



# Bunched Beams – Longitudinal Beam Dynamics

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# Parameters of the Longitudinal Beam Dynamics

$V_0$ : Rf (peak) voltage

$dp/p$ : Momentum spread (coasting, bunched)

Bf: Bunching factor (mean current/ peak current) – Bunch (phase) length:  $\phi_B = 3/2 \pi Bf$

$\phi_s$ : Phase of synchronous particle

$\omega_s$ : Synchrotron frequency (beam in rf bucket)

$h_{\text{bunch}}$ : Harmonic number of the bunches

$h_{\text{Rf}}$ : Harmonic number of the Rf system (may be different to  $h_{\text{bunch}}$ , e.g. kicker gap)

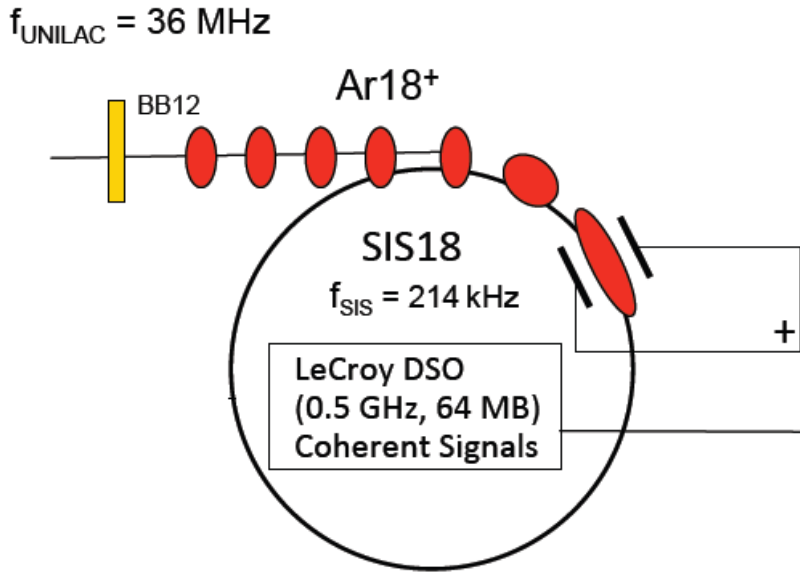
$\alpha$ : Momentum compaction factor =  $\frac{1}{\gamma_t^2} = \alpha_p = \frac{1}{C} \oint \frac{D(s)}{\rho(s)} ds$   $\gamma_T \sim Q$

(Density of particle tracks with different momenta – function of the ring lattice)

$\eta$ : Slip factor =  $1/\gamma^2 - 1/\gamma_T^2$

$\eta = 0$ : All particles, independent from the momentum deviation have the same revolution time  
(isochronous mode > storage rings)

# Injection and Debunching



$$z_m'' + k_{z0}^2 z_m - \frac{K_L}{z_m^2} - \frac{\epsilon_L^2}{z_m^3} = 0$$

$$E_{||} \sim -K_L z$$

Longitudinal Envelope Equation

$z_m$ : bunch length

$\epsilon_L$ : longitudinal emittance

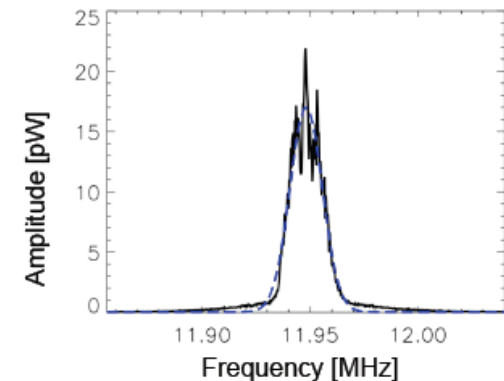
$K_L$ : space charge parameter

$k_z$ : longitudinal focusing (Rf system)

## Coasting (debunched) beam:

Debunched, dc beam, „equally“ distributed over the circumference with a „flat“ longitudinal distribution. The linac beam has a microstructure, given by the linac Rf system – normally of much higher frequency than the ring Rf system.

The (micro)bunches from the linac are debunching after injection until they overlap. The momentum spread of the coasting beam is defined by the momentum spread of the microbunches (without space charge and debunching Rf system).



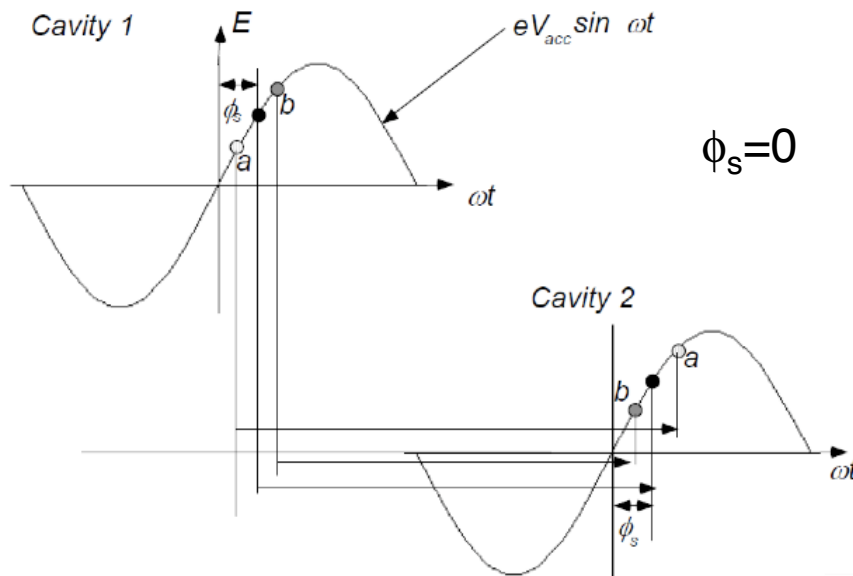
Schottky Spectrum



# Longitudinal Profiles in Circular Accelerators

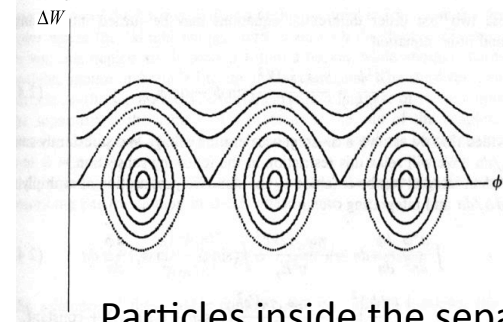
## Bunched beam (stationary):

Particles capture in the Ring Rf bucket. Parabolic longitudinal distribution. Number of bunches are defined by the ratio of Rf frequency/ revolution frequency = harmonic number  $h$ .



$$T = h \frac{2\pi}{\omega_{RF}}$$

'stationary buckets'

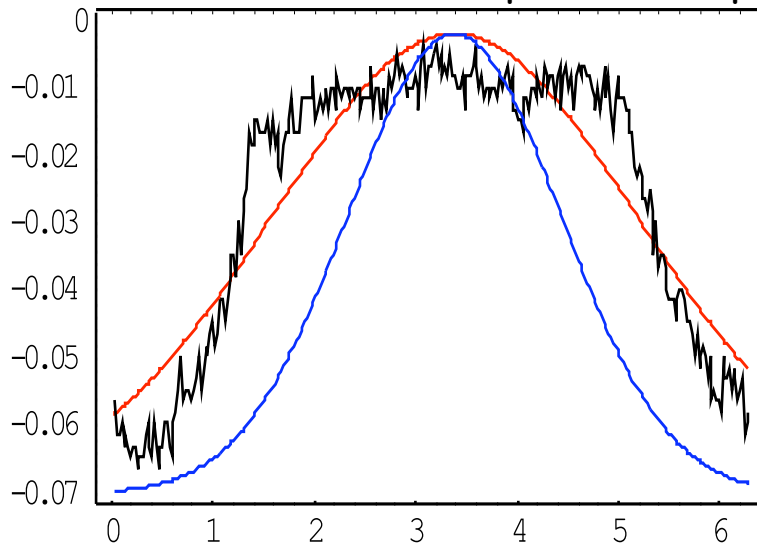


Particles inside the separatrix: bunch

The run time  $T$  of the particle between two cavities must be an integer number  $h$  of oscillations.

## Observed bunch profiles in SIS 18 after rf capture

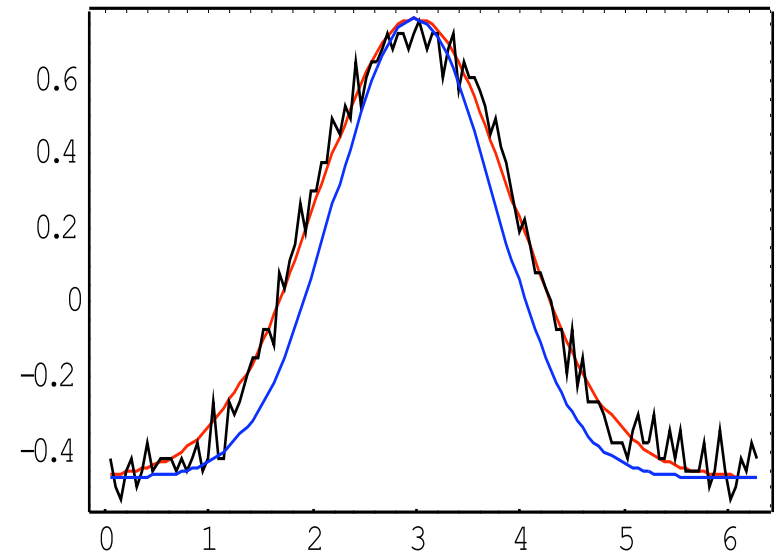
SIS-MODI rf amplitude ramp



Distorted bunch form.

Bunch area blow-up:  $\approx 100\%$

self-generated adiabatic rf ramp



Matched bunch.

Bunch area blow-up:  $\approx 30\%$

# Longitudinal Phase Space Conservation

The longitudinal phase space  $\varepsilon_L$  is invariant.

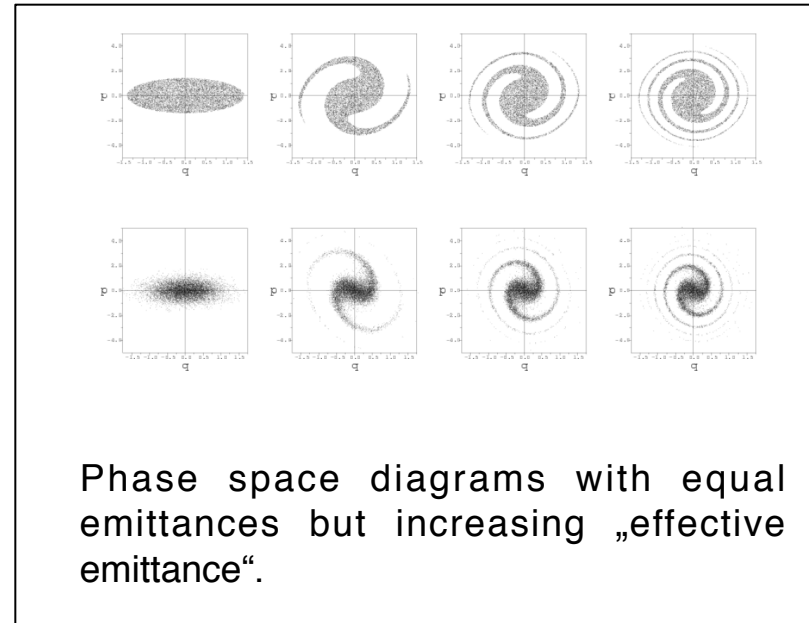
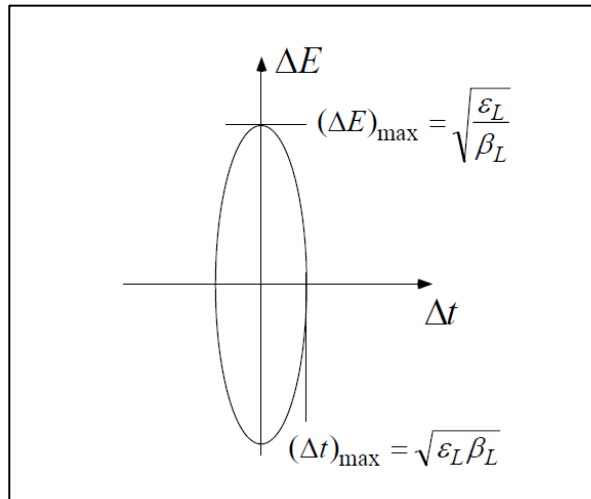
Even nonlinear systems do not change the emittance.

Only mechanisms changing the total energy of the systems change the emittance,

- e.g. acceleration (damping with  $\varepsilon \sim \beta\gamma$ ), cooling etc.

Other mechanisms which may potentially change the emittance:

- charge exchange (stripping, stripping injection ...)



However, the effective emittance can be changed. E.g. „air“ in the phase space generated by e.g. instabilities, coherent longitudinal oscillations, mismatch, Rf phase jumps etc. increases the effective emittance.

Since beam loss has to be avoided, the effective emittance is the only important parameter.

# Bunching: Coasting Beam > Bunched Beam

The Rf frequency must be matched to the revolution frequency of the beam (schottky measurement).

The bunching process must be performed (iso)adiabatically.

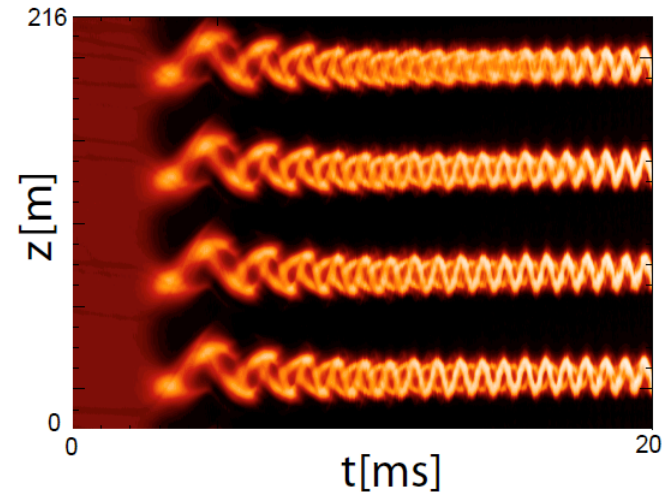
The bunch must be matched to the bucket at any time.

The capture time must be a multiple of the synchrotron period (e.g. 30x).  
The change in synchrotron frequency must be small with respect to the synchrotron period.

