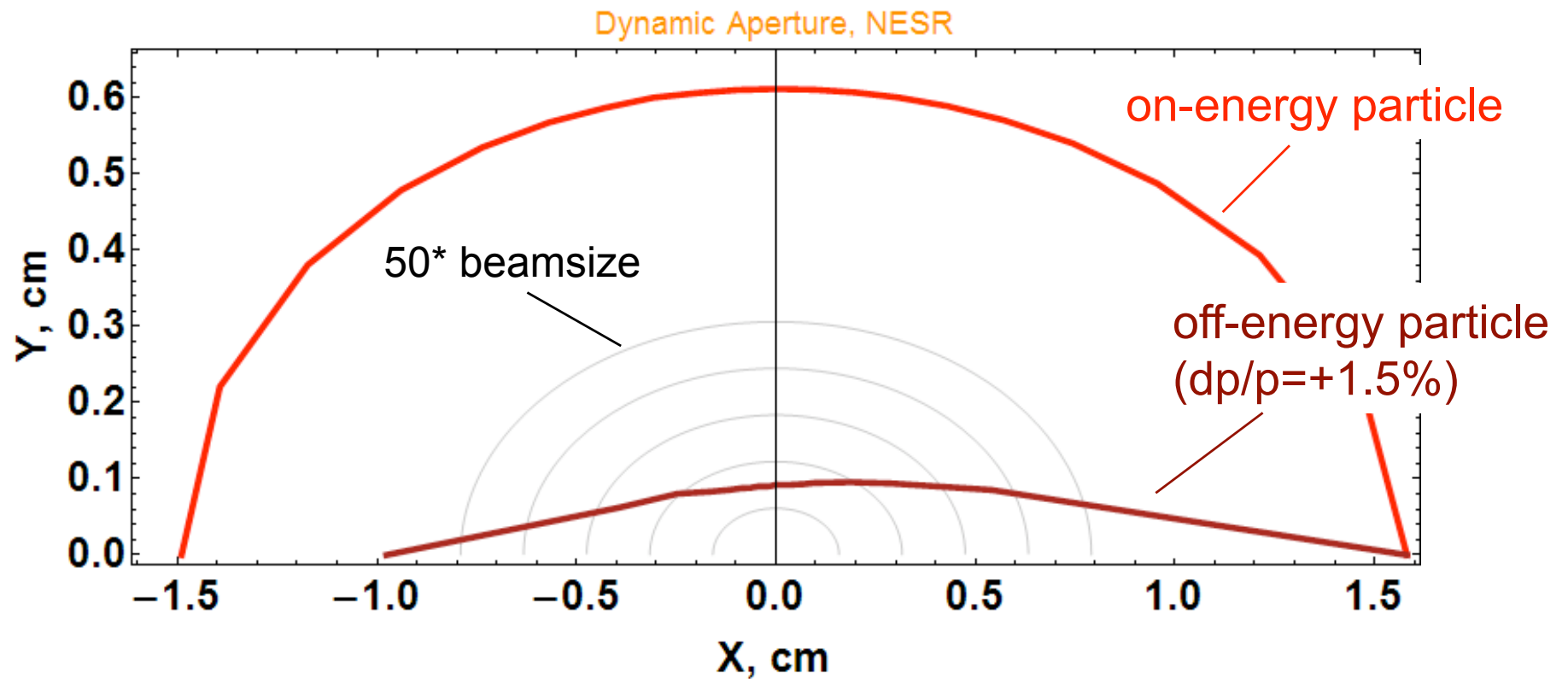
$$B\lambda \frac{-3}{8} \langle {}^2b_3 \rangle \frac{a^2}{0}$$

Sextupoles also can shift betatron tunes, but only in second order (complicated formulas), and $\partial\nu/\partial a^2$ depends on working point.

Vertical phase space



NESR dynamic aperture



The NESR dynamic aperture in collider mode decrease drastically for large momentum deviation. To be fixed...

Thank you for attention!