Phase space conservation

$$(dp/p)_C \times C = Ff \times h_B \times (dp/p)_B \times z_B$$

$$(dp/p)_B = 8/3 \times (dp/p)_C / (\pi Bf)$$



**Observation:**  
Persistent dipolar or quadrupolar bunch oscillations above a threshold intensity.

Persistent dipole oscillations in SIS 18:  $\Sigma \approx 0.2$

# Stationary Bunches

$$V_0 = \frac{(dp/p)^2}{d\phi^2} \times \frac{2\pi h \eta}{q e} mc^2 \beta \gamma (1 + \Sigma_0)$$
$$\Sigma_0 = \frac{3Qhgqe}{8\pi\epsilon_0 mc^2 \beta^2 \gamma^3 \eta (dp/p)^2 R d\phi}$$

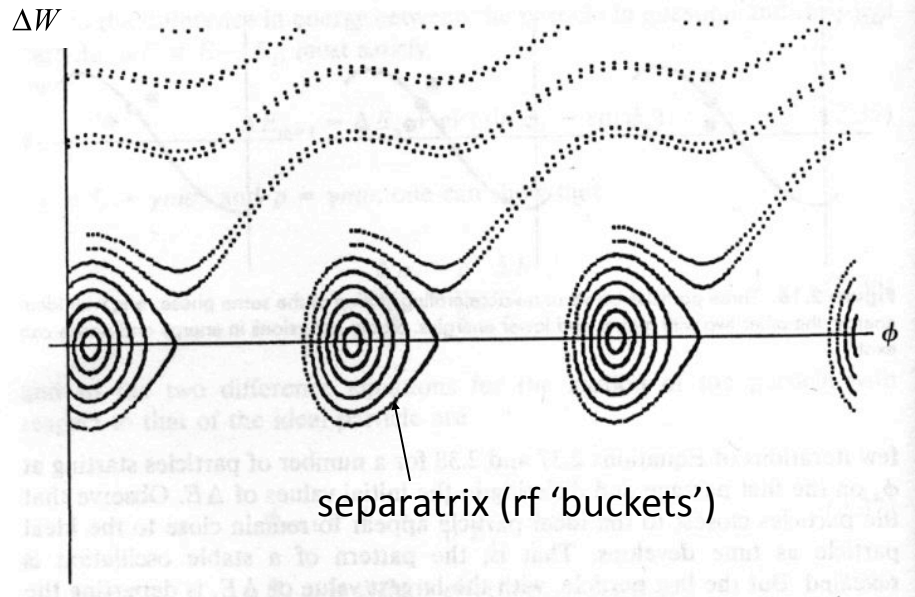
Rf voltage with space charge parameter

R: mean ring radius

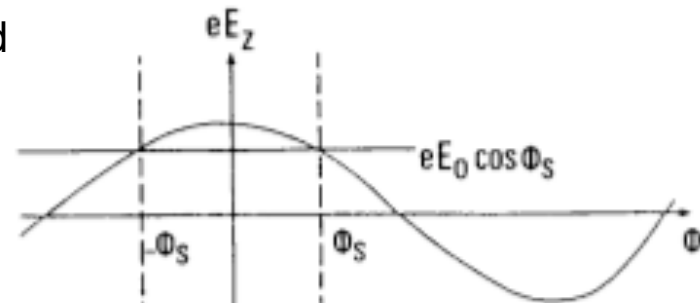
g: form factor =  $\frac{1}{2} + 2 \ln (r_{\text{tube}}/r_{\text{beam}})$

# Acceleration

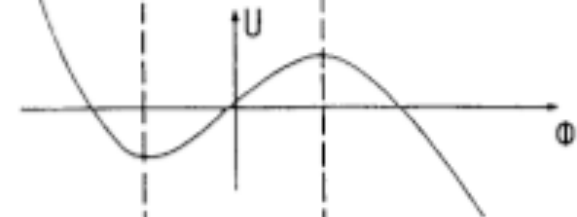
'accelerating buckets'



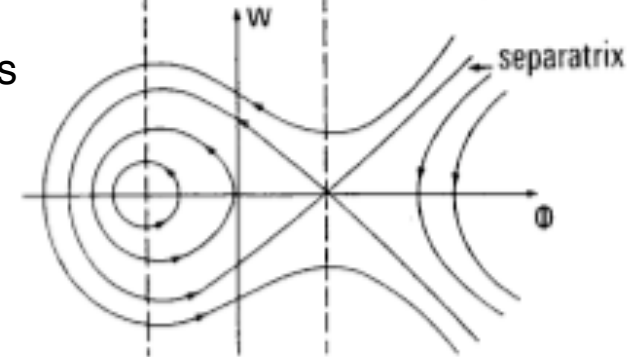
Electric Field



Potential



Trajectories





## Synchrotronfrequency

$$\omega_S = \sqrt{\frac{qVh \sin\phi_s \eta}{2\pi R^2 \gamma m}}$$

SIS18: typically 1 kHz

SIS100: proton operat.  $> \infty$

## Bucket Area (Phase Space Acceptance)

$$A_B \propto \frac{1}{h^2} \sqrt{\frac{qhV_0}{M \cos\phi_s}} \frac{1 - \sin\phi_s}{1 + \sin\phi_s}$$



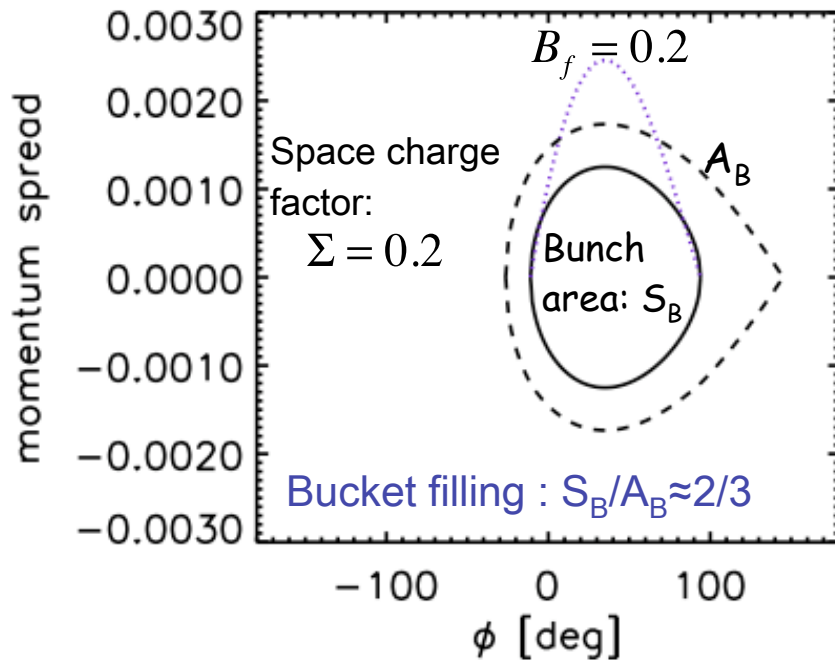
# SIS18/SIS100 Rf Bucket Area and Beam Quality

Bucket area: 
$$A_B \propto \frac{1}{h^2} \sqrt{\frac{qhV_0}{M \cos\phi_s} \frac{1 - \sin\phi_s}{1 + \sin\phi_s}}$$

Bunch area and equivalent coasting beam momentum spread

$$S_B = C \left( \frac{\Delta p}{p} \right)_{dc} \propto N_{inj} (\beta_0 \gamma_0)^{-1}$$

$\omega = 4 \text{ T/s}; V_0 = 400 \text{ kV}, h=10, \phi_s = 35^\circ$

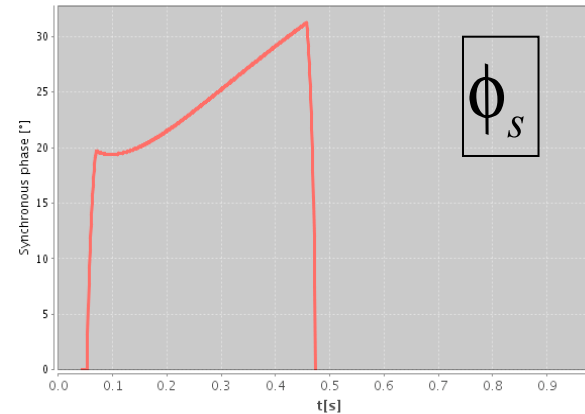
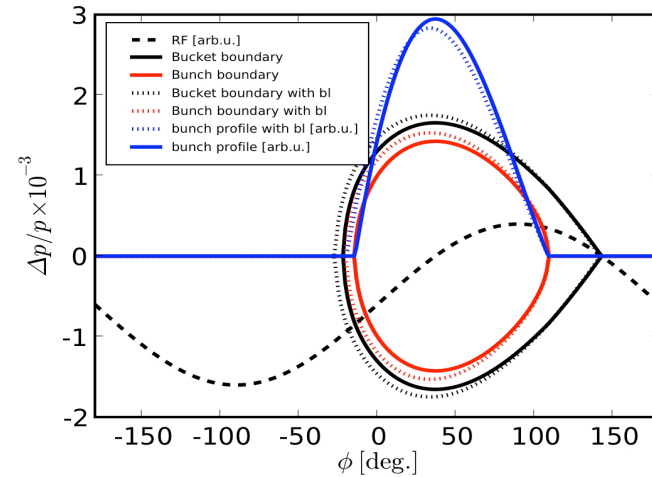
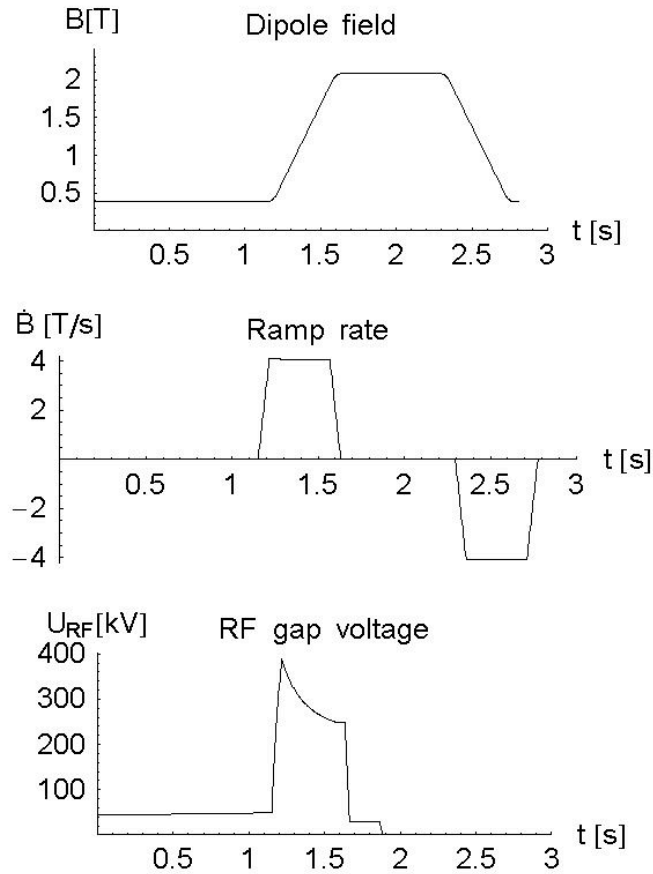


	FAIR design	today (e.g. M.Kirk, H.Damerou)
SIS 18 injection	$10^{-3}$	$1-2 \times 10^{-3}$
SIS 18 extraction	$4 \times 10^{-4}$ (dilution factor: 2)	$1-2 \times 10^{-3}$ (dilution factor: 5)
SIS 100 injection	$4 \times 10^{-4}$	$1-2 \times 10^{-3}$

The budget for longitudinal blow-up in SIS 18/100 is tight (factor 2-3) !

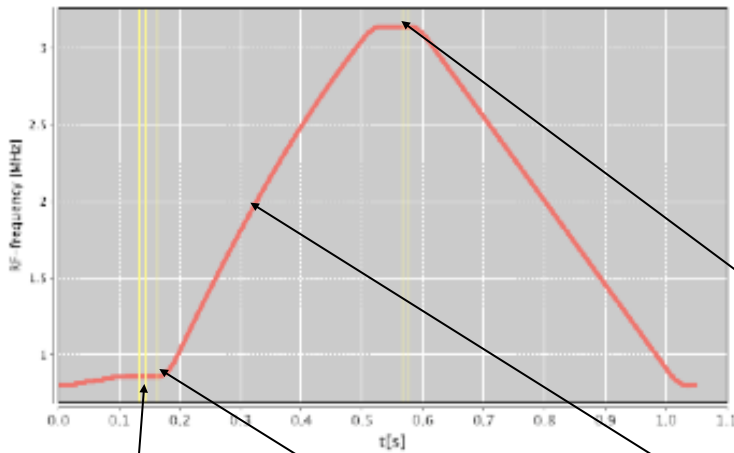
The present blow-up (> factor 5) in SIS 18 is not acceptable for FAIR !

# Acceleration in SIS100

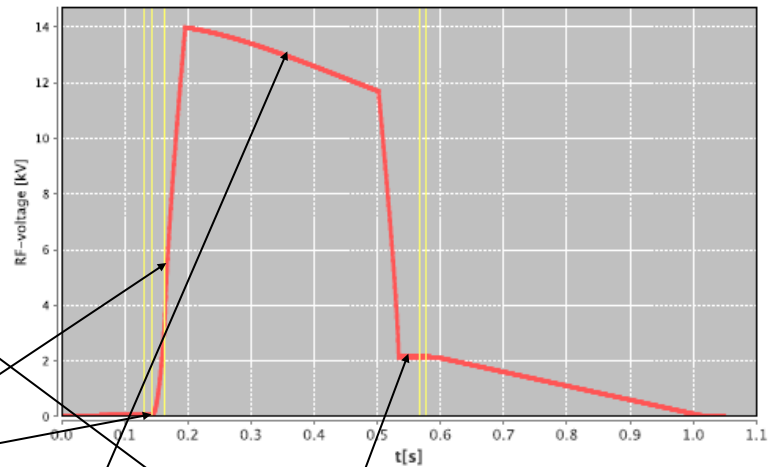


# Realistic Rf Cycles (fast extraction)

Rf frequency cycle



Rf voltage cycle



Injection

Rf capture

Acceleration

Flat-top

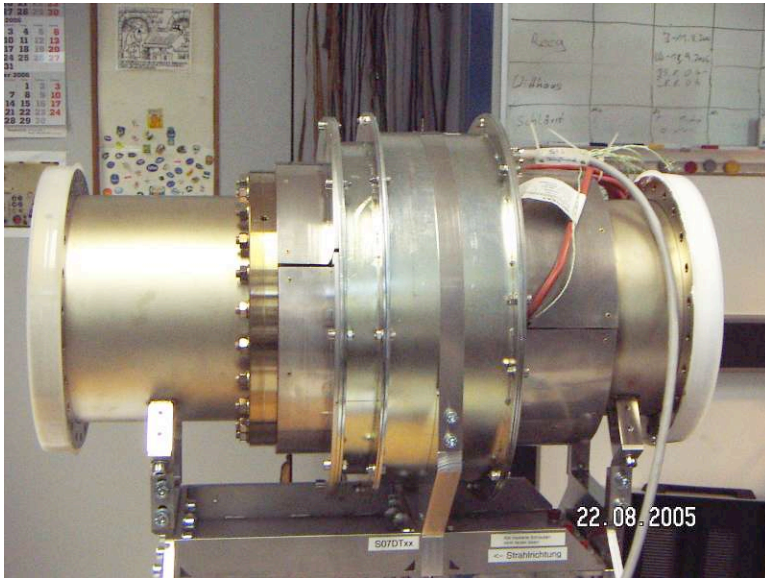
$dB/dt = \text{const}$

$\eta$ : decreasing

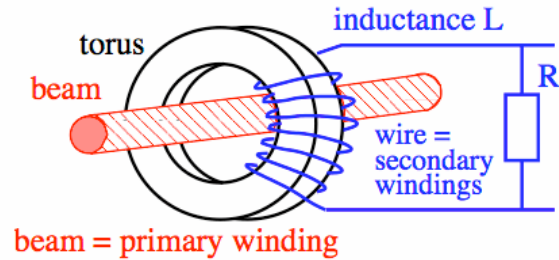
$\epsilon_L$ : decreasing

# Broadband Current Transformers

Transformer with beam pipe for average (dc) and bunch (ac) current



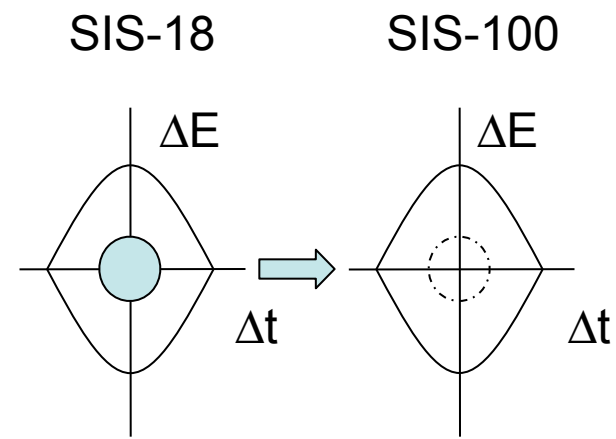
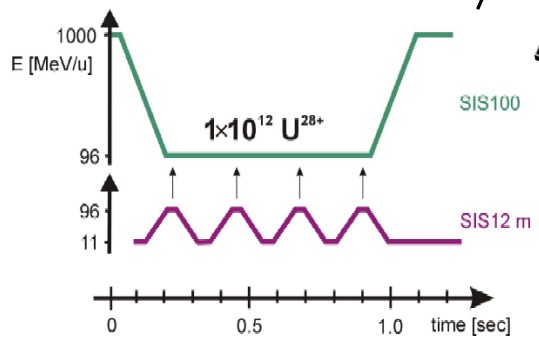
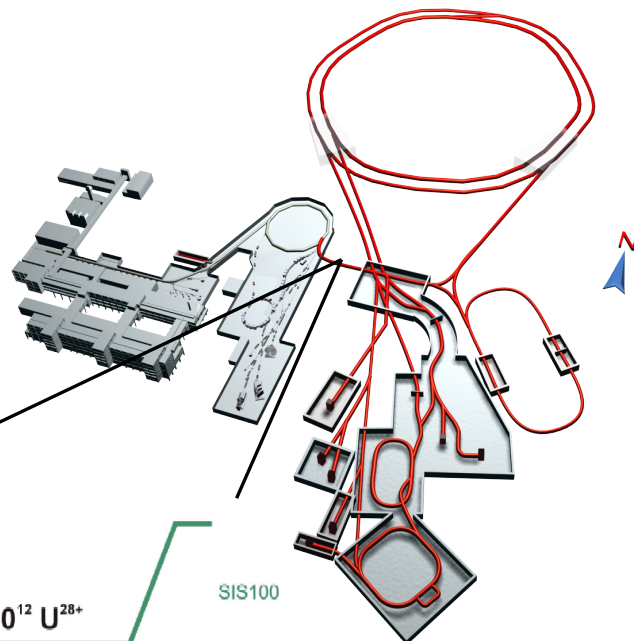
$$V = L \frac{dI_b}{dt}$$



- BERGOZ Instrumentation, France
- Bandwidth: 1 kHz ~ 650 MHz
- Rise time: 540 ps
- cost: 8000 Euro



# SIS18 > SIS100 Bunch to Bucket Transfer



Extraction kicker is triggered according to beat between SIS18 and SIS100 bucket phase.

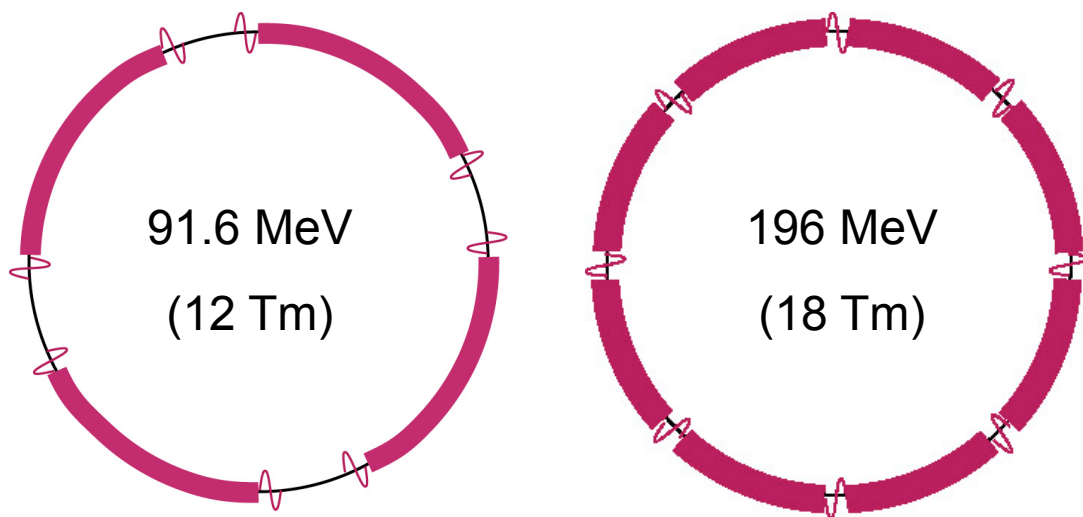
Circumference relation must be slightly non-integer.



# Barrier Bucket Injection (temporary concepts)

Barrier Bucket System in SIS18 :

Debunching before transfer to SIS100



Barrier bucket injection system in SIS100 :

2 individual systems of MA loaded cavities

15 kV at 2,4 MHz

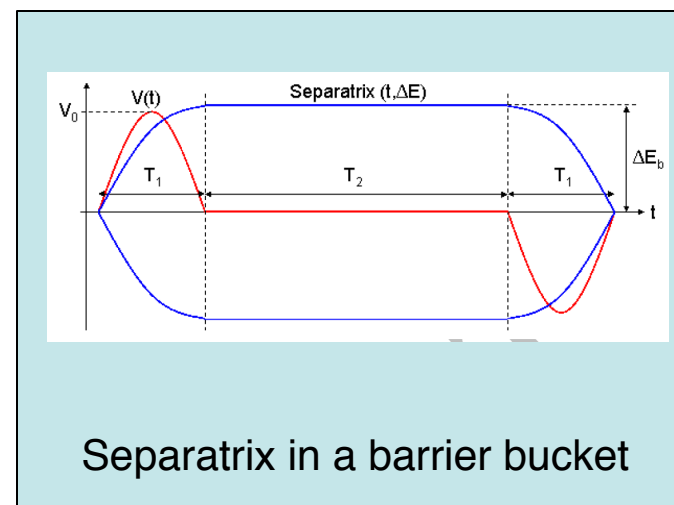
(Cavity under development at GSI)

Inc. Tune Shift  $dQ \propto 1 / (\beta^2 \gamma^3)$

and  $dQ \propto I_{spitze} / \langle I \rangle$

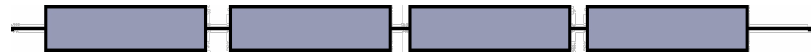
$dQ < 0.25$  (1 Sek.)

Synchrotron  $\neq$  Storage Ring

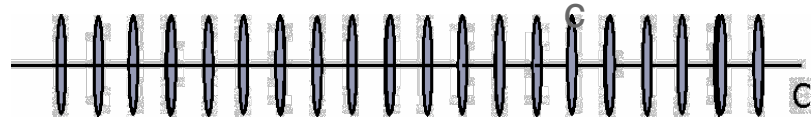


# Rf Cycle in SIS100 (temporary concepts)

**Barrier Bucket Injection**  
(RF System 1)



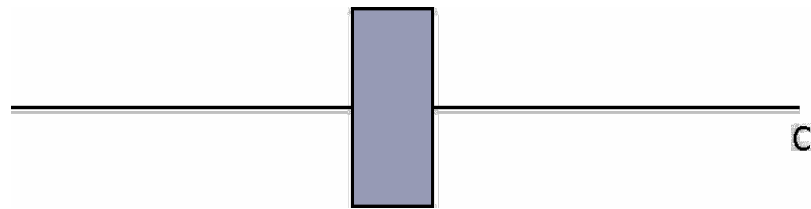
**Acceleration at  $h = 20$**   
(RF System 2)



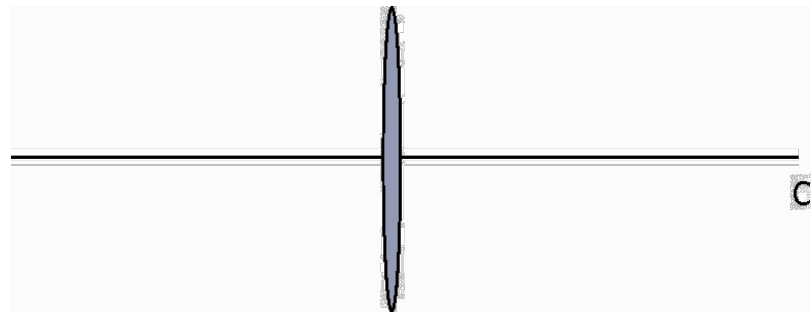
**Debunching in Barrier Bucket**  
(RF System 1)



**Precompression in Barrier Bucket**  
or Harmonic Potential  
(RF system 1/2)



**Compression at  $h = 2$**   
(RF system 3)





# Rf Systems in SIS100

- **Acceleration Systems**

18 ferrite loaded Cavities

$V_{a,tot} = 300 \text{ kV}$  - Frequency Range : 2.28 – 5.34 MHz

- **Compression Systems**

38 MA-loaded Cavities

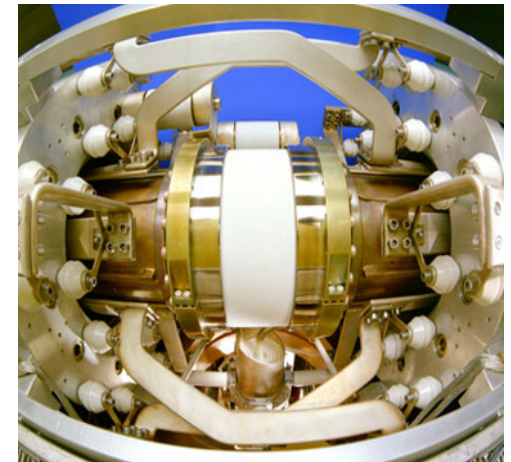
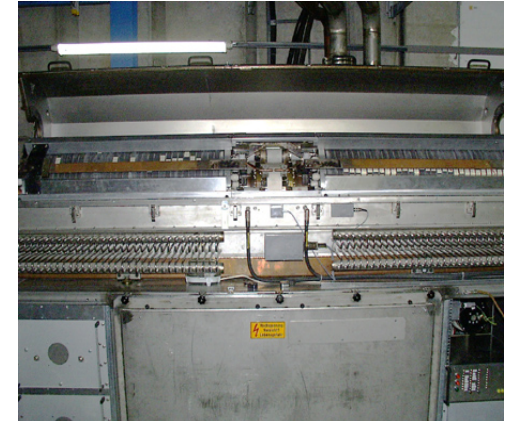
$V_{c,tot} = 1.3 \text{ MV}$  – Frequency Range : 465 kHz ( $\pm 70$ )

- **Barrier Bucket Systems**

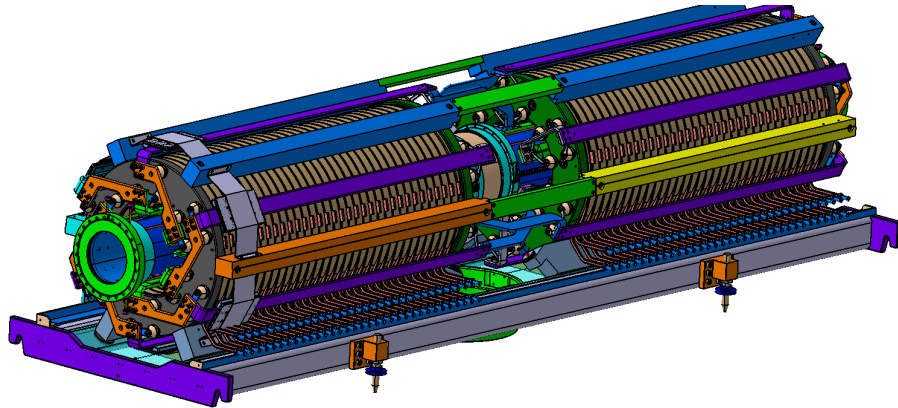
Broad band MA-loaded Cavities

$V_b = 2 \times 15 \text{ kV}$  – Frequency = 2.4 MHz.

Total Length of RF-Systems ~ 120 m  
( 11% of Circumference )



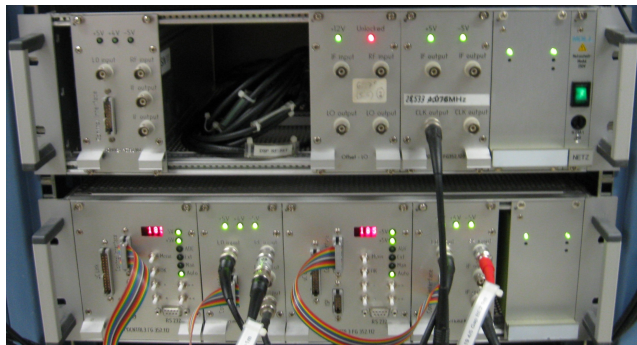
# SIS18 and SIS100 Inductively Loaded Rf Cavities



Ferrite loaded SIS18 acceleration cavity



MA loaded SIS18 bunch compressor cavity



Phase control unit for two harmonic operation of the ferrite loaded SIS18 cavities and the MA loaded h=2 cavity

New LLRF modules developed:

Flexible Direct Digital Synthesis (DDS) unit for RF signal generation,

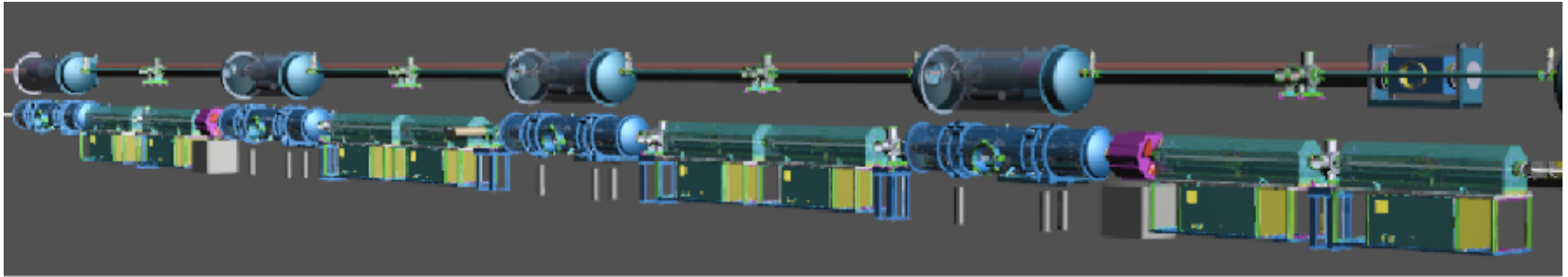
Programmable distribution amplifier for the switching of RF reference signals,

FPGA interface board that distributes information from the central control system via optical networks to the target devices (e.g. to the DSP system for closed-loop phase control)

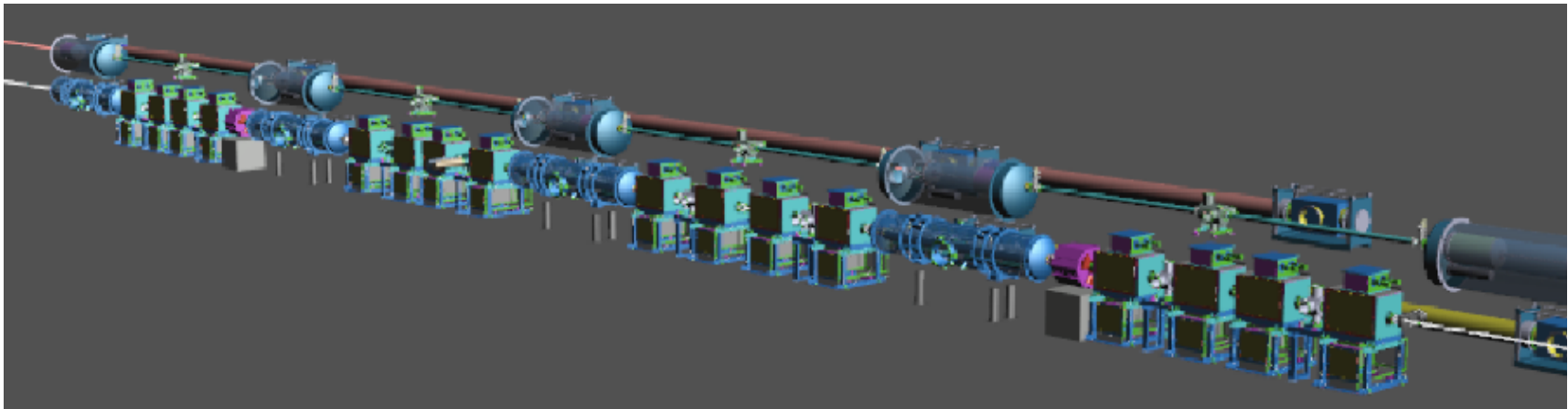
# Rf System Developments

- Digital Cavity Control
  - Synchronization of cavities > Increased longitudinal acceptance at high ramp rates and rigidities
  - Synchronization of cavities running at different harmonics
  - Bunch phase feed back
- Longitudinal feed back system (separate broad band cavity)
  - Damping of coupled bunch modes
  - Damping of instabilities in the coasting beam phase
- Fast semiconductor gap switches for low and high duty cycle cavities

# SIS100 Rf Sections



Rf acceleration section

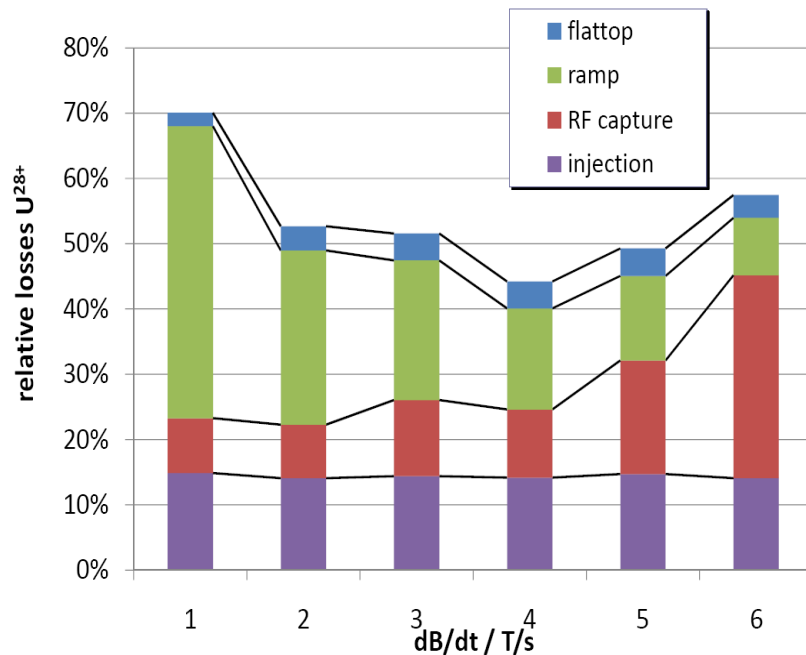


Rf compression section



# SIS18 - U<sup>28+</sup> Beam Loss at High Ramp Rates

Insufficient bucket area creates beam loss. The bucket area depends on the phase of the synchronous particle which increases with increasing ramp rate.

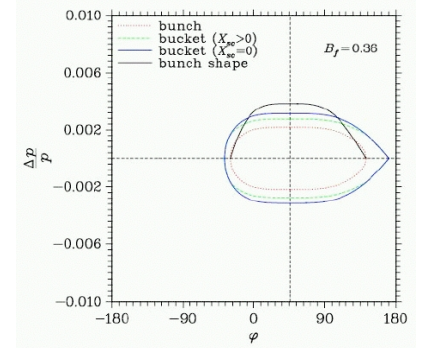
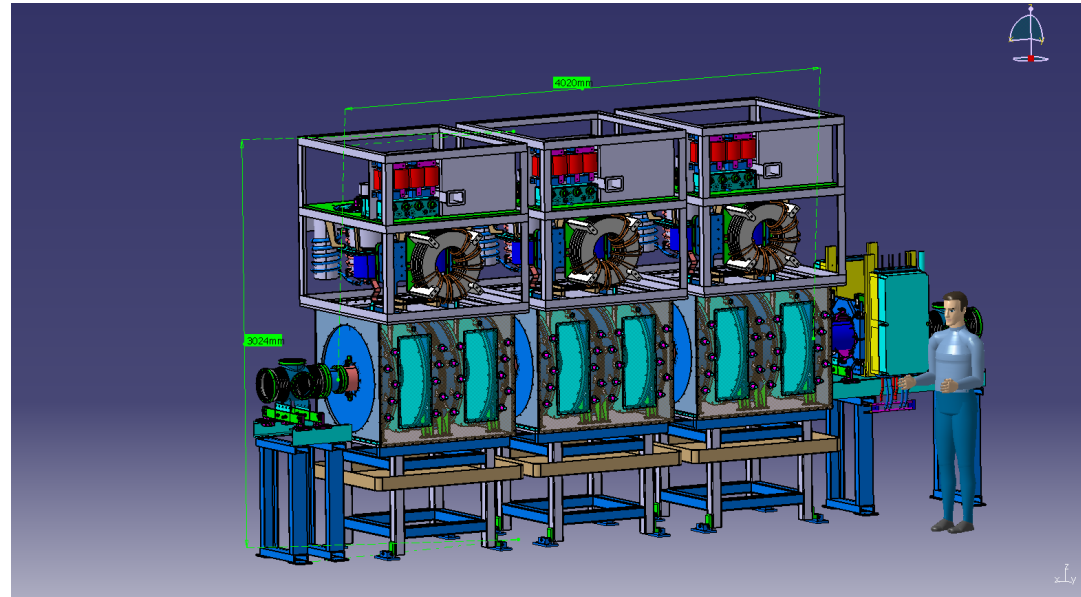


$$V_{acc,min} = V_0 \sin \phi_s = 2\pi R_{syn} \rho_B \times dB / dt$$

Fractional loss of different mechanisms during fast ramping

# New h=2 Acceleration System

- Sufficient Rf voltage for fast ramping with low charge state heavy ions
  - $U^{73+}$  acceleration with 4 T/s ( $2 \times 10^{10}$  ions)
  - $U^{28+}$  acceleration with 10 T/s ( $2 \times 10^{11}$  ions)
- Sufficient bucket area for minimum loss (30 % safety)
- Flat bunch profile (high  $B_f$ ) for lower inc. tune shift
  - two harmonic acceleration*
  - $h=4$  (existing cavity) and  $h=2$  (new cavity)*
- Compatibility with SIS100 Rf cycle



Design study for the new, high duty cycle MA loaded, h=2 acceleration cavities (0.5 MHz - 50 kV)

# Dual Harmonic Operation

Dual harmonic test operation with the existing SIS18 cavities at  $h=4$  and  $h=8$  with the new LLRF system.

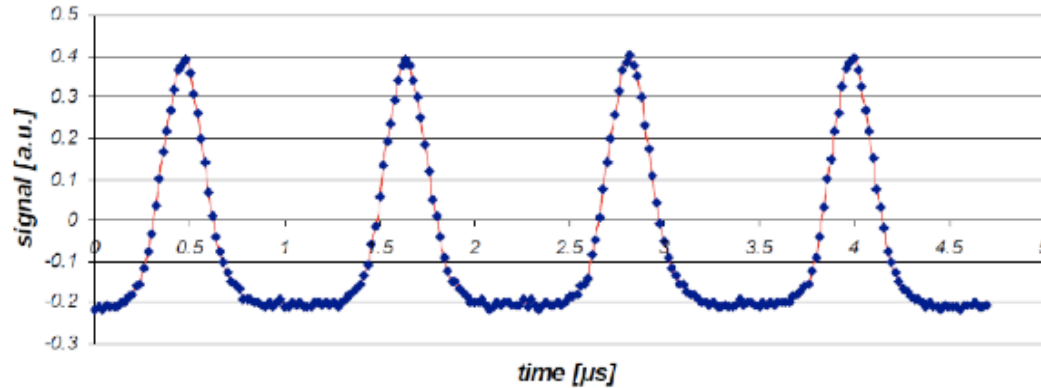


Figure 4: Bunch Profile Single-Harmonic Operation (B. Zipfel)

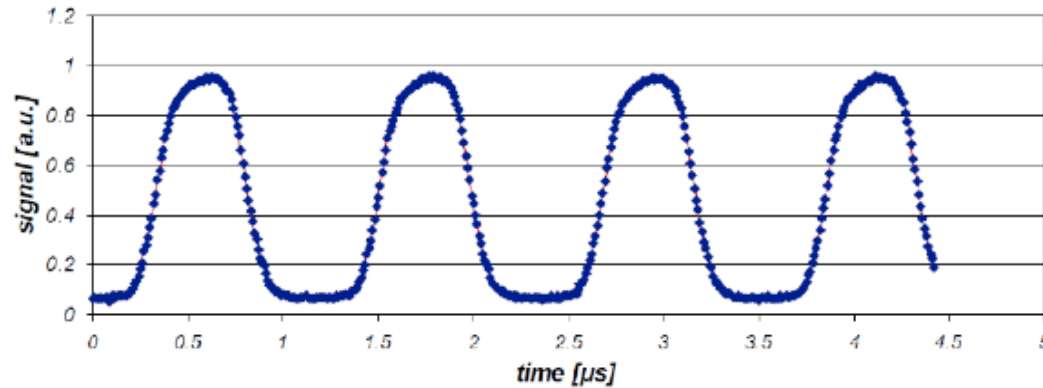


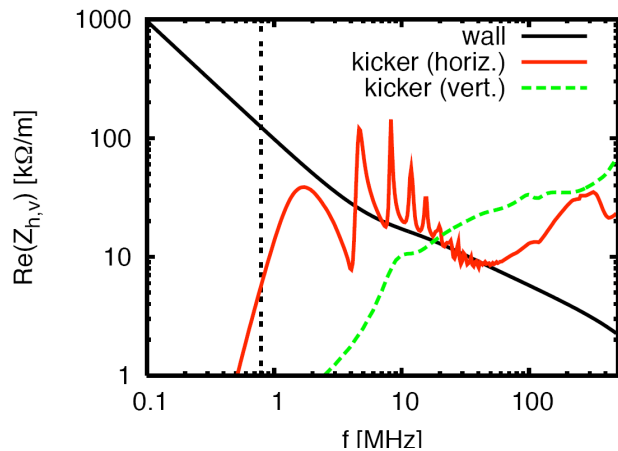
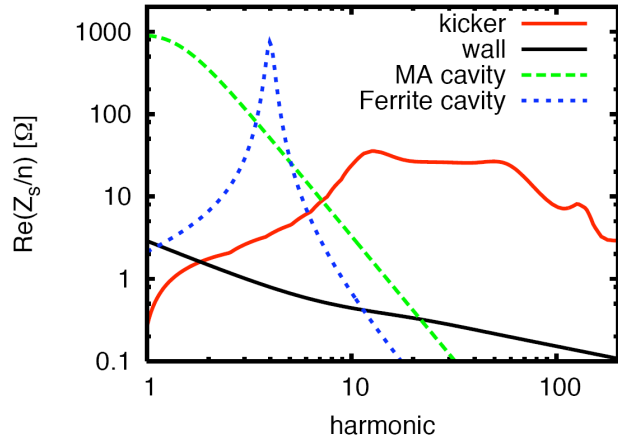
Figure 5: Bunch Profile Dual-Harmonic Operation (B. Zipfel)





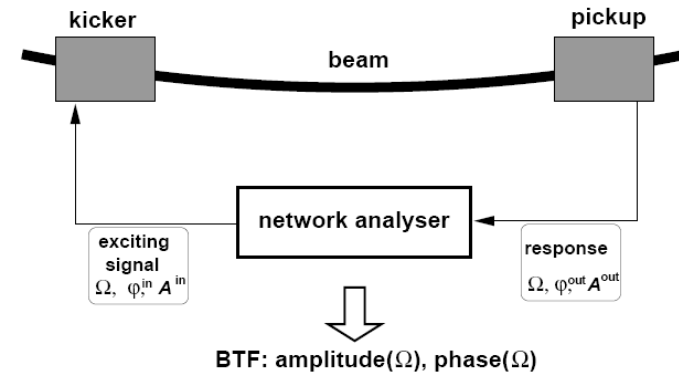
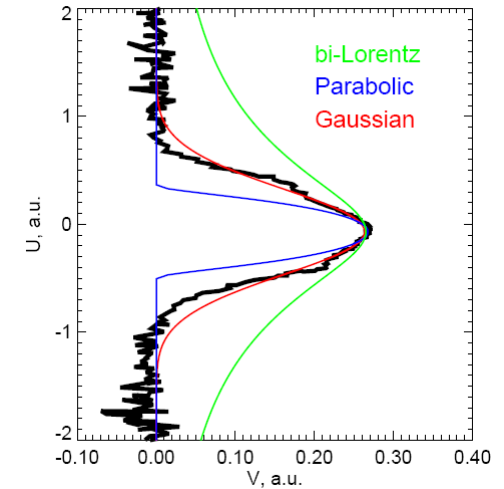
# Single Bunch Generation

# Impedance and Beam Stability



Measurement of

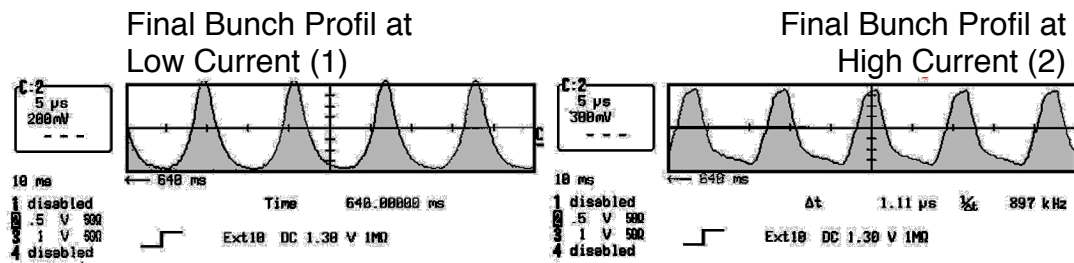
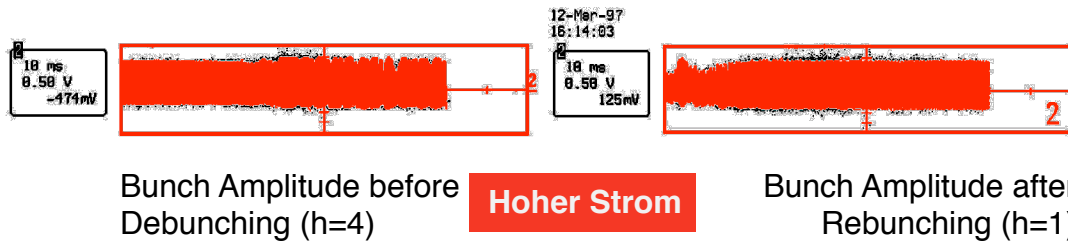
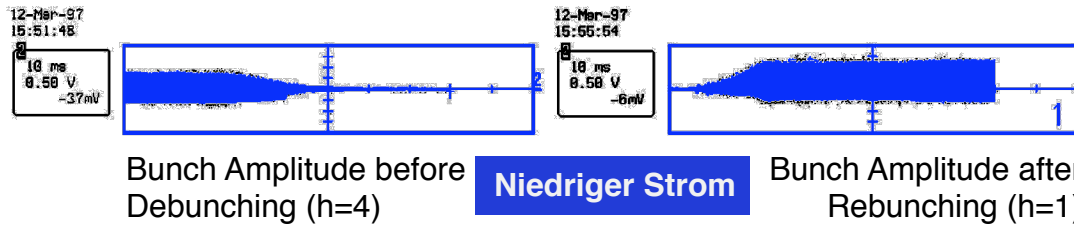
- Beam stability diagram
- Betatron tune  $Q$ ,
- Chromaticity  $\xi$
- Momentum spread  $dp/p$



Goal: Determination of impedance spectrum - Measurement of kicker- and resistive wall impedance and their influence on beam stability

# Beam Instability in the Coasting Beam Phase

Cavity impedance : 3 kOhm – Resistive Wall Impedance : 1.5 kOhm



Ne<sup>10+</sup>-beam  $1 \times 10^9$  and  $2 \times 10^{10}$  Teilchen

- Fast detuning the cavity during or after debunching
- Operation with slightly bunched beams during slow extraction
- Broad band feed back system (under development)

# Bunch Merging

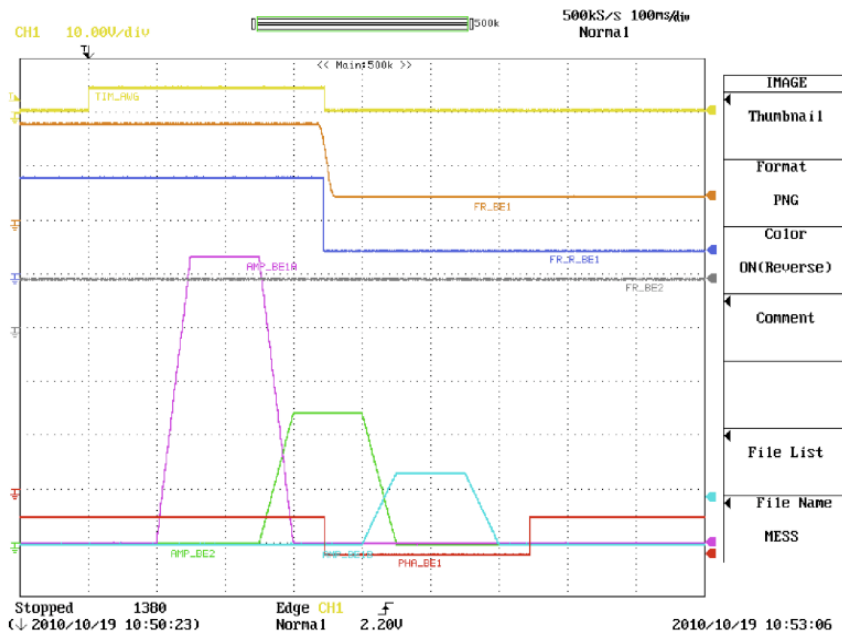


Figure 2: Oscilloscope plot of the generated ramps

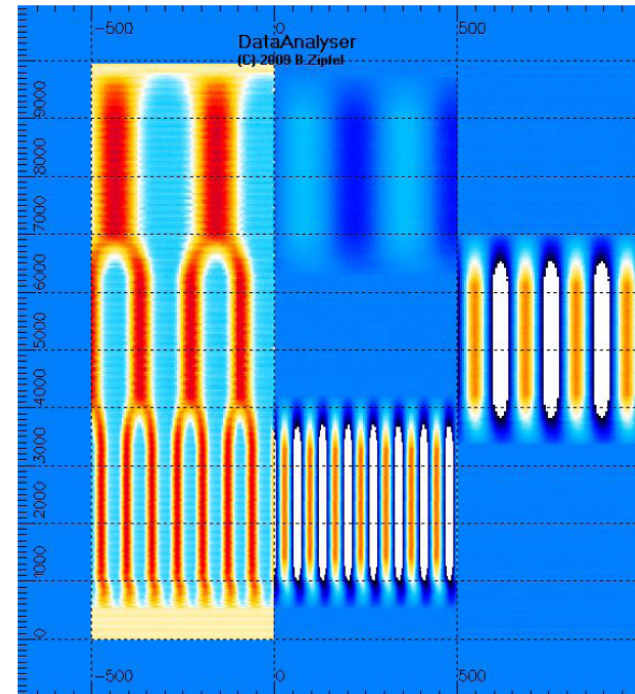


Figure 4: Waterfall plot (leftmost section: Beam signal (beam phase monitor S05DP3P), section in the middle: Gap voltage S02BE1, right section: Gap voltage S08BE2)

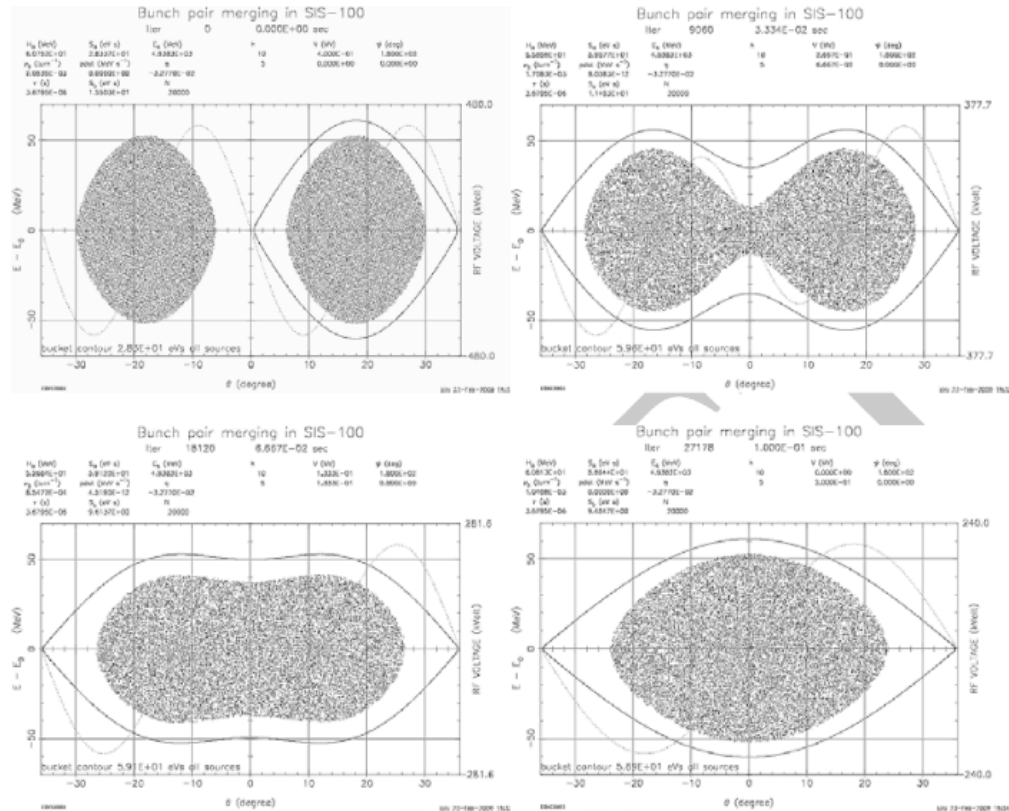
The cavity S02BE1 was temporarily operating at  $h=4$  and temporarily at  $h=1$ , the cavity S08BE2 was permanently operating at  $h=2$ .

The height (amplitude) of two subsequent overlapping trapezoidal ramps differs by a factor of  $\frac{1}{2}$ . This ratio was chosen in order to keep the overall bucket area (proportional to  $\sqrt{U_{RF} / h}$ ) constant.



# Proton Bunch-Merging in SIS100

**Figure 4.** Simulated phase space plots of the beam during bunch merging of 4 GeV protons. The plots below correspond to the times  $t=0$  (top left),  $t=T_{\text{merge}}/3$  (top right),  $t=2T_{\text{merge}}/3$  (bottom left),  $t=T_{\text{merge}}$ .



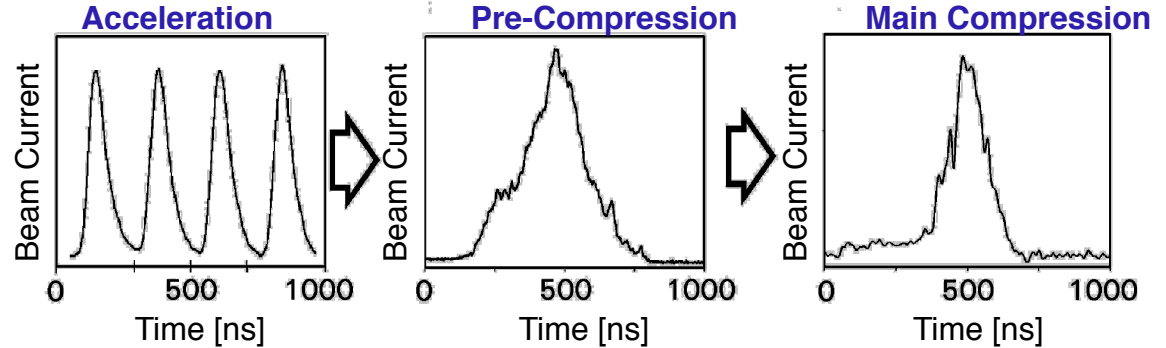
Since the synchrotron frequency at extraction level is too low, proton bunch merging (single bunch generation) in SIS100 must be performed on injection level

# Bunch Compression and Target Matching

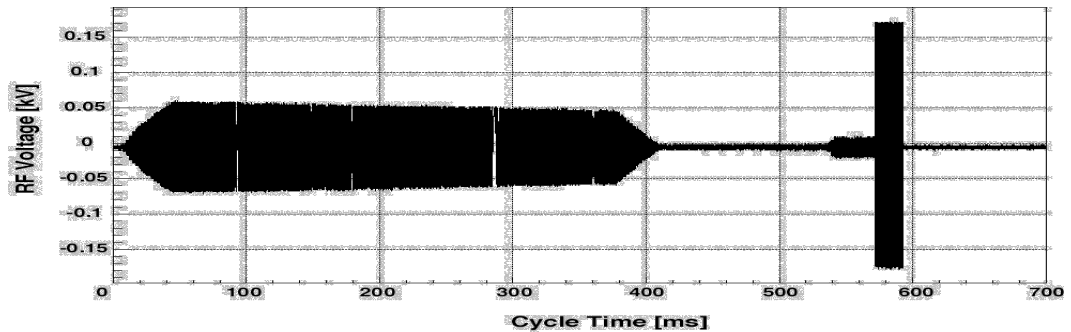


# Single Bunch Generation and Compression in SIS18

## Measured Beam Currents



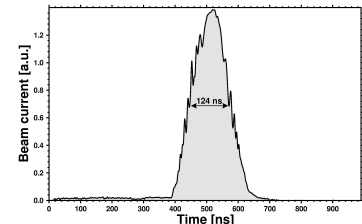
## RF- Cycle



Fast Compression  $t_{b,f} = \sqrt{(V_i/V_f)} * t_{b,i}$

Adiabatic Compression  $t_{b,f} = \sqrt[3]{(V_i/V_f)} * t_{b,i}$

Dec. 2003 : Compression of  $4 \times 10^9$  U-ions to 120 ns



# Bunch Compression in SIS18

- **Proposal (1996):**

Compression of  $U^{28+}$  at 200 MeV/u for PP experiments

Proposed compression voltage: 240 kV

- **Present Situation:**

Realized is one Rf system with: 40 kV

- **Application change:**

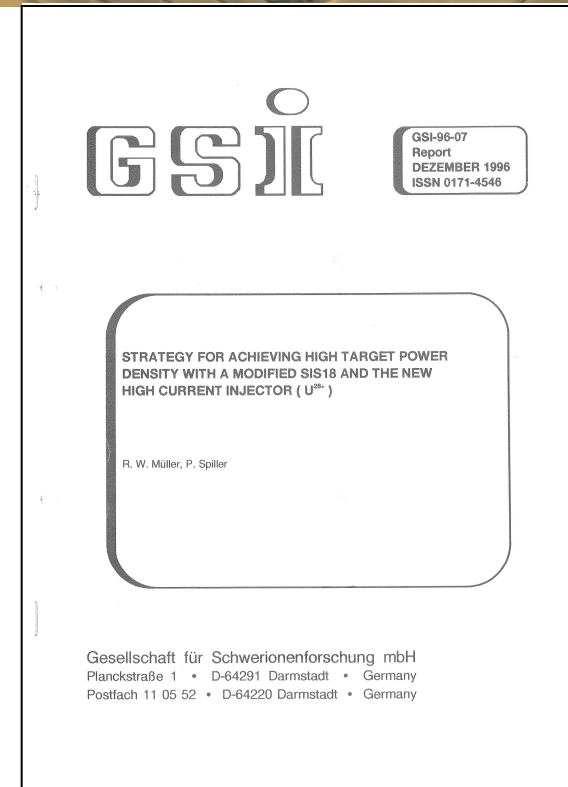
Compression of  $U^{73+}$  at 1000 MeV/u for FAIR stage 1

## Bunch Compressor is a Low Duty Cycle Cavity

Operation frequency can only be adjusted via the gap capacitor and is almost fixed.

Rf pulse length of 500  $\mu$ s just sufficient for the long compression time (1 ms)

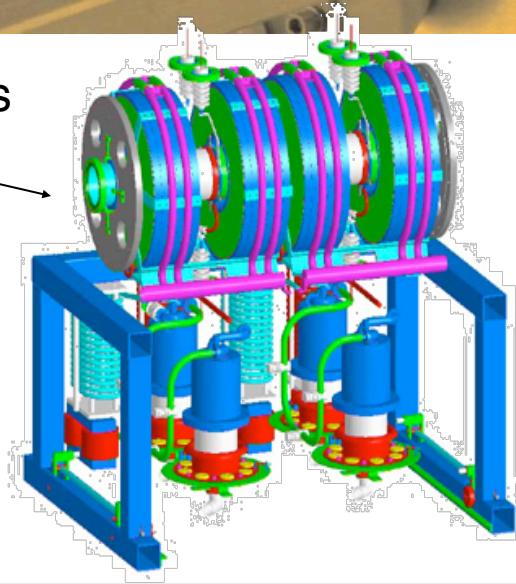
> combined compression with existing Ferrite cavities



# Compression Cavity and MA Research for SIS18

Amorphous MA Cores  
Cobalt based

40 kV per Gap

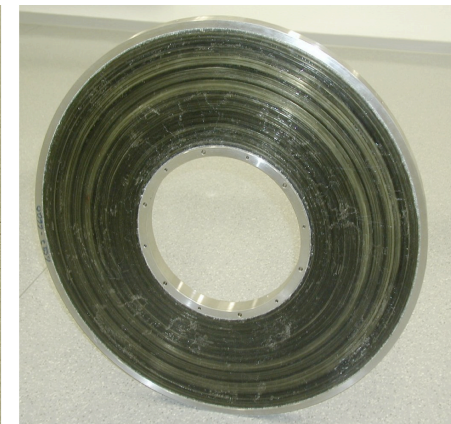


Low Duty Cycle System  
(Rf pulse 500  $\mu$ s) > air cooling

Original Goal:  $\mu$ Qf = 6 GHz

For an optimization of shunt impedance and inductivity, a large variety of nanocrystalline (Fe based) and amorphous (Co based) core materials have been investigated

(Vitrovac, Honeywell, Finemet)



# MAGNETIC ALLOY (MA) versus FERRITE

## Properties of MA - Materials

- High saturation flux density (0.8 T) (higher gap voltage)
- Linear permeability  $\mu(B)$
- Constant power loss product  $1/\mu Qf$  at high flux densities
- Low power density at high voltages
- High Curie Temperature (570°C)

## Properties of Ferrites

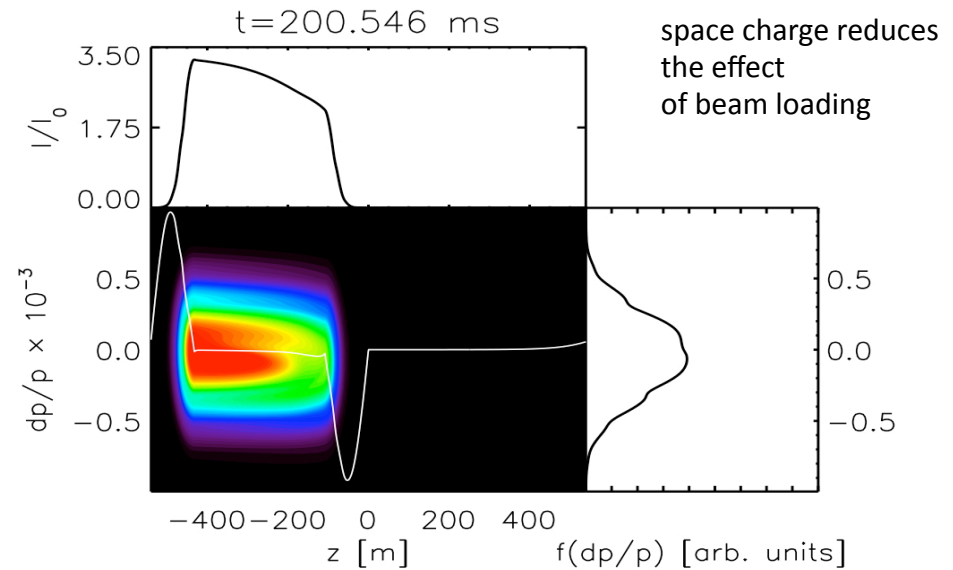
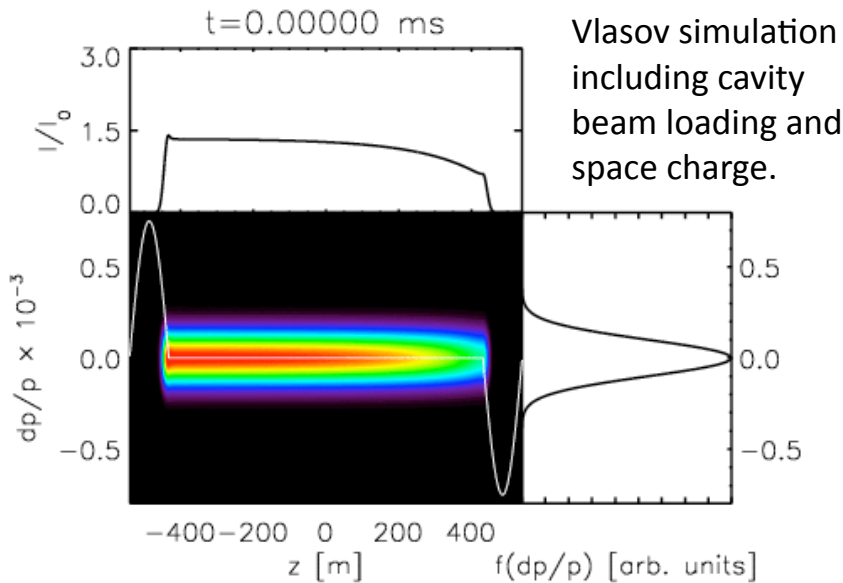
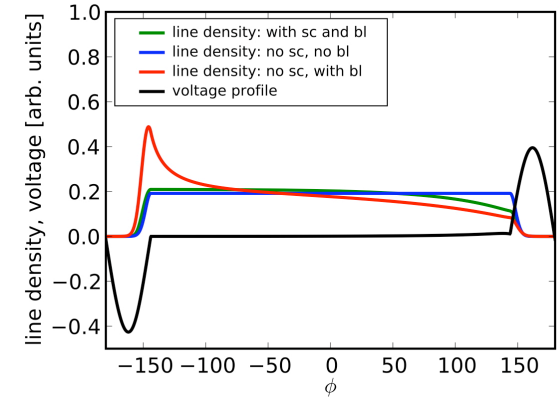
- Lower saturation flux density (0.3 T) (lower gap voltages)
- Decreasing power loss product  $1/\mu Qf$  at high flux densities
- Higher power loss density at high voltages
- Low Curie Temperaturw (100° - 250°C)

**MA - Typen:** z.B. Vitrovac (VAC), Vitroperm (VAC), Finemet (HITACHI)



# Pre-Compression in SIS100

	# cavities	$R_s/\text{cavity}$ [k $\Omega$ ]	$Q_s$	$f_{\text{res}}$
acceleration	20	3	10	$10f_0$
barrier	2	1	0.4	1.5 MHz
compression	16	1	2	1.5 MHz

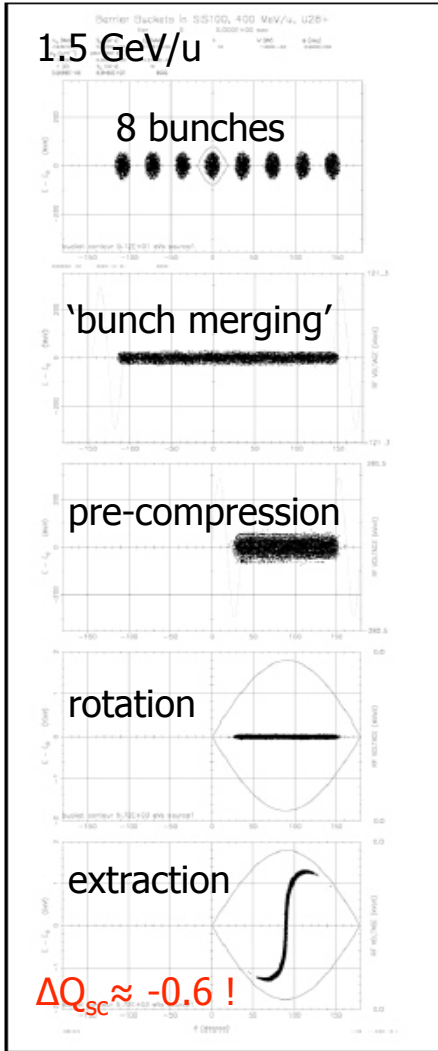


Bunch area increases by 20 % during pre-compression. Longitudinal dilution budget in SIS-100: Factor 2.

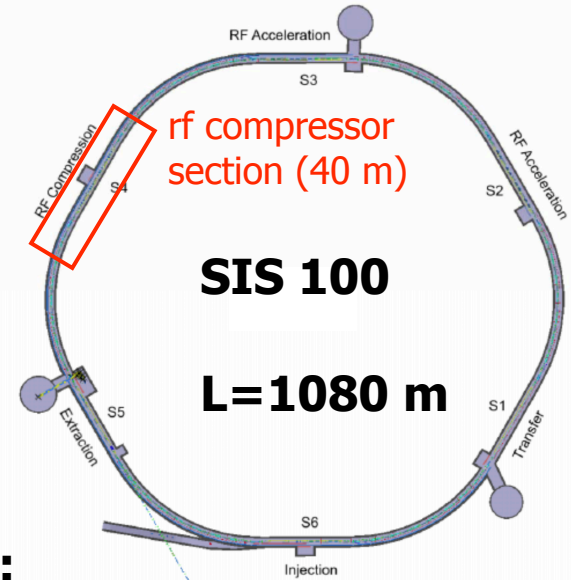
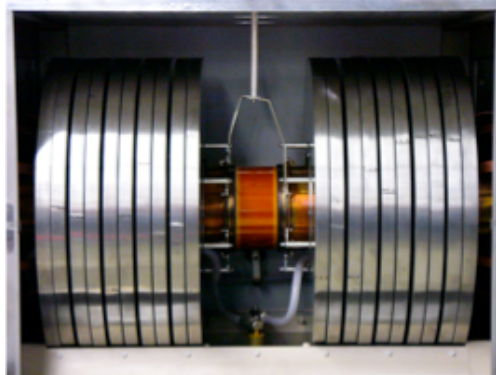


# Bunch Compression in SIS100

## Single bunch formation



SIS-18 bunch compressor loaded with 20 MA cores



## RF cavity systems in SIS 100:

	#cavities	Voltage [kV]	Frequency [MHz]	Concept
<b>Acceleration</b>	20	400	1.1-2.7 (h=10)	Ferrite
<b>Compression</b>	16	600	0.4-0.5 (h=2)	MA (low duty cycle)

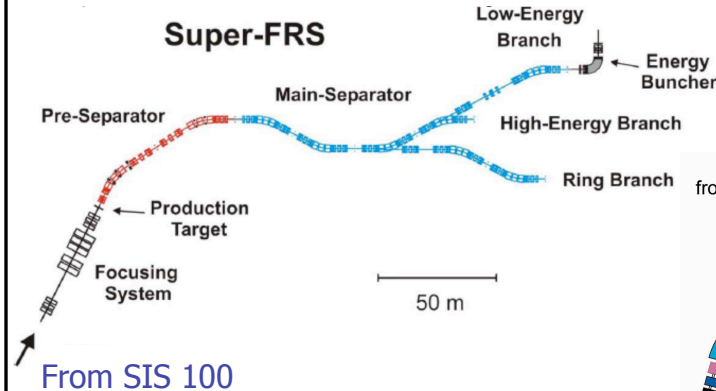
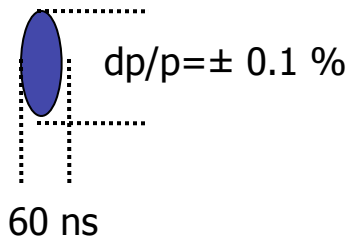
## Final bunch parameters

	Particles/bunch	bunch length
1.5 GeV/u U <sup>28+</sup>	5x10 <sup>11</sup>	60 ns
29 GeV/u p	2-4x10 <sup>13</sup>	25 ns

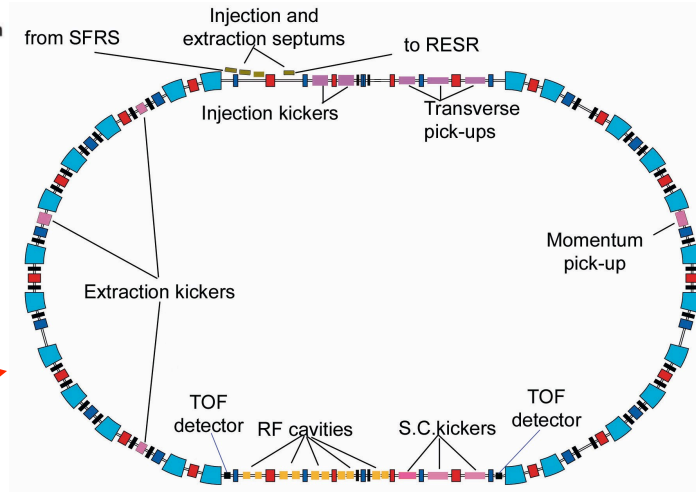
# Target Matching and Bunch Rotation

## Short SIS 100 bunches:

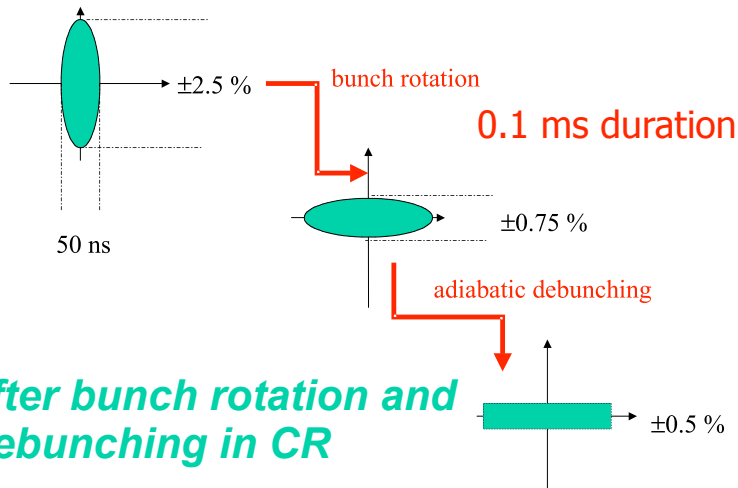
- target matching
- RIB/pbar pre-cooling



**Collector Ring (CR)**  
 circumference 212 m  
 rigidity 13 Tm



RF voltage in the CR: 200 kV (1.5 MHz)



## CR ring properties:

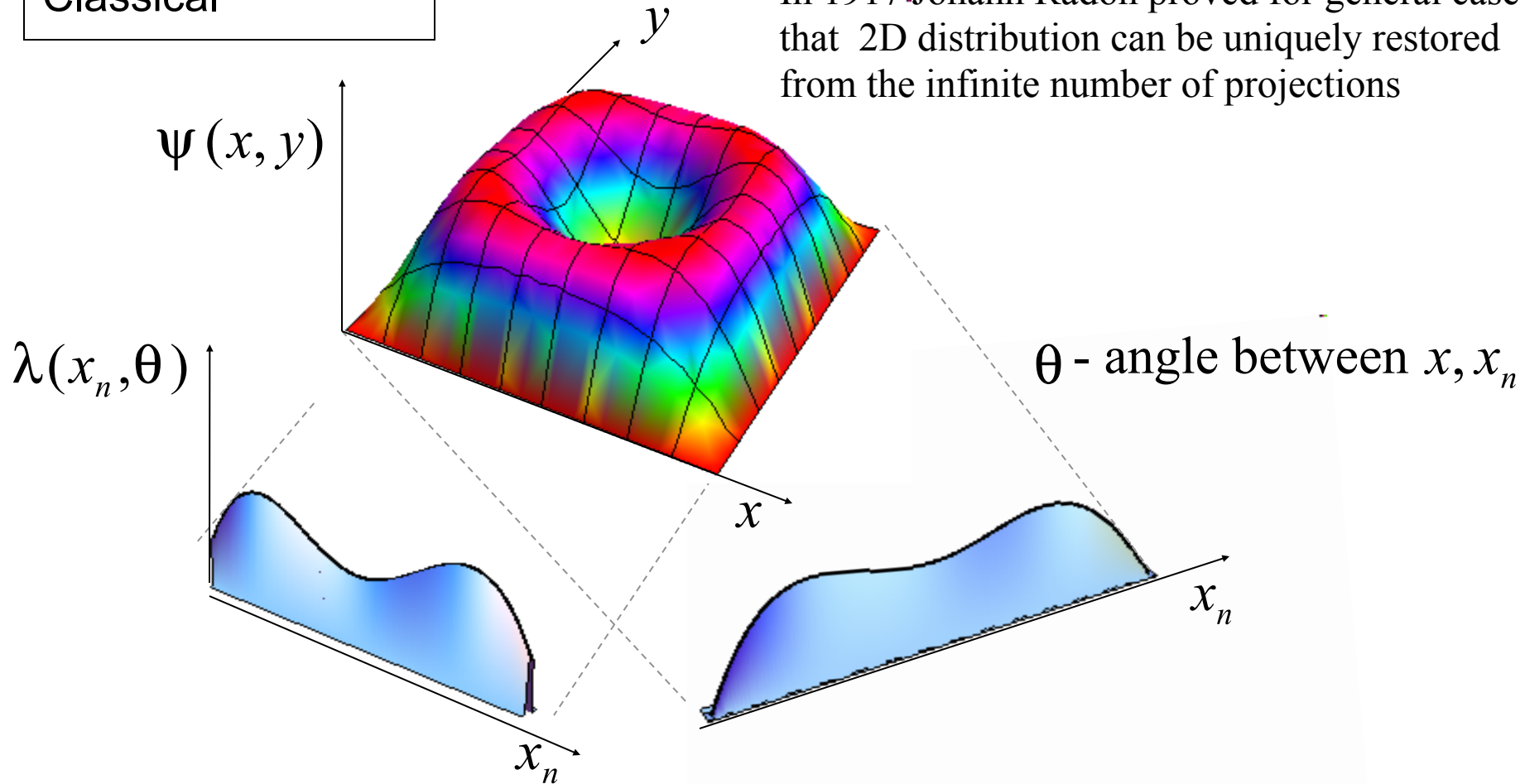
	RIB	pbar
energy	740 MeV/u	3.0 GeV
mom. accept.	$\pm 1.5\%$	$\pm 3.0\%$
transv. accept.	$200 \times 10^{-6} \text{ m}$	$240 \times 10^{-6} \text{ m}$
Cooling down time	1.5 s	10 s

M. Steck, TUOBM01 (oral)

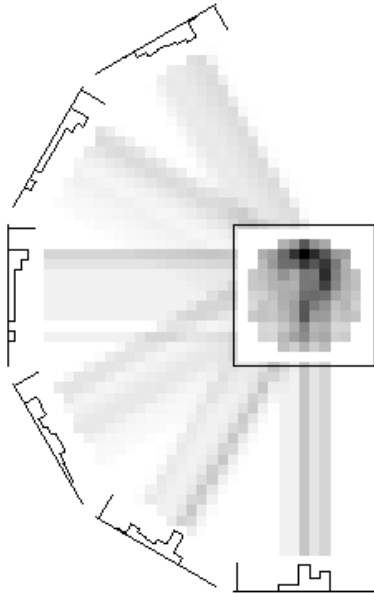
# Tomographic Reconstruction of 2D Objects

Classical

In 1917 Johann Radon proved for general case that 2D distribution can be uniquely restored from the infinite number of projections



# Longitudinal Phase Space Reconstruction

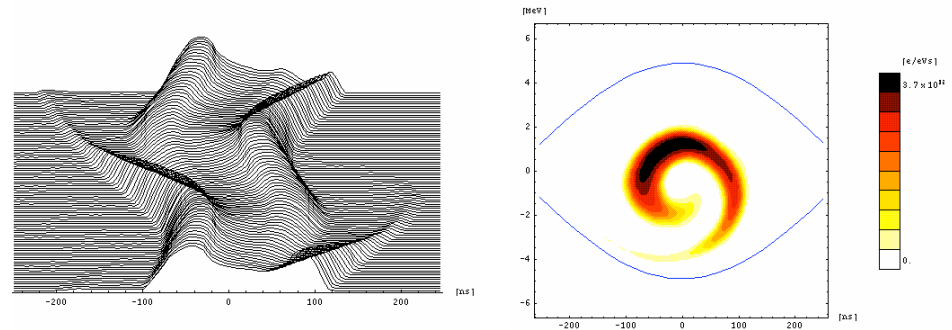


Tomographic reconstruction of phase space requires views from different sides onto the phase space distribution.

Synchrotron oscillation generates projections of the phase space distributions (line density) which can be measured by a beam transformer.

A mountain range (waterfall) plot (turn by turn monitoring of the bunch profile) can be used to reconstruct the phase space distribution.

S. Hancock, CERN

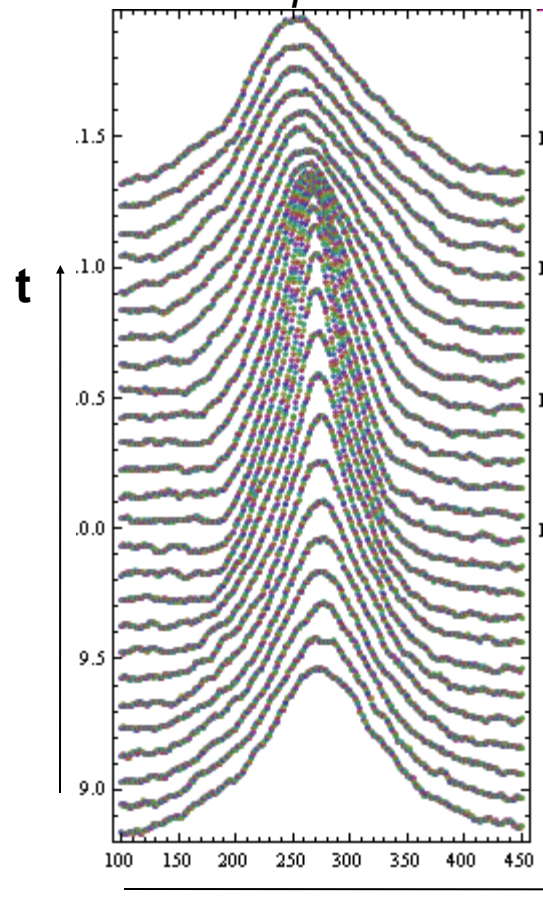




# TOMO Phase Space Reconstruction

Input parameters:  
line density in ascii format

*example*

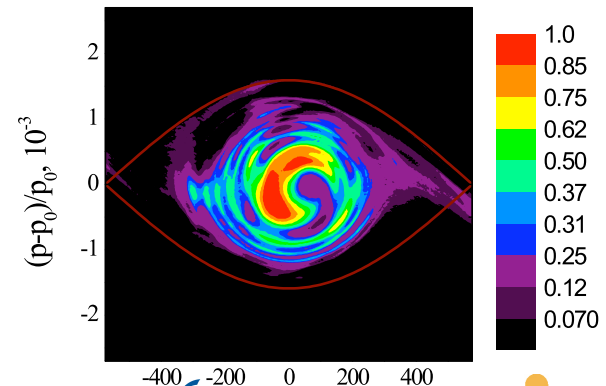


Input parameters:  
Header information of the line density file  
Machine parameters in ascii format

Number of bins  
Number of frames  
...  
Harmonic  
Voltage amplitude  
...

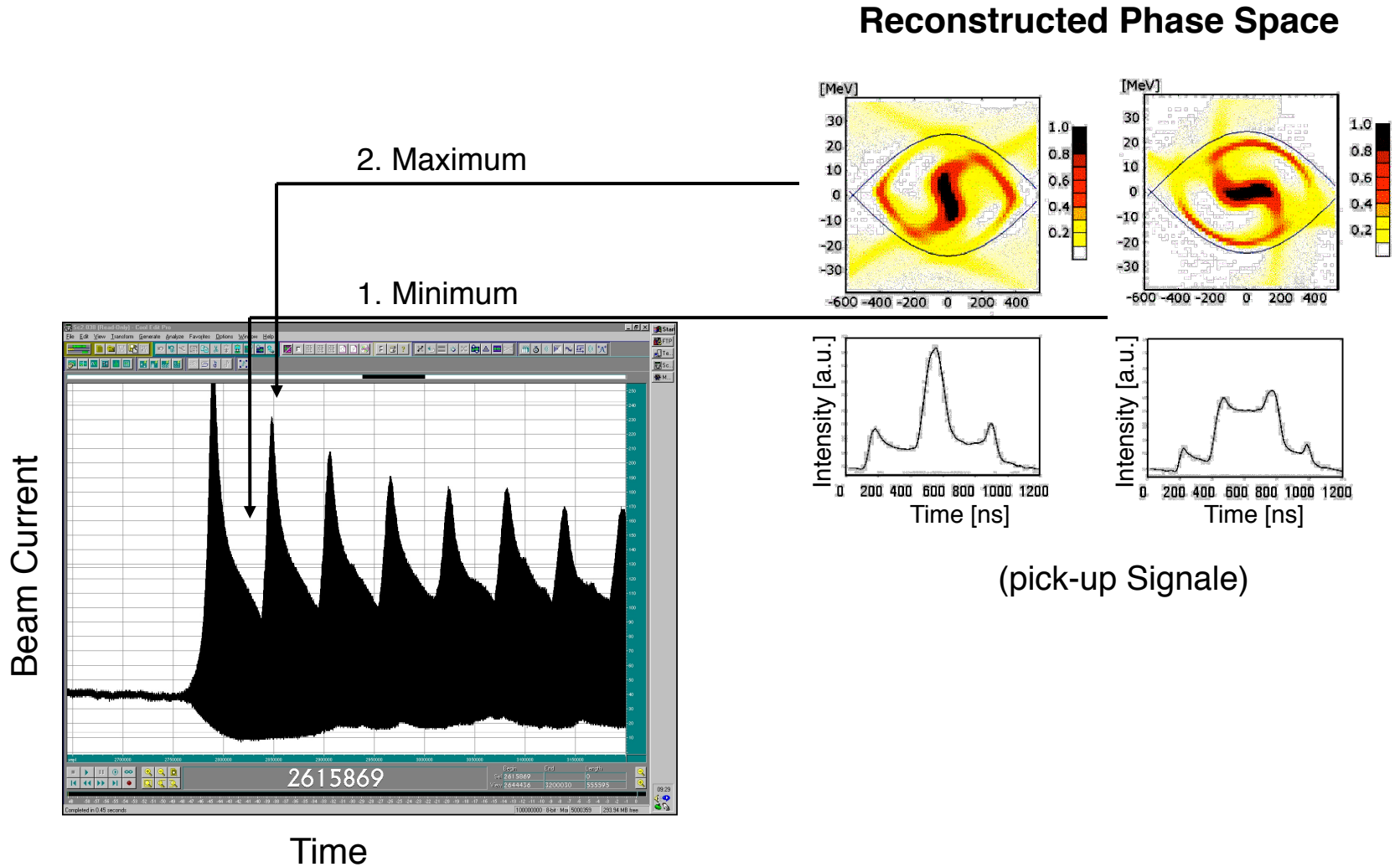
“TOMO”

*example*



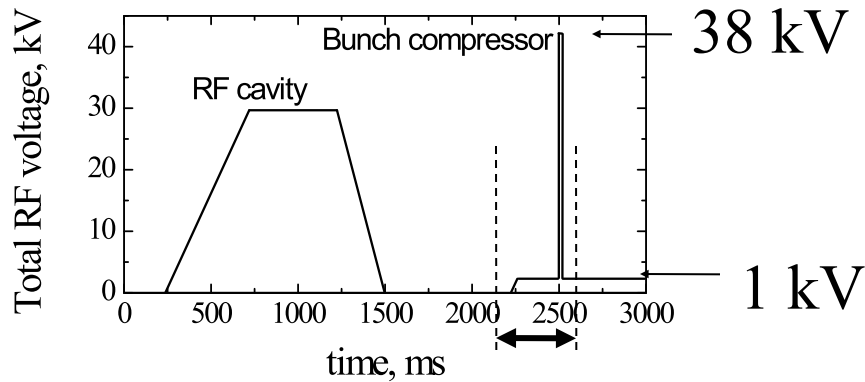


# Tomography of Bunch Compression



# Tomography of Bunch Compression

## RF cycle in SIS18

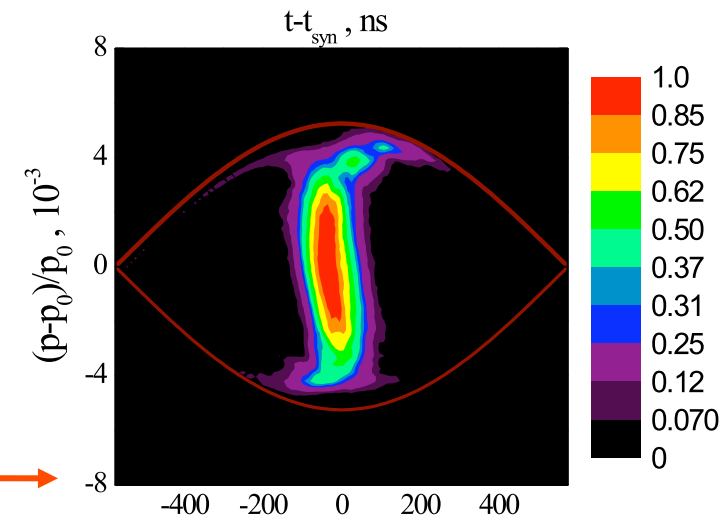
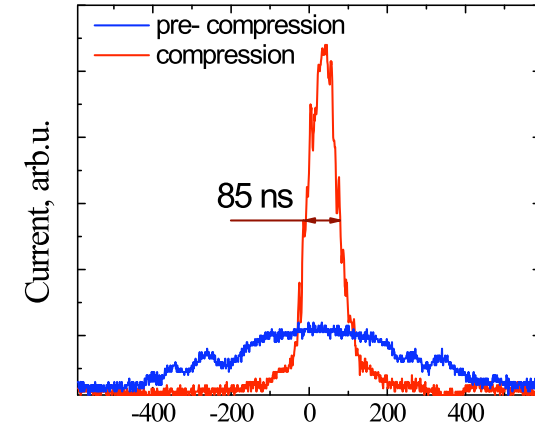


## Main parameters

Ion:	$U^{+73}$
Energy:	295 MeV/u
Pre-bunching RF amplitude:	1 kV
Bunch Compressor amplitude:	38 kV
Particles in the ring:	$1 \times 10^9$

Tomographically reconstructed phase space of the compressed bunch

## Measurements before and during compression

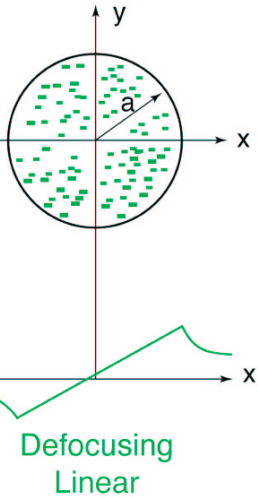




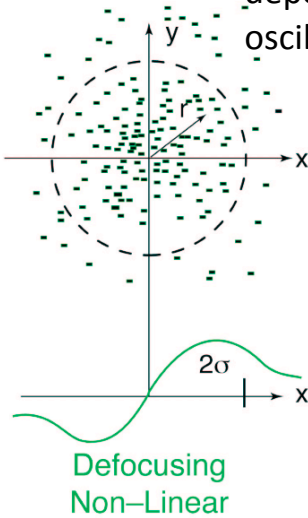
# Transverse-Longitudinal Effects

# Transverse Space Charge

Uniform



Gaussian



the space charge tune shift depends on the betatron oscillation amplitude  $a$ .

Amplitude dependent tune shift:

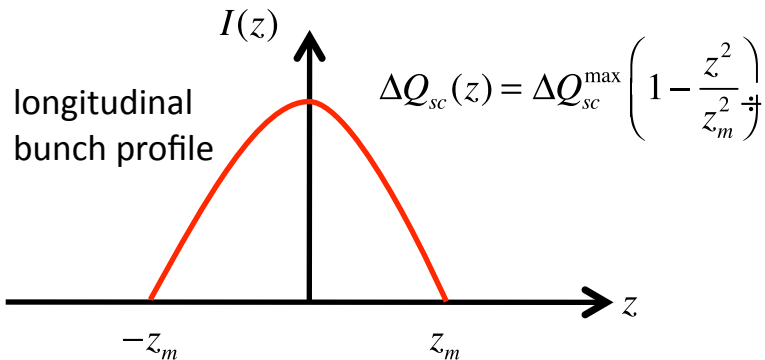
$$Q(a_x, a_y) = Q_0 - \Delta Q_{sc}(a_x, a_y, z)$$

Maximum space charge tune shift:

$$\Delta Q_{sc}^{\max} \propto -\frac{g_f}{B_f} \frac{qN}{\epsilon_x \beta_0^2 \gamma_0^3} \frac{2}{1 + \sqrt{\epsilon_x/\epsilon_y}}$$

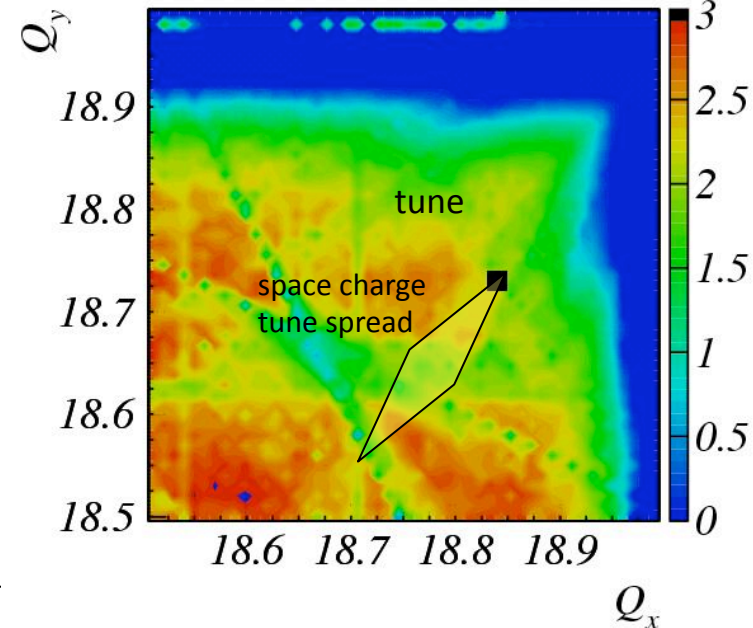
$$g_f = 1 - 2 \quad (1: \text{uniform}, 2: \text{Gaussian})$$

Space charge force changes along the bunch:

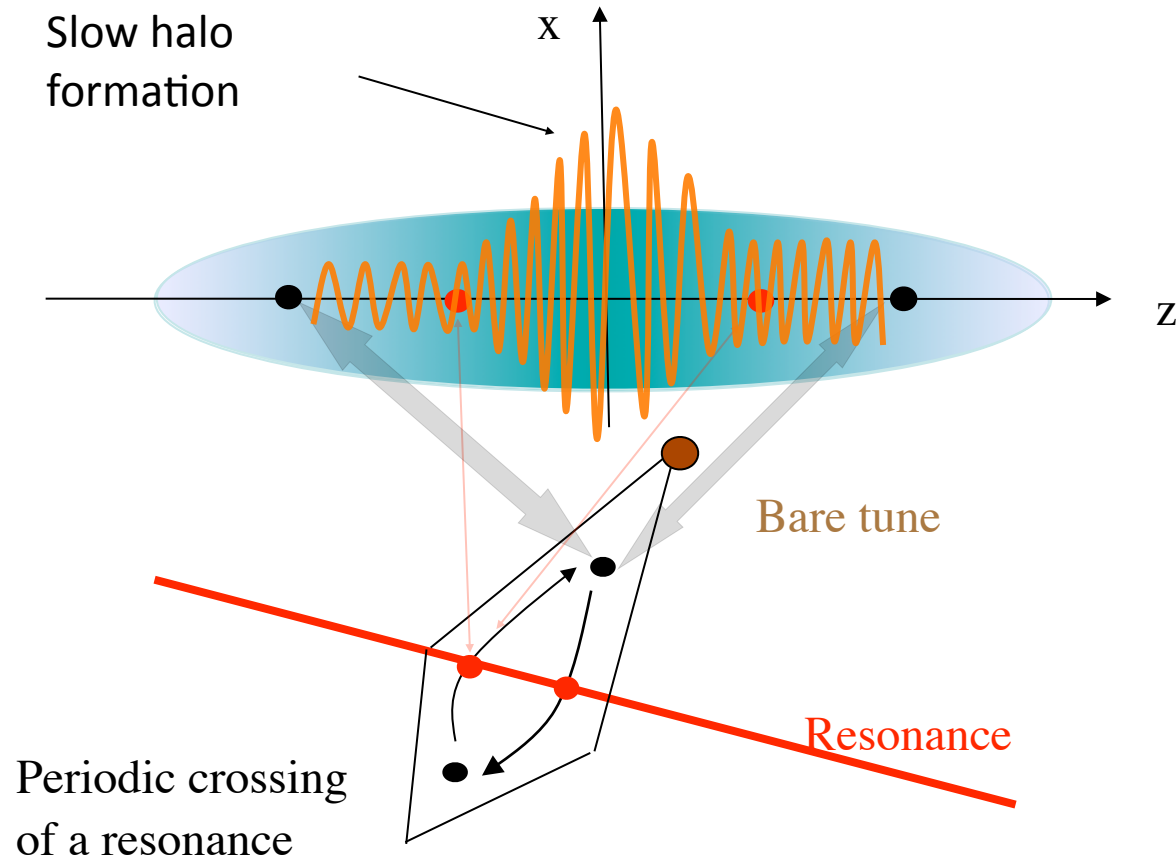


DA scan for SIS-100

DA / σ



# Beam Loss by Resonance Trapping





# Bunch Profile Reformation by Resonances

Dual harmonic operation was supposed to reduce beam loss by resonance trapping.

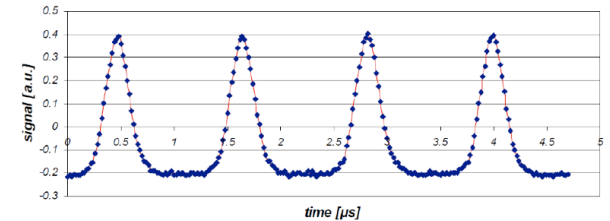
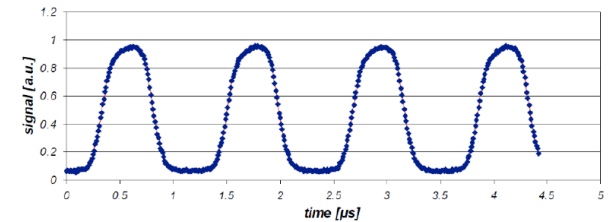
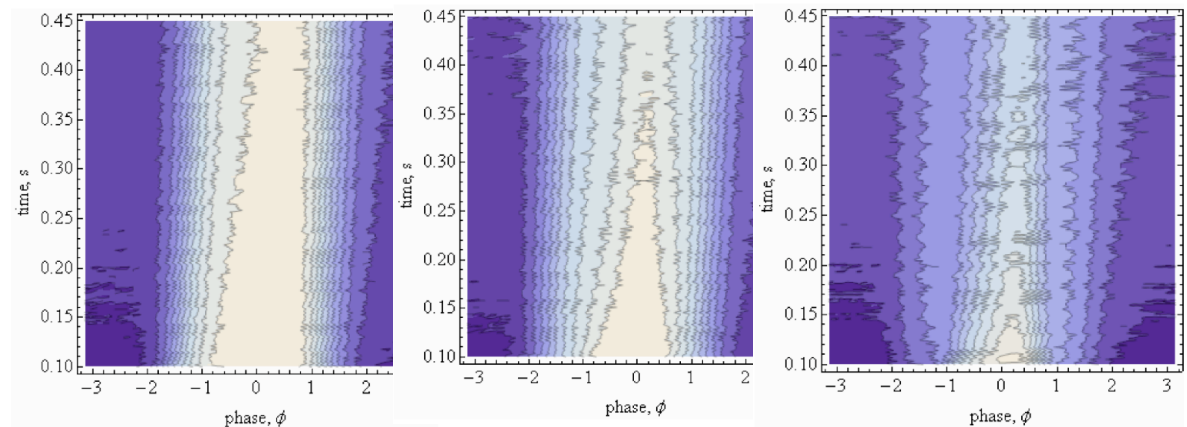


Figure 4: Bunch Profile Single-Harmonic Operation (B. Zipfel)



„single harmonic bunch“

Flat, dual harmonic bunch



Different working points

# Acceleration

The bucket area  $A_0$  becomes reduced by factor  $\alpha_s(\phi_s)$ .

$$A_B = A_0 \alpha_s(\phi_s)$$

The bucket factor  $\alpha_s(\phi_s)$  is given by the numerical solution of the elliptic integral

$$\alpha_s(\phi_s) = \frac{\sqrt{2}}{8} \int_{\phi_1}^{\phi_2} \left| \sqrt{\cos\phi + \cos|\phi_s| + (\phi + |\phi_s| - \pi) \sin|\phi_s|} \right| d\phi$